

# Experimental Searches for Charged Lepton Flavor Violation with Muons

A Fermilab lecture series on  
Physics at the Intensity Frontier  
throughout 2009

**extreme  
BEAM**

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Fermi National Laboratory

# Outline

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A Fermilab lecture series on  
Physics at the Intensity Frontier  
throughout 2009

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- Intensity Frontier and Charged Lepton Flavor Violation (cLFV)
- cLFV Physics Motivation with Muons
- Overview of cLFV Experiments with Muons
  - $\mu \rightarrow e\gamma$
  - $\mu$ -e conversion
- Experimental searches for  $\mu$ -e conversion
- cLFV of taus with neutrinos (if a time allows)
- Summary



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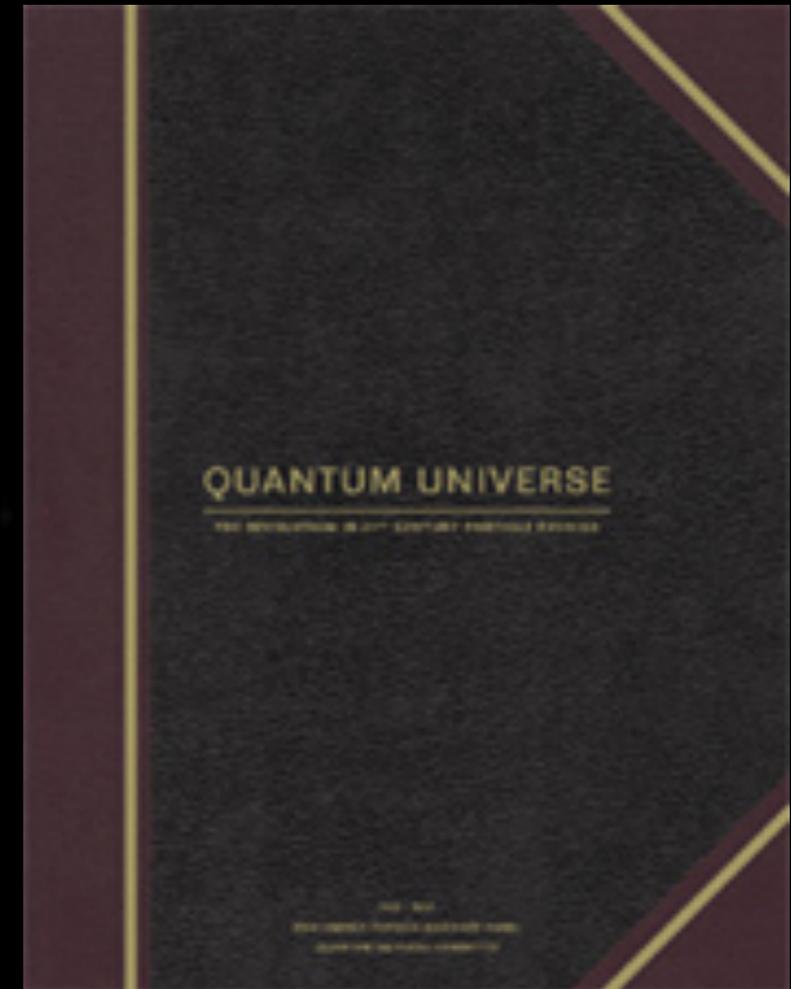
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# Intensity Frontier and Charged Lepton Flavor Violation (cLFV)

# The Big Questions to explore the mysteries of the Universe

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1. What is the origin of mass for fundamental particles?
2. Are there undiscovered principles of nature?
3. Are there extra dimensions of space?
4. Do all the forces becomes one?
5. Why are there so many kinds of particles?
6. What happened to the antimatter?
7. What is dark matter?  
How can we make it in the laboratory?
8. How can we solve the mystery of dark energy?
9. How did the universe come to be?
10. What are neutrinos telling us?

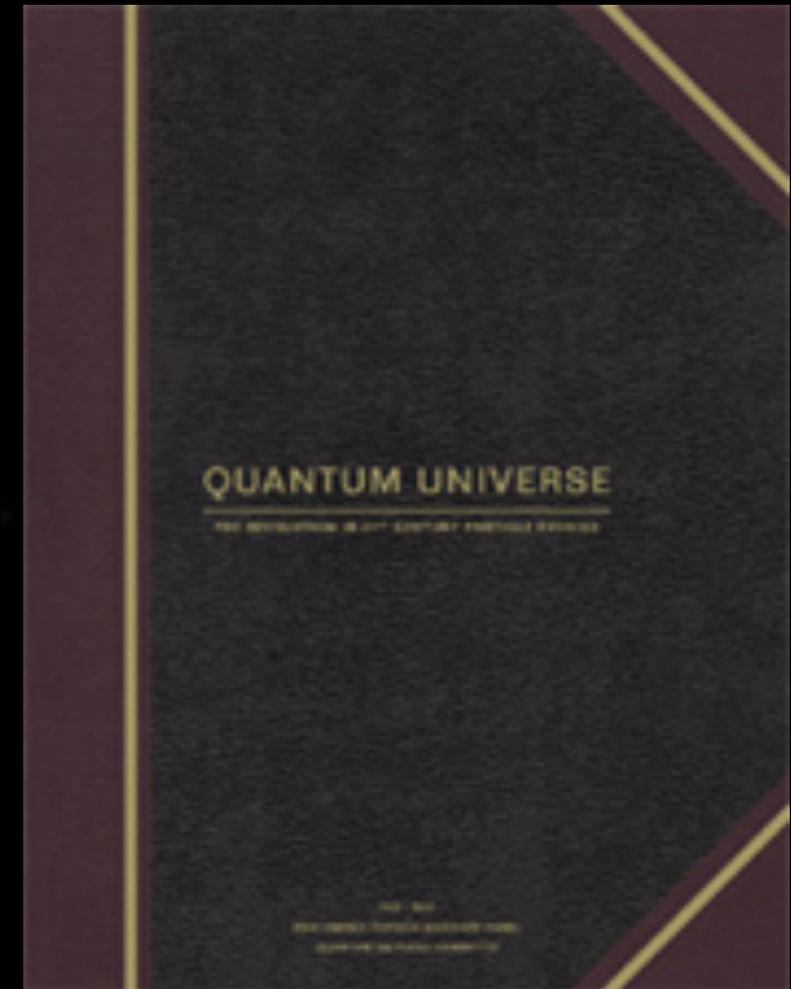


DOE/NSF high  
energy physics advisory panel

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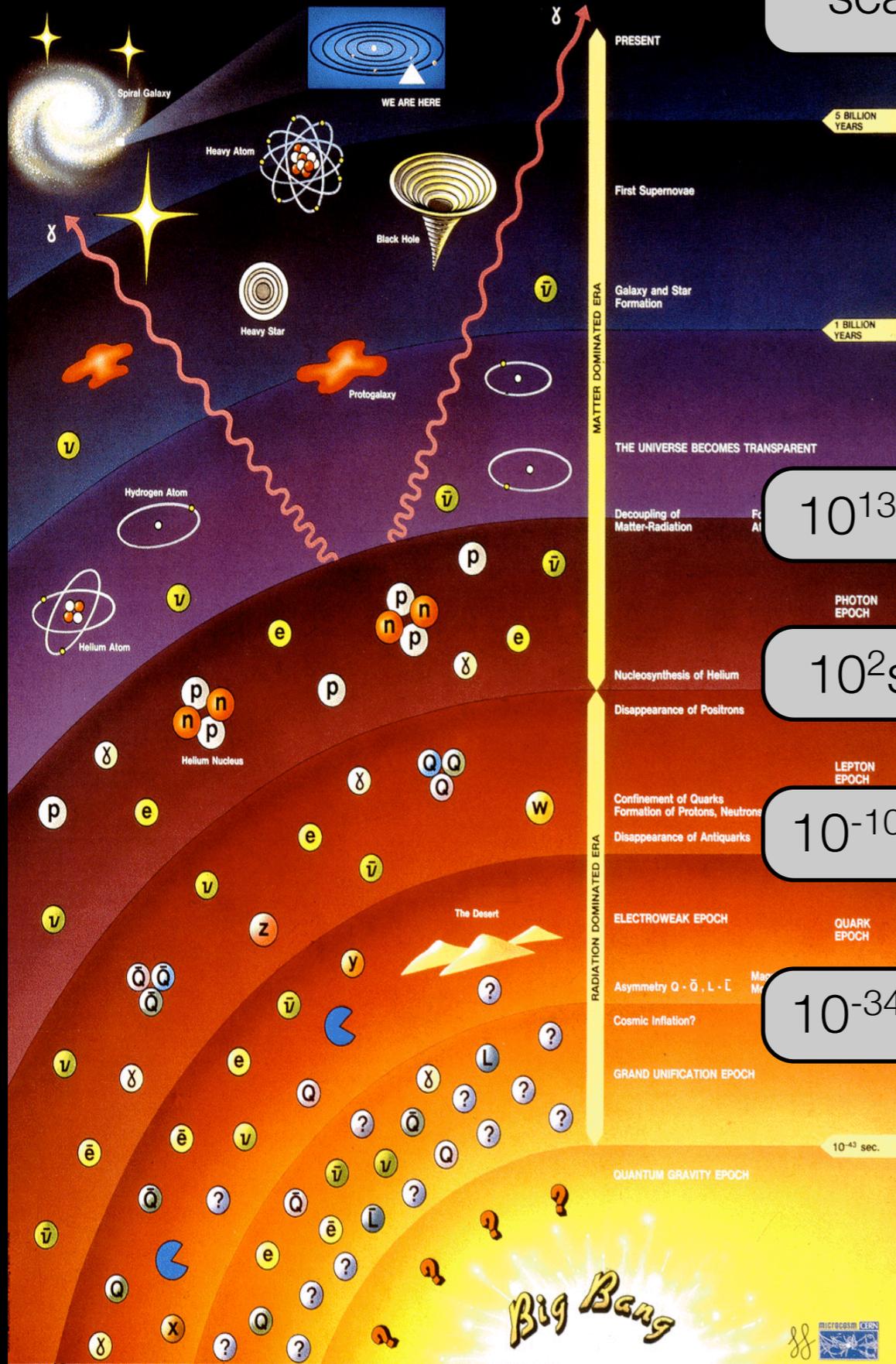
The Standard Model continues working well, but cannot answer these fundamental questions.



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energy physics advisory panel

Search for new physics at higher energy scale!

# History of the Universe



time  
scale

energy  
scale

Electroweak Epoch

Higgs particles

Supersymmetry

Unification Epoch

Grand unification of  
fundamental forces

Origin of Neutrino  
mass (RH neutrino)

Leptogenesis  
(baryogenesis)

Quantum Gravity Epoch

Superstrings

$10^{13}$ sec

$10^{-9}$ GeV

$10^2$ sec

$10^{-3}$ GeV

$10^{-10}$ sec

$10^2$ GeV

$10^{-34}$ sec

$10^{16}$ GeV

$10^{19}$ GeV

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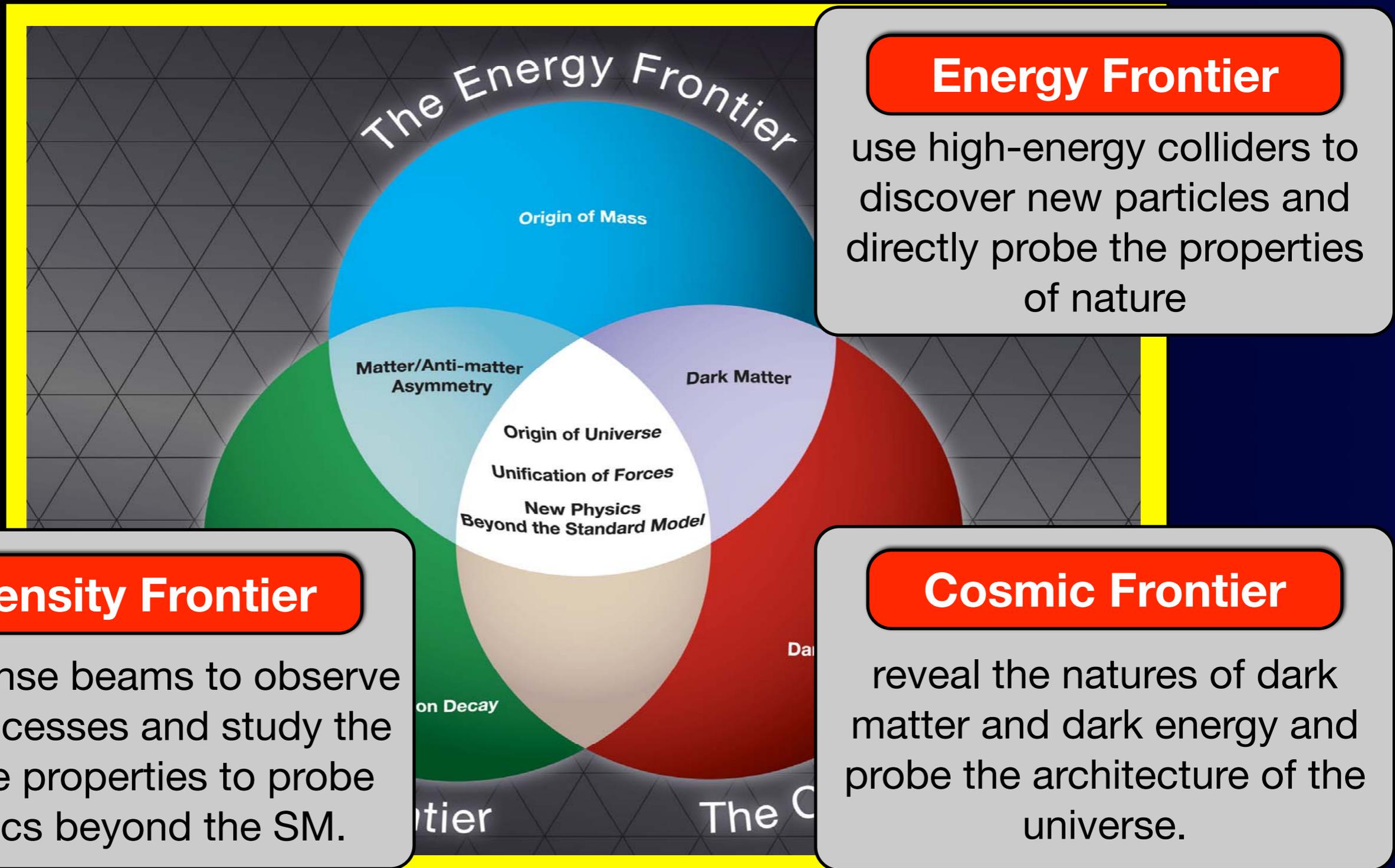
$10^{16}$ GeV

$10^{19}$ GeV

Accelerators cannot  
reach directly here.

# Tools :

## The Three Frontiers of Particle Physics



# The Intensity Frontier

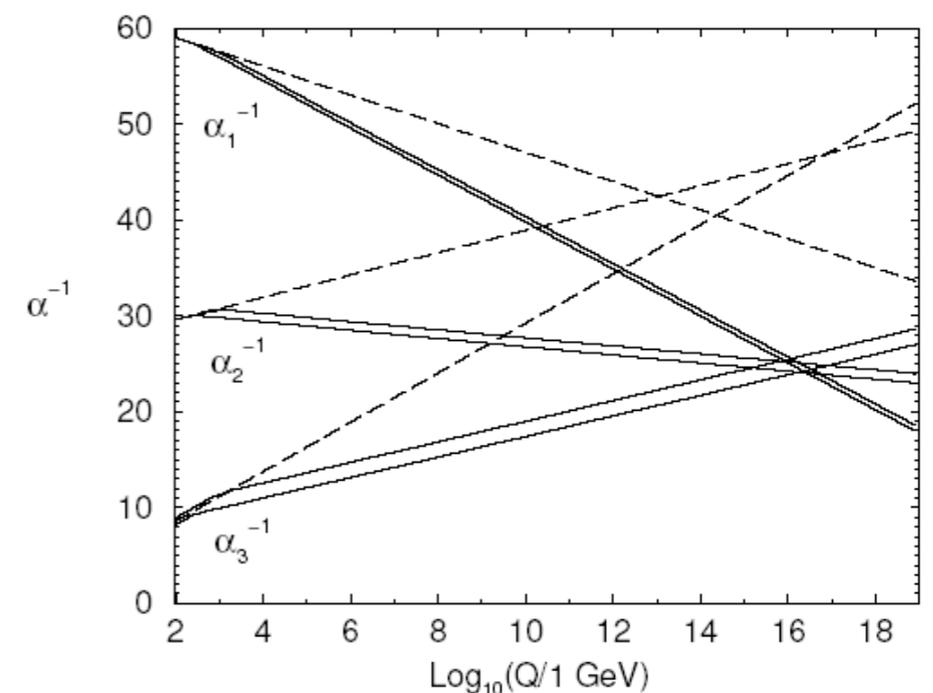
- The Intensity Frontier is
  - an indirect search, but
  - energy scale that could be studied would be much higher than that of accelerators of  $O(1 \text{ TeV})$ .
- Through quantum radiative corrections
  - renormalization group equations

Quantum Corrections



- Effects are small.
  - High precision measurements
  - High intensity beams

usefulness of renormalization equations



# Which Rare Processes at Low Energy ?

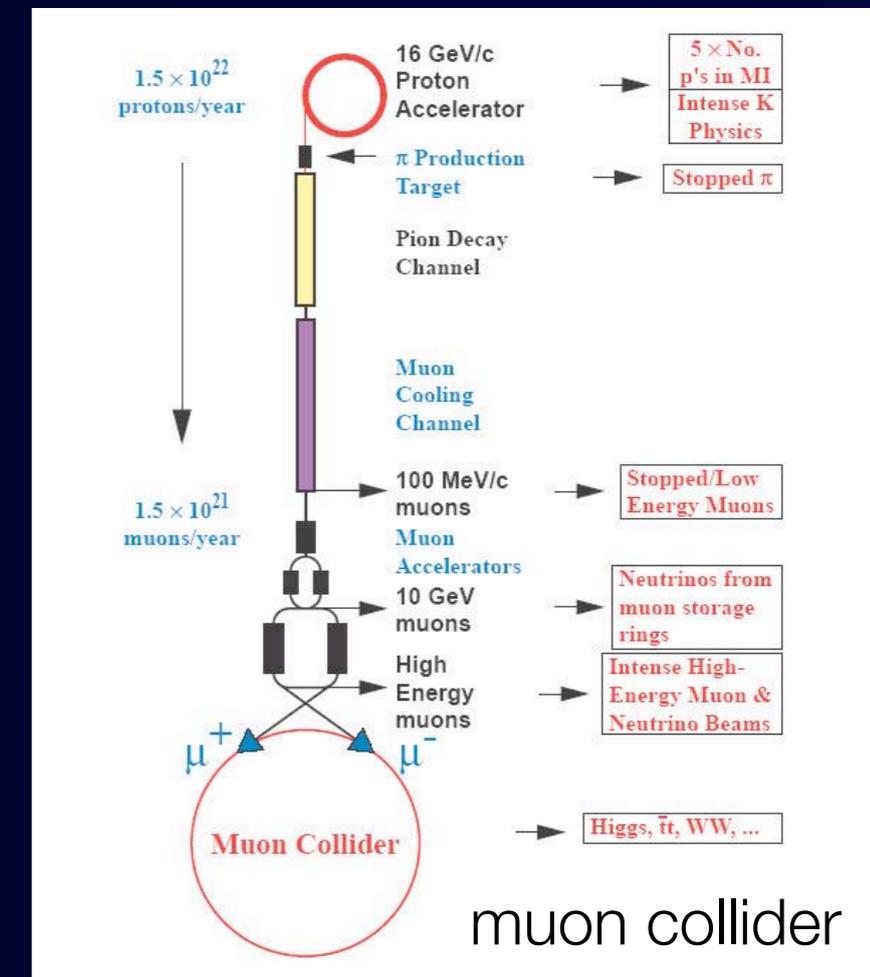
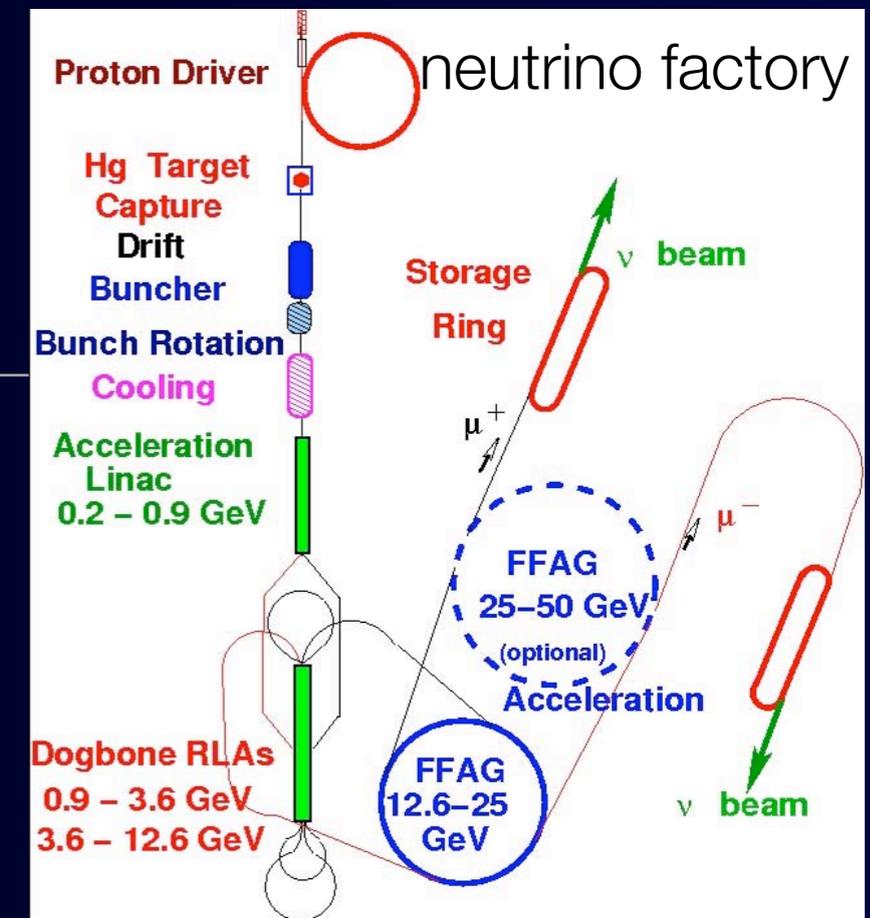
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- Processes which are forbidden or highly suppressed in the Standard Model would be the best ones to search for new physics beyond the Standard Model.
- **Flavor Changing Neutral Current Process (FCNC)**
- **FCNC in the quark sector**
  - $b \rightarrow s\gamma$ ,  $K \rightarrow \pi\nu\nu$ , etc.
  - Allowed in the Standard Model.
  - Need to study deviations from the SM predictions.
    - Uncertainty of more than a few % (from QCD) exists.
- **FCNC in the lepton sector**
  - $\mu \rightarrow e\gamma$ ,  $\mu + N \rightarrow e + N$ , etc. ( **Lepton Flavor Violation = LFV** )
  - Not allowed in the Standard Model ( $\sim 10^{-50}$  with neutrino mixing)
  - Need to study deviations from none
    - clear signature and high sensitivity

# Why Muons, not Taus ?

- Taus at B factories is not large enough, like about **10** taus/sec.
  - At future super-B factories, intensity increase of  $O(10-100)$  is expected. Also some of the decay modes are already background-limited.
- Muons at PSI is about  $10^8$  /sec.
  - Intensity increase of  $10^{11}-10^{14}$  /sec with the technology developed for the front end R&D of muon colliders and/or neutrino factories, where intensity improvement factor of up to about  $O(1,000,000)$ .

A larger window for new physics !





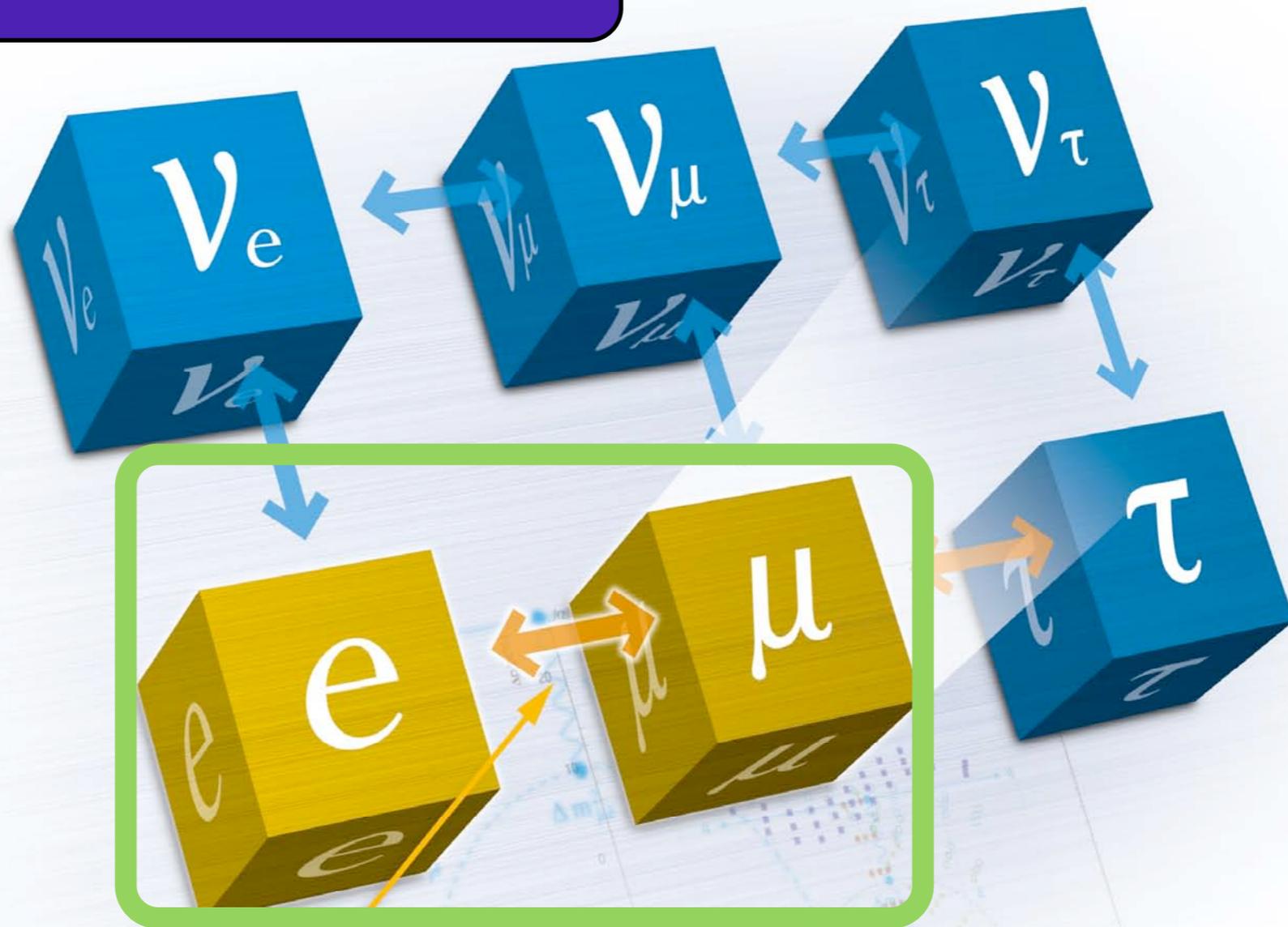
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Physics Motivation of cLFV

# Lepton Flavor Violation of Charged Leptons (cLFV)

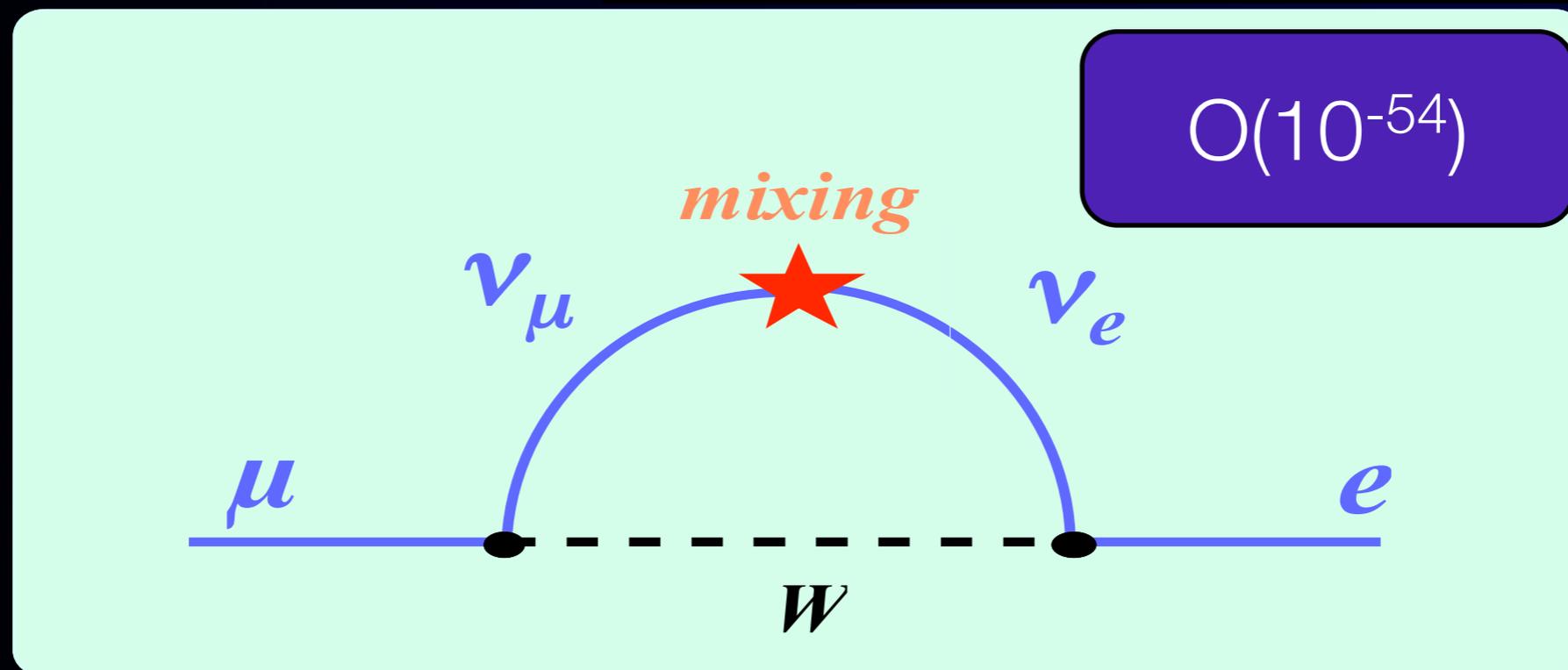
LFV of neutrinos is confirmed.



LFV of charged leptons is not observed.

# Standard Model Contribution from Neutrino Mixing (GIM mechanism)

$$B(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_l (V_{MNS})_{\mu l}^* (V_{MNS})_{el} \frac{m_{\nu_l}^2}{M_W^2} \right|^2$$



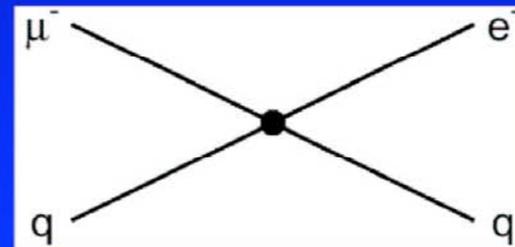
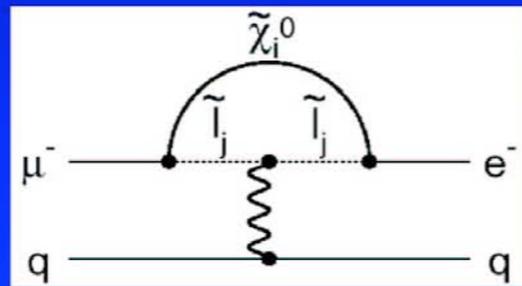
A Large Window for New Physics beyond the Standard Model

# Various Models Predict Charged Lepton Mixing.

## Sensitivity to Different Muon Conversion Mechanisms

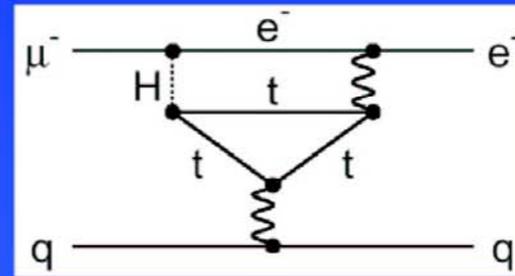
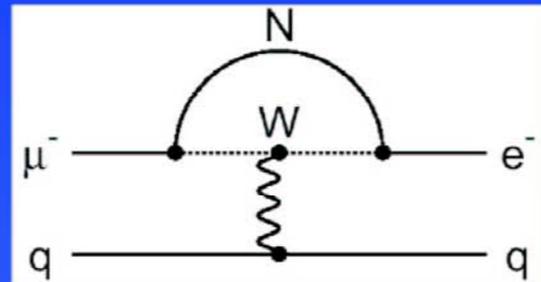


Supersymmetry  
Predictions at  $10^{-15}$



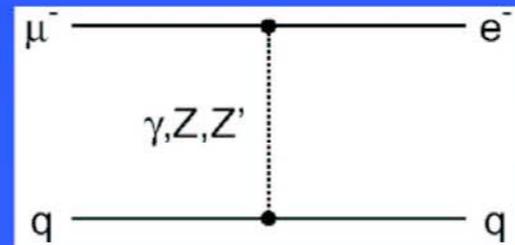
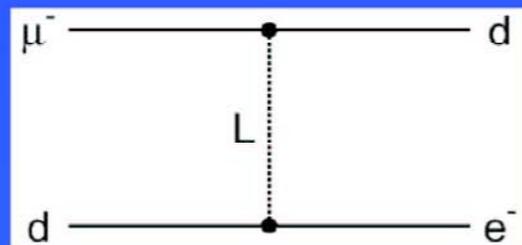
Compositeness  
 $\Lambda_c = 3000 \text{ TeV}$

Heavy Neutrinos  
 $|U_{\mu N}^* U_{eN}|^2 =$   
 $8 \times 10^{-13}$



Second Higgs doublet  
 $g_{H\mu e} = 10^{-4} \times g_{H\mu\mu}$

Leptoquarks



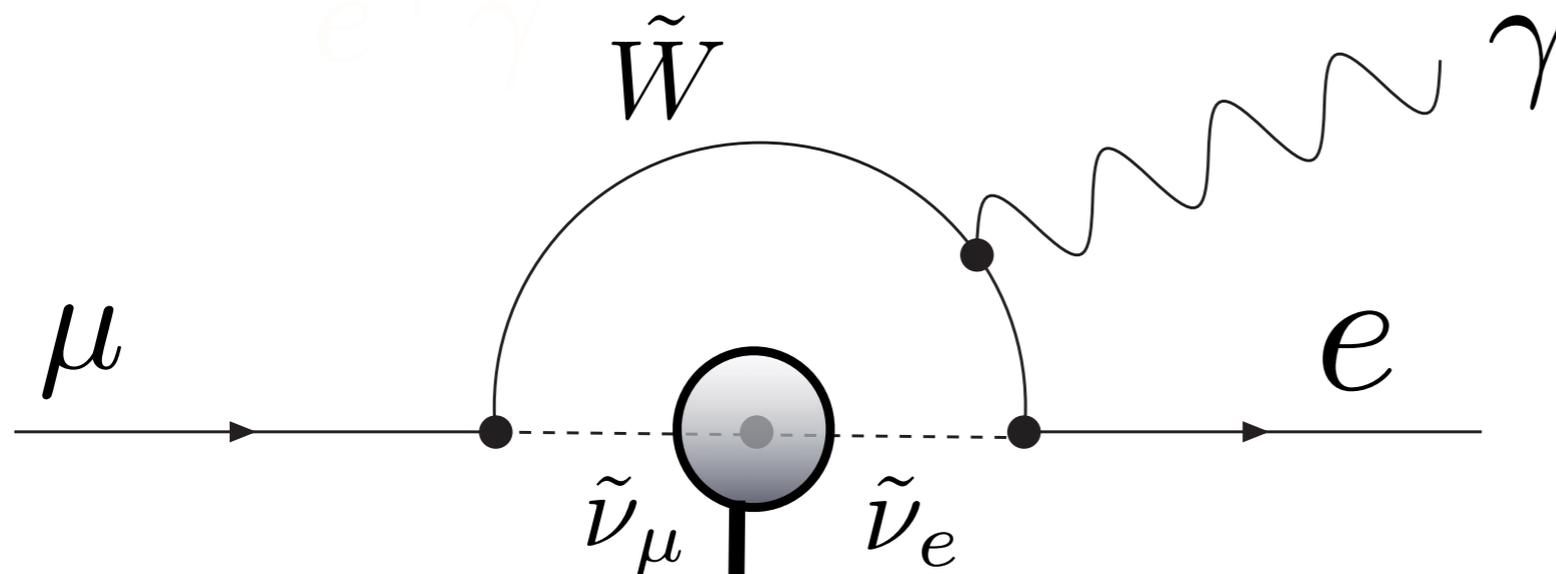
Heavy  $Z'$ ,  
Anomalous  $Z$   
coupling  
 $M_{Z'} = 3000 \text{ TeV}/c^2$   
 $B(Z \rightarrow \mu e) < 10^{-17}$

$M_L =$   
 $3000 (\lambda_{\mu d} \lambda_{e d})^{1/2} \text{ TeV}/c^2$

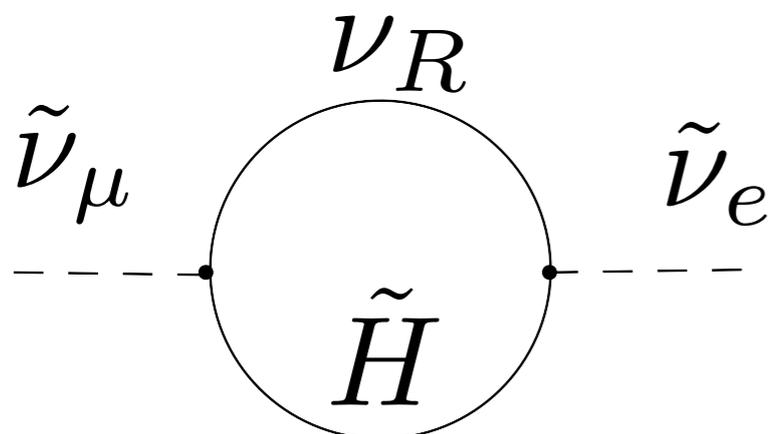
After W. Marciano

# LFV in SUSY Models

an example diagram



Slepton Mixing



Through quantum corrections, LFV could access ultra-heavy particles such as  $\nu_R$  ( $\sim 10^{12}-10^{14}$  GeV/c<sup>2</sup>) and GUT that cannot be produced directly by any accelerators.

## Features

- The decay rate is **not too small**, because it is determined by the SUSY mass scale.
- But, it contains the information at  $10^{16}$  GeV through the **slepton mixing**.
- It is in contrast to **proton decays** or **double beta decays** which need many particles.

SUSY GUT and SUSY Seesaw

# Slepton Mixing in mSUGRA Models

$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{11}^2 & m_{12}^2 & m_{13}^2 \\ m_{21}^2 & m_{22}^2 & m_{23}^2 \\ m_{31}^2 & m_{32}^2 & m_{33}^2 \end{pmatrix}$$

$$(m_{\tilde{l}}^2)_{ij} = m_0^2 \delta_{ij} \quad @ M_{\text{planck}}$$

GUT Yukawa interaction

Neutrino Yukawa interaction

SUSY-GUT Models

SUSY Seesaw Models

$$(\Delta m_{\tilde{l}}^2)_{ij} \neq 0$$

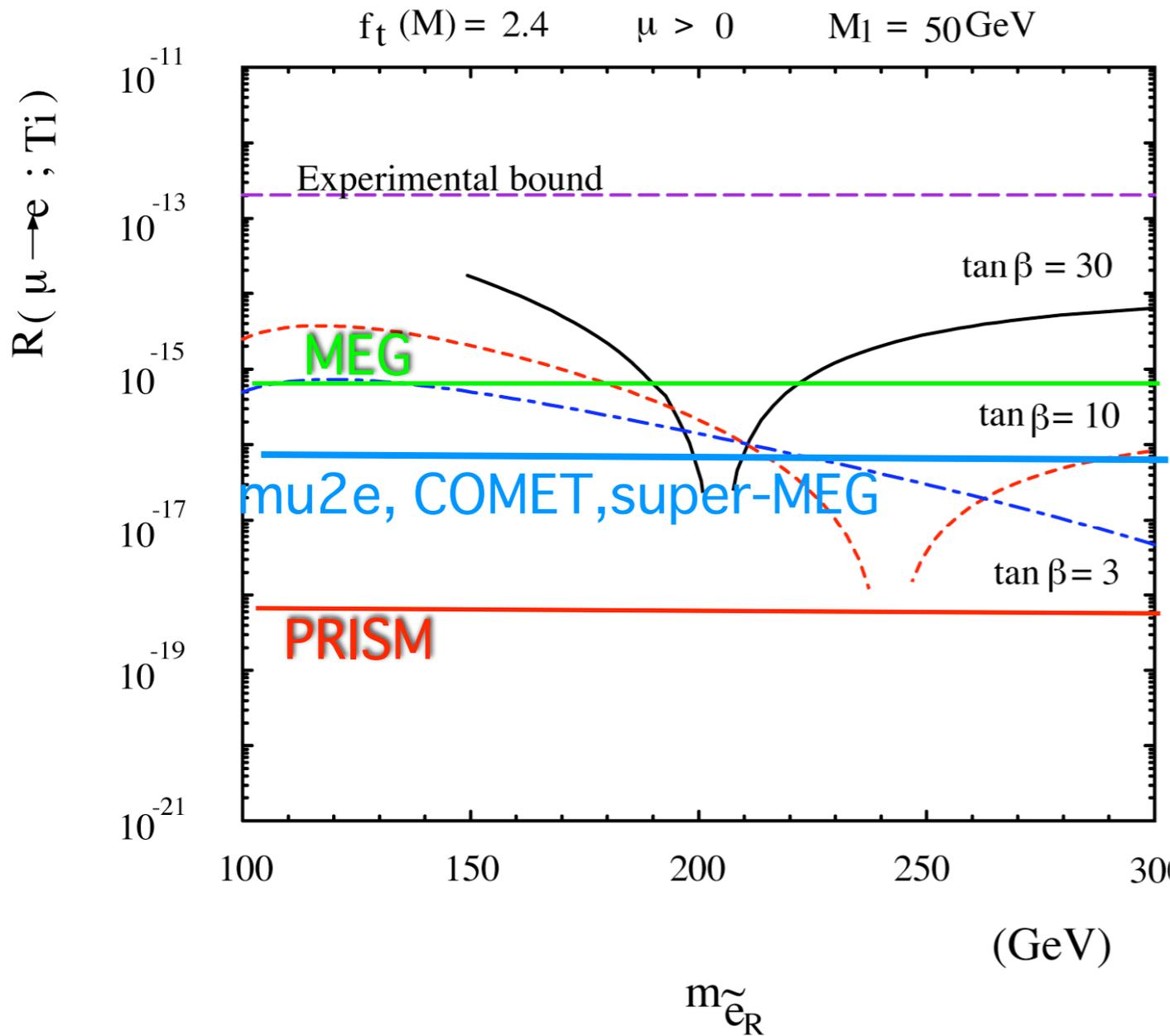
$$(m_{\tilde{L}}^2)_{21} \sim \frac{3m_0^2 + A_0^2}{8\pi^2} h_t^2 V_{td} V_{ts} \ln \frac{M_{GUT}}{M_{R_s}}$$

$$(m_{\tilde{L}}^2)_{21} \sim \frac{3m_0^2 + A_0^2}{8\pi^2} h_t^2 U_{31} U_{32} \frac{M_{GUT}}{M_{R_s}}$$

CKM matrix

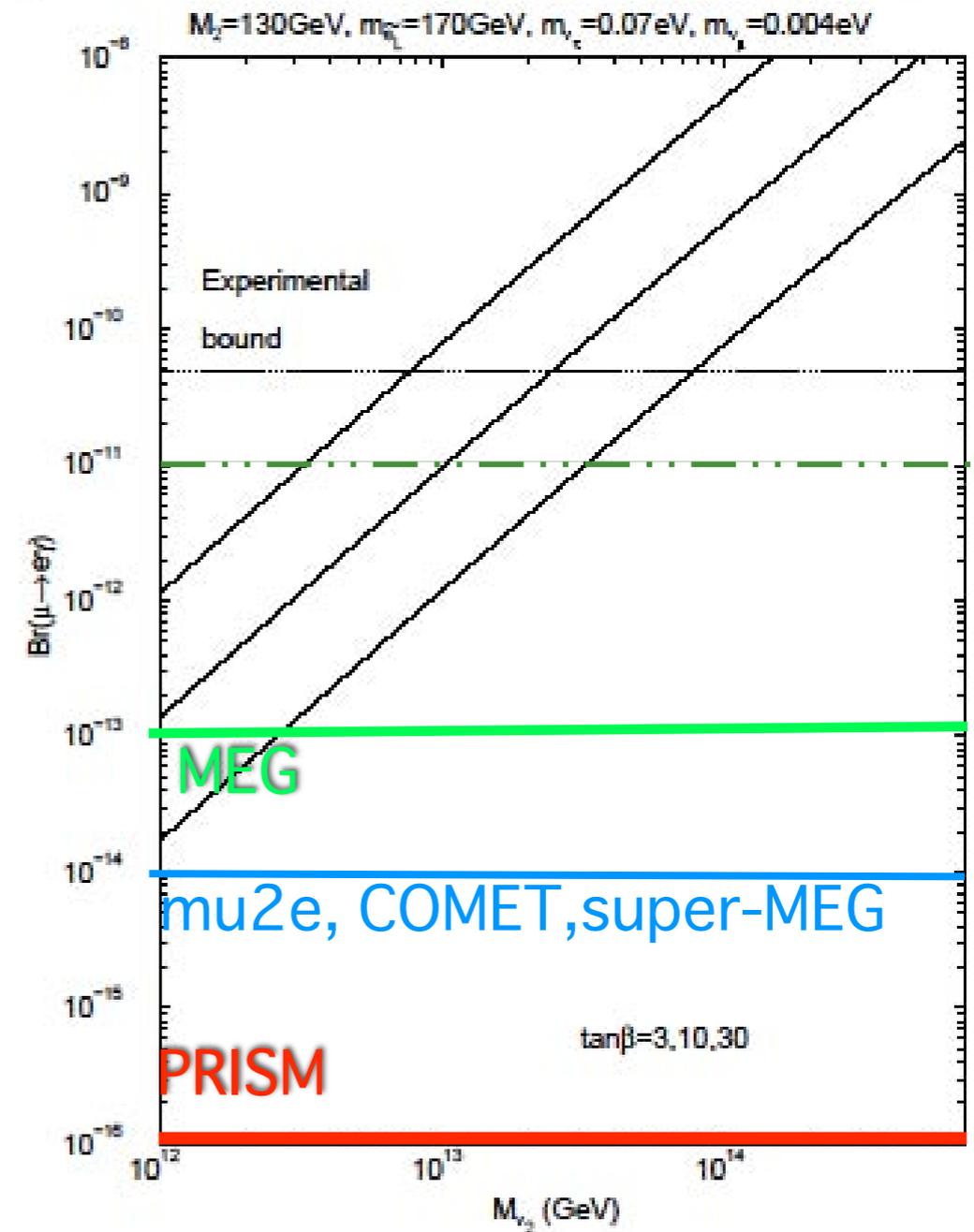
Neutrino oscillation

# SUSY Predictions for cLFV



SU(5) SUSY GUT

$\mu \rightarrow e \gamma$  in the MSSMRN with the MSW large angle solution

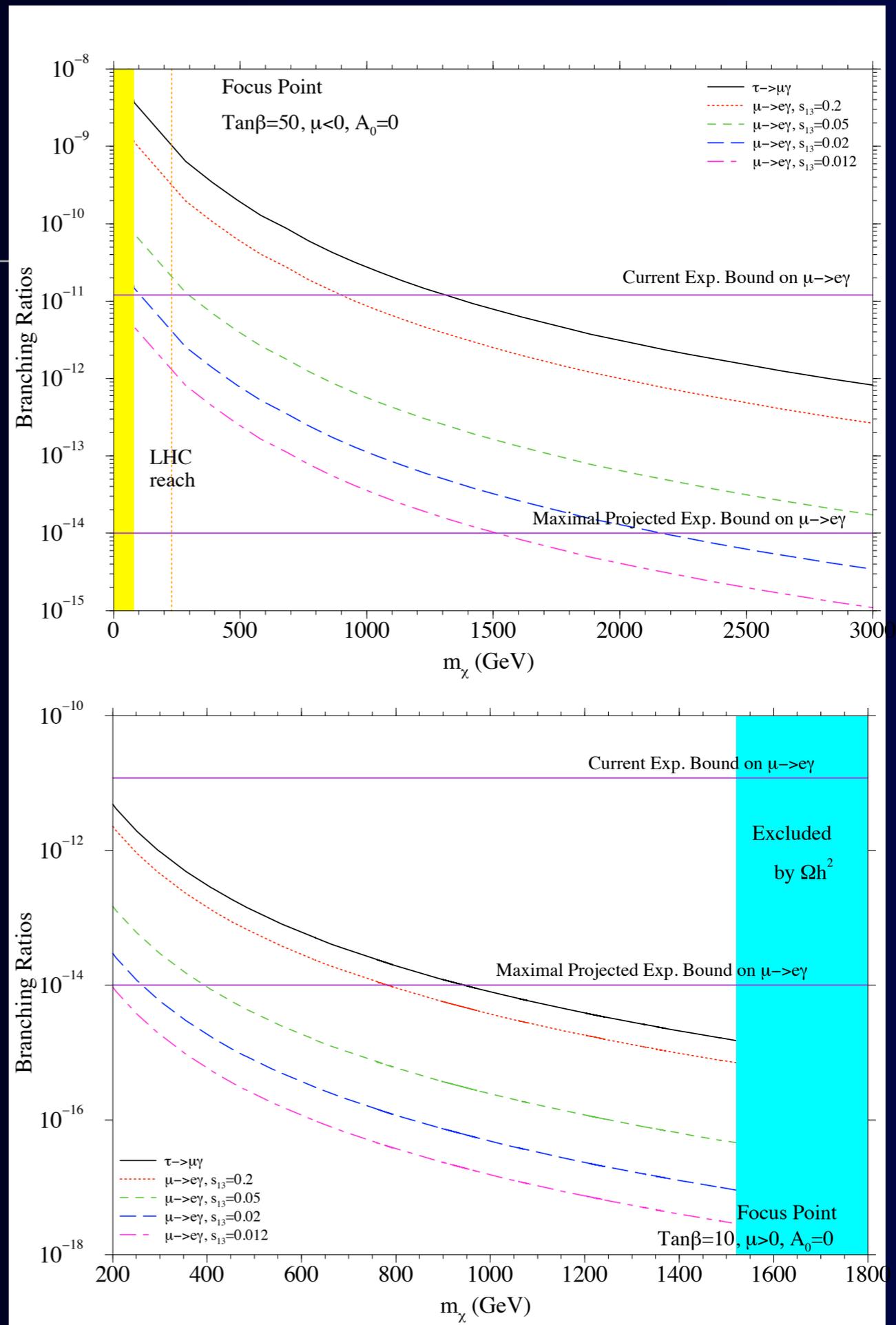


SUSY Seesaw Model

# Complementarity to LHC (mSUGRA)

- In mSUGRA, some of the parameter regions, where LHC does not have sensitivity to SUSY, can be explored by cLFV.
- Bench mark points
  - **Focus point**  $\longrightarrow$ 
    - LHC can not cover and cLFV can cover.

cLFV is complementary to LHC, and in some case has much better sensitivity than LHC.



# Short Summary of Physics Motivation : cLFV, Energy Frontier and SUSY

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- In SUSY models, cLFV is sensitive to slepton mixing.
- LHC would have potentials to see SUSY particles. However, at LHC nor even ILC, **slepton mixing would be difficult to study** in such a high precision as proposed here.
- Slepton mixing is sensitive to either (or both) Grand Unified Theories (SUSY-GUT models) or neutrino seesaw mechanism (SUSY-Seesaw models).
- If cLFV sensitivity is extremely high, it might be able to explore multi-TeV SUSY which LHC cannot reach, in particular SUSY parameters.





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# LFV Experiments



# Present Limits and Expectations in Future

| process                        | present limit          | future                 |                 |
|--------------------------------|------------------------|------------------------|-----------------|
| $\mu \rightarrow e\gamma$      | $<1.2 \times 10^{-11}$ | $<10^{-13}$            | MEG at PSI      |
| $\mu \rightarrow eee$          | $<1.0 \times 10^{-12}$ | $<10^{-13} - 10^{-14}$ | ?               |
| $\mu N \rightarrow eN$ (in Al) | none                   | $<10^{-16}$            | Mu2e / COMET    |
| $\mu N \rightarrow eN$ (in Ti) | $<4.3 \times 10^{-12}$ | $<10^{-18}$            | PRISM           |
| $\tau \rightarrow e\gamma$     | $<1.1 \times 10^{-7}$  | $<10^{-9} - 10^{-10}$  | super B factory |
| $\tau \rightarrow eee$         | $<3.6 \times 10^{-8}$  | $<10^{-9} - 10^{-10}$  | super B factory |
| $\tau \rightarrow \mu\gamma$   | $<4.5 \times 10^{-8}$  | $<10^{-9} - 10^{-10}$  | super B factory |
| $\tau \rightarrow \mu\mu\mu$   | $<3.2 \times 10^{-8}$  | $<10^{-9} - 10^{-10}$  | super B factory |

# List of cLFV Processes with Muons

---

$\Delta L=1$

- $\mu^+ \rightarrow e^+ \gamma$

- $\mu^+ \rightarrow e^+ e^+ e^-$

- $\mu^- + N(A, Z) \rightarrow e^- + N(A, Z)$

- $\mu^- + N(A, Z) \rightarrow e^+ + N(A, Z - 2)$

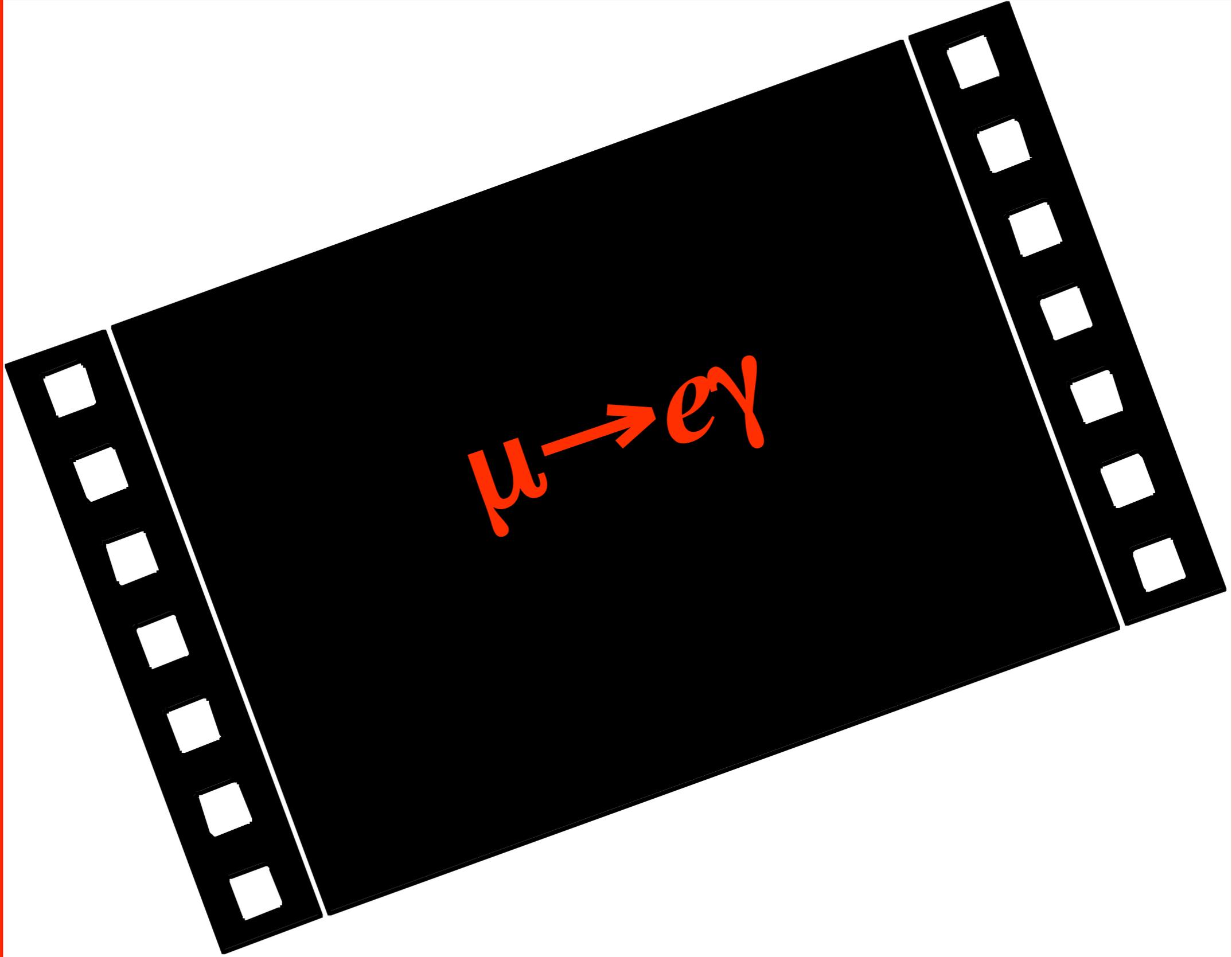
$\Delta L=2$

- $\mu^+ e^- \rightarrow \mu^- e^+$

- $\mu^- + N(A, Z) \rightarrow \mu^+ + N(A, Z - 2)$

- $\nu_\mu + N(A, Z) \rightarrow \mu^+ + N(A, Z - 1)$

- $\nu_\mu + N(A, Z) \rightarrow \mu^+ \mu^+ \mu^- + N(A, Z - 1)$



# What is $\mu \rightarrow e\gamma$ ?

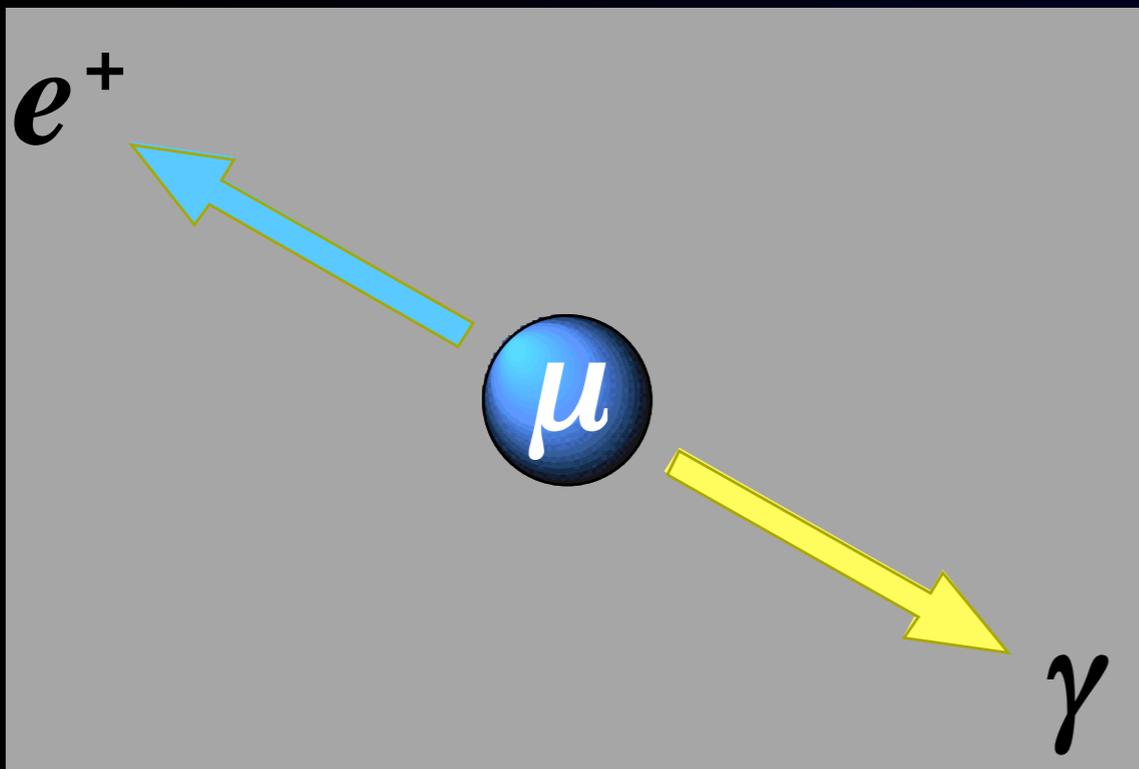
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- **Event Signature**

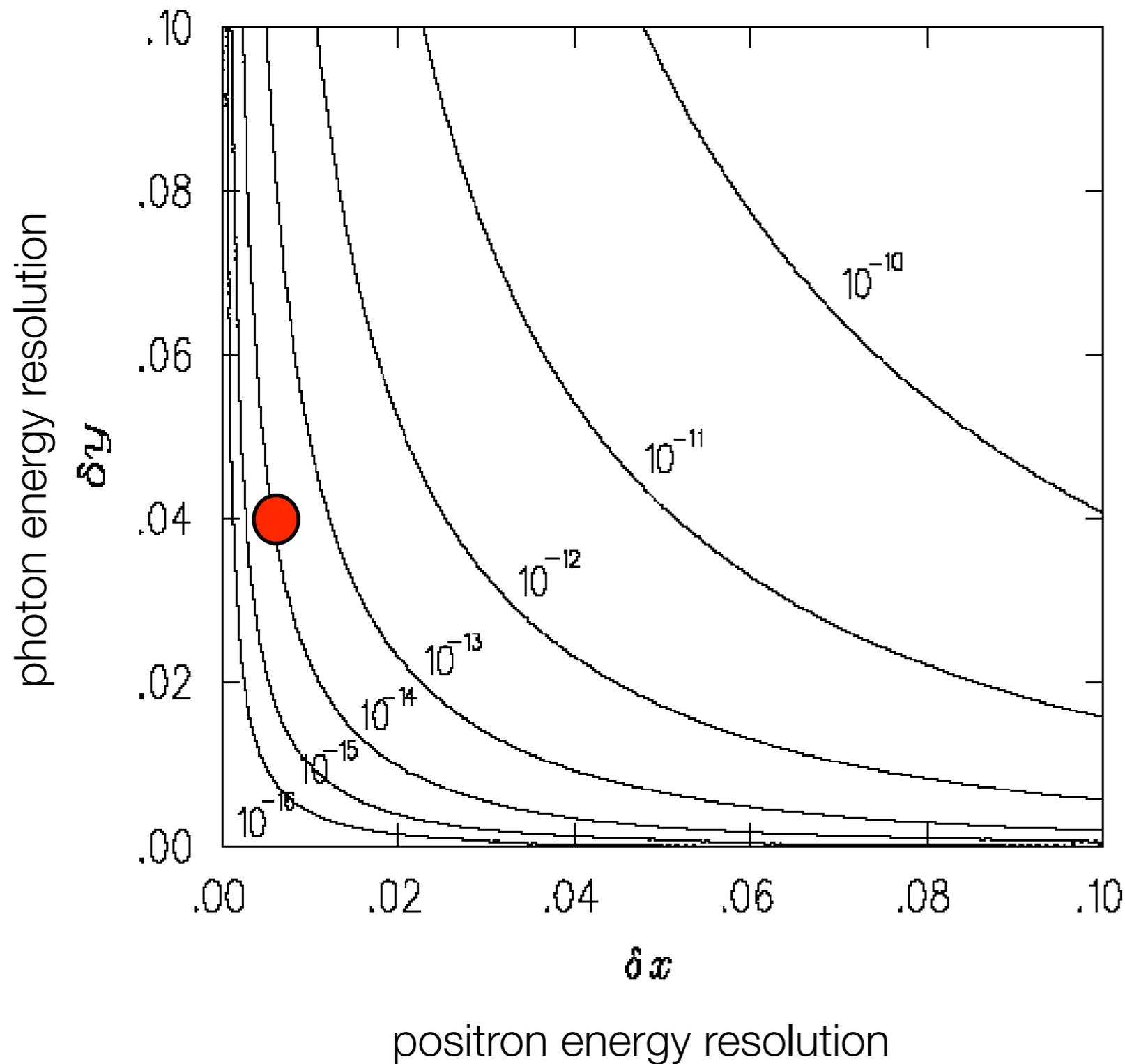
- $E_e = m_\mu/2$ ,  $E_\gamma = m_\mu/2$   
(=52.8 MeV)
- angle  $\theta_{\mu e}=180$  degrees  
(back-to-back)
- time coincidence

- **Backgrounds**

- prompt physics backgrounds
  - radiative muon decay  $\mu \rightarrow e\nu\nu\gamma$  when two neutrinos carry very small energies.
- accidental backgrounds
  - positron in  $\mu \rightarrow e\nu\nu$
  - photon in  $\mu \rightarrow e\nu\nu\gamma$  or photon from  $e^+e^-$  annihilation in flight.



# Physics Background for $\mu \rightarrow e\gamma$ Decay



Effective branching ratio is a function of the resolution of electron detection ( $\delta x$ ) and that of photon detection ( $\delta y$ ).

Background level is about  $10^{-14}$  for  $\delta x \sim 1\%$  and  $\delta y = 5\%$ .

# Accidental Backgrounds for $\mu \rightarrow e\gamma$

| Place     | Year | $\Delta E_e$ | $\Delta E_\gamma$ | $\Delta t_{e\gamma}$ | $\Delta\theta_{e\gamma}$ | Upper limit             |
|-----------|------|--------------|-------------------|----------------------|--------------------------|-------------------------|
| TRIUMF    | 1977 | 10%          | 8.7%              | 6.7ns                | —                        | $< 3.6 \times 10^{-9}$  |
| SIN       | 1980 | 8.7%         | 9.3%              | 1.4ns                | —                        | $< 1.0 \times 10^{-9}$  |
| LANL      | 1982 | 8.8%         | 8%                | 1.9ns                | 37mrad                   | $< 1.7 \times 10^{-10}$ |
| LANL      | 1988 | 8%           | 8%                | 1.8ns                | 87mrad                   | $< 4.9 \times 10^{-11}$ |
| LANL      | 1999 | 1.2%         | 4.5%              | 1.6ns                | 15mrad                   | $< 1.2 \times 10^{-11}$ |
| PSI (MEG) | 2007 | 0.9%         | 5 %               | 0.1 ns               | 23mrad                   | $< 10^{-13}$            |

states  
of arts

$$\text{Accidental Background} \propto \left(R_\mu\right)^2 \times \Delta E_e \times \left(\Delta E_\gamma\right)^2 \times \Delta t_{e\gamma} \times \left(\Delta\theta_{e\gamma}\right)^2$$

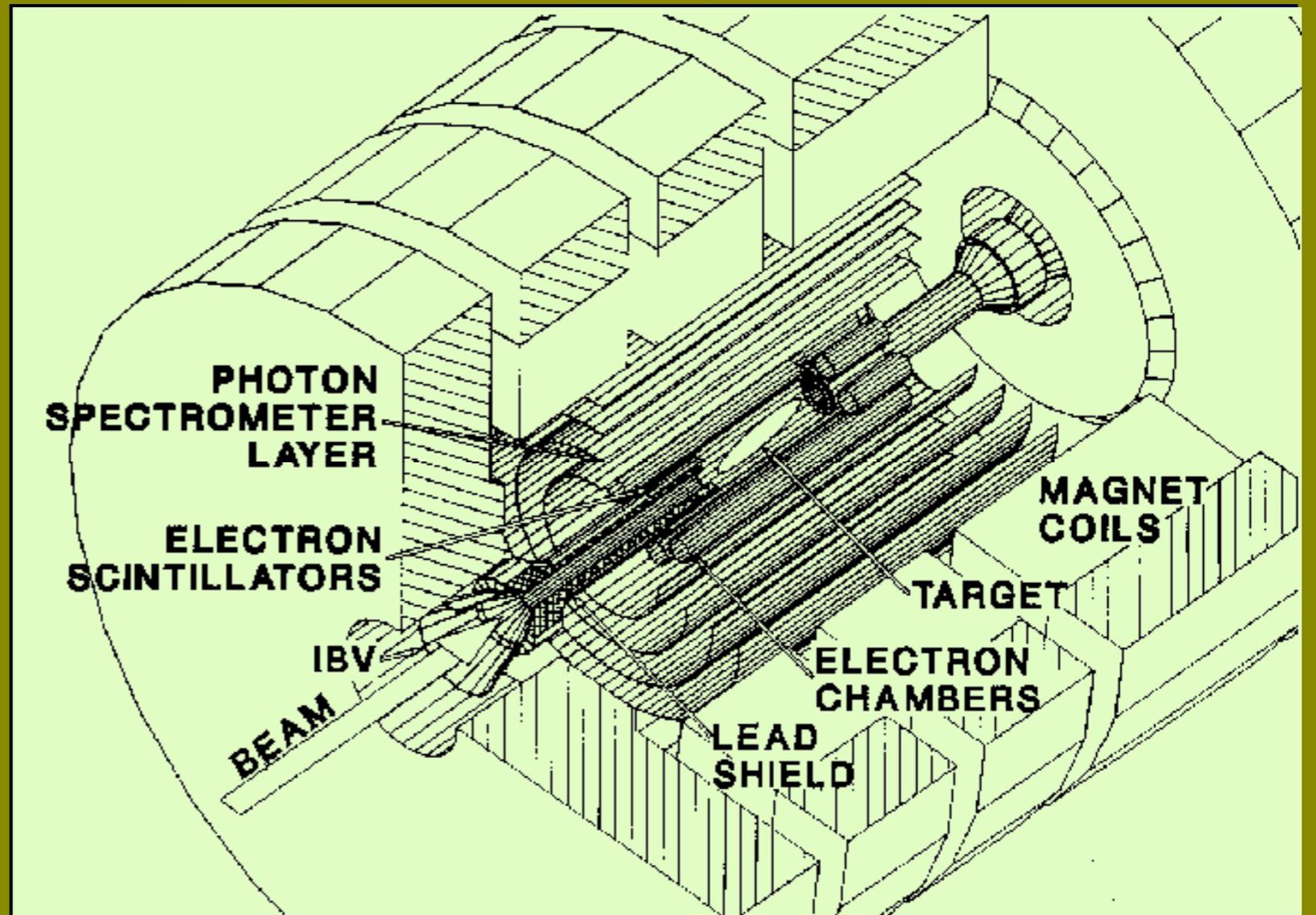
$N_B=0.5$  events at  $B(\mu \rightarrow e\gamma) \sim 10^{-13}$

With the same resolutions,  $N_\mu=10^{10}$   $\mu/s$ ,  
 $N_B=5000$  events at  $B(\mu \rightarrow e\gamma) \sim 10^{-16}$

Improvements of  
 detector resolutions  
 are critical.

# MEGA at Los Alamos

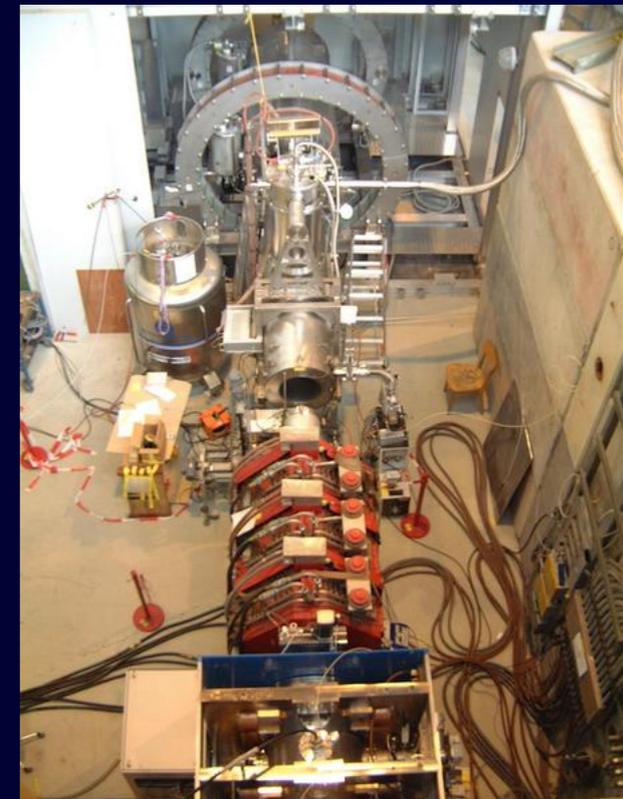
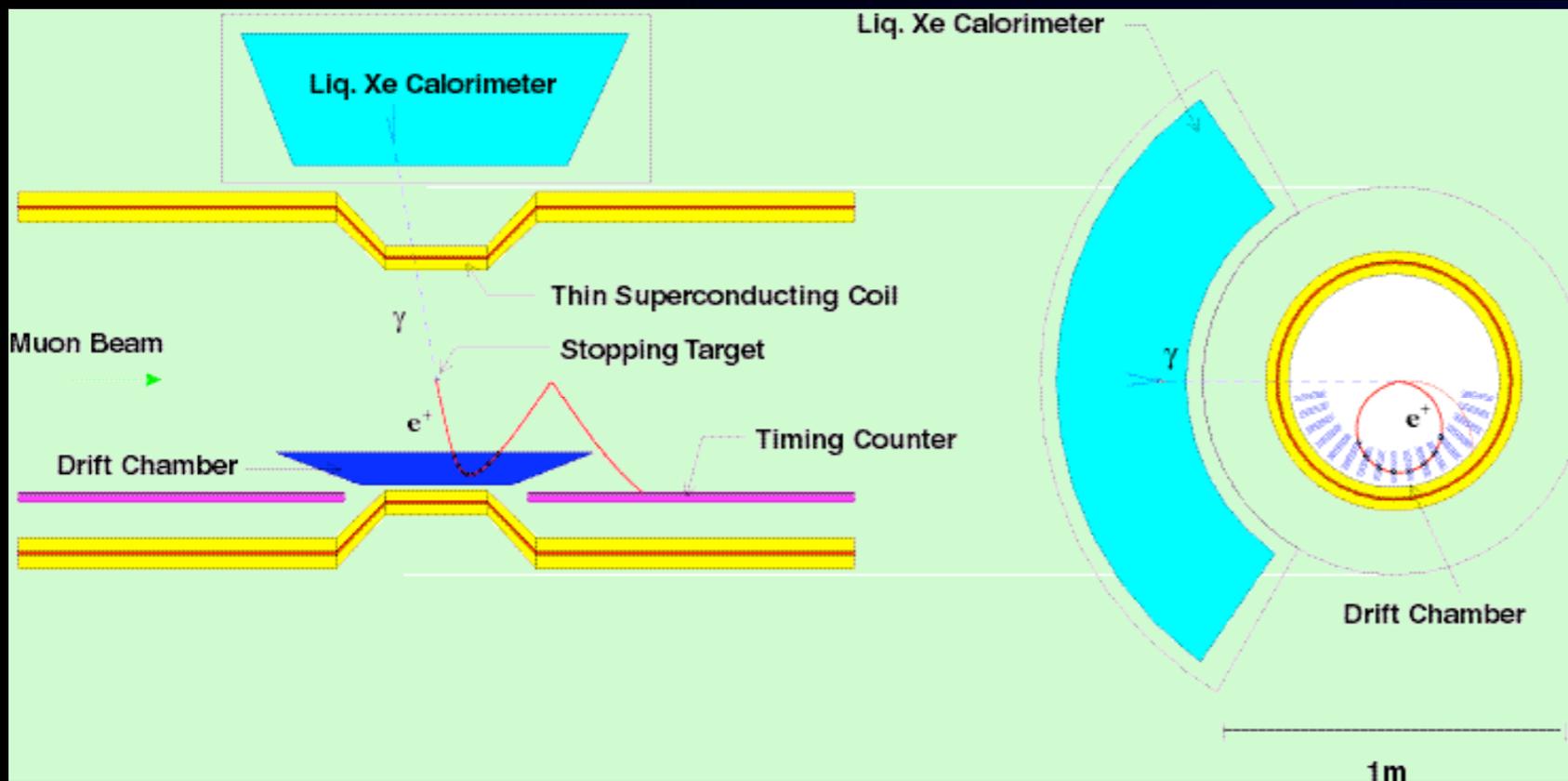
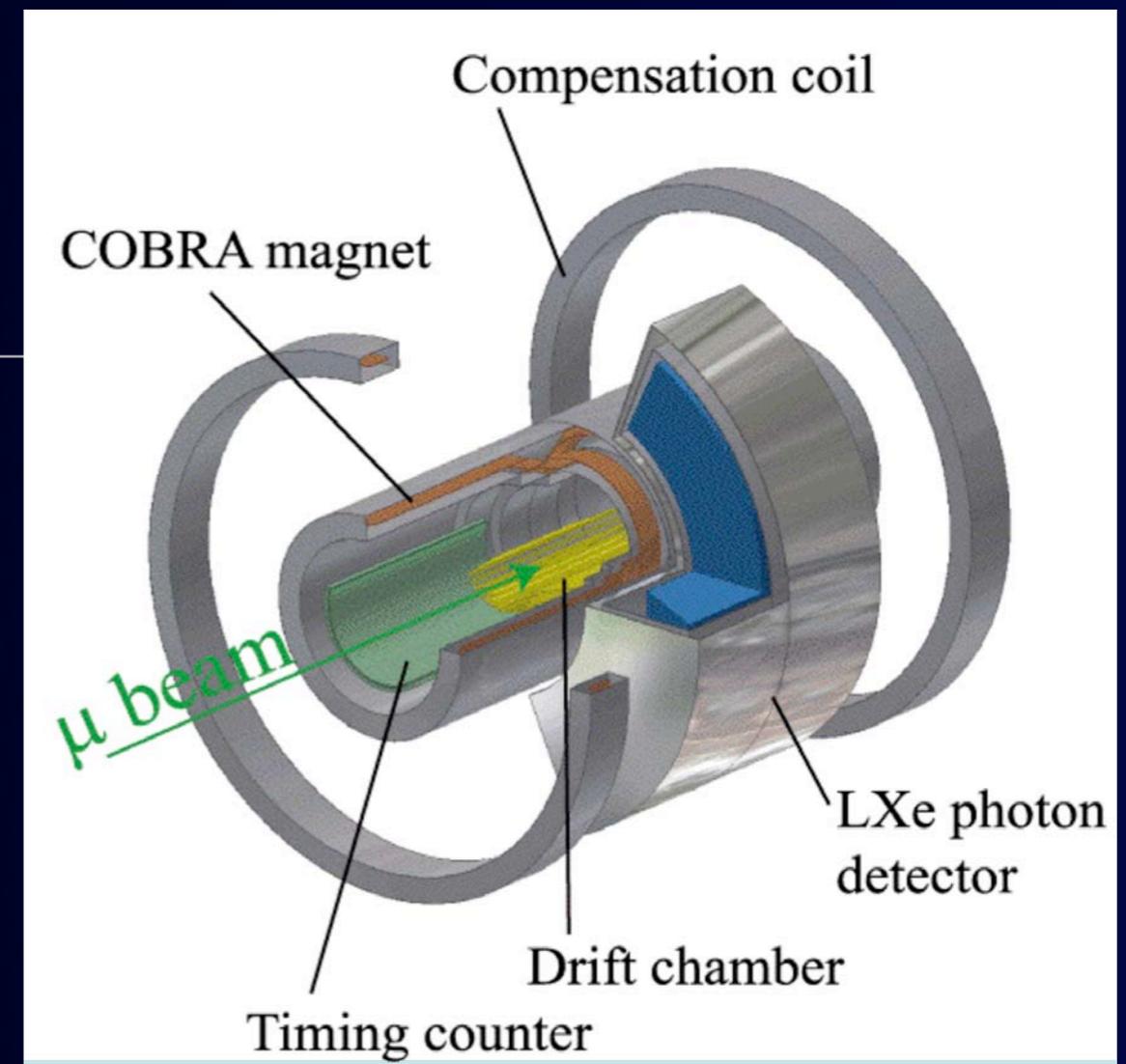
- MEGA at Los Alamos (~1999)
- A thin slanted target.
- 1.5 T solenoid magnetic field
- 7 dwarf chambers for  $e^+$  tracking
- pair spectrometer for gamma detection



$$B(\mu^+ \rightarrow e^+ \gamma) < 1.2 \times 10^{-11}$$

# MEG at PSI

- DC beam  $10^7$  muons/sec.
- Goal :  $B < 2 \times 10^{-13}$
- COBRA : spectrometer for  $e^+$  detection.
- Liquid Xenon detector for photon detection.

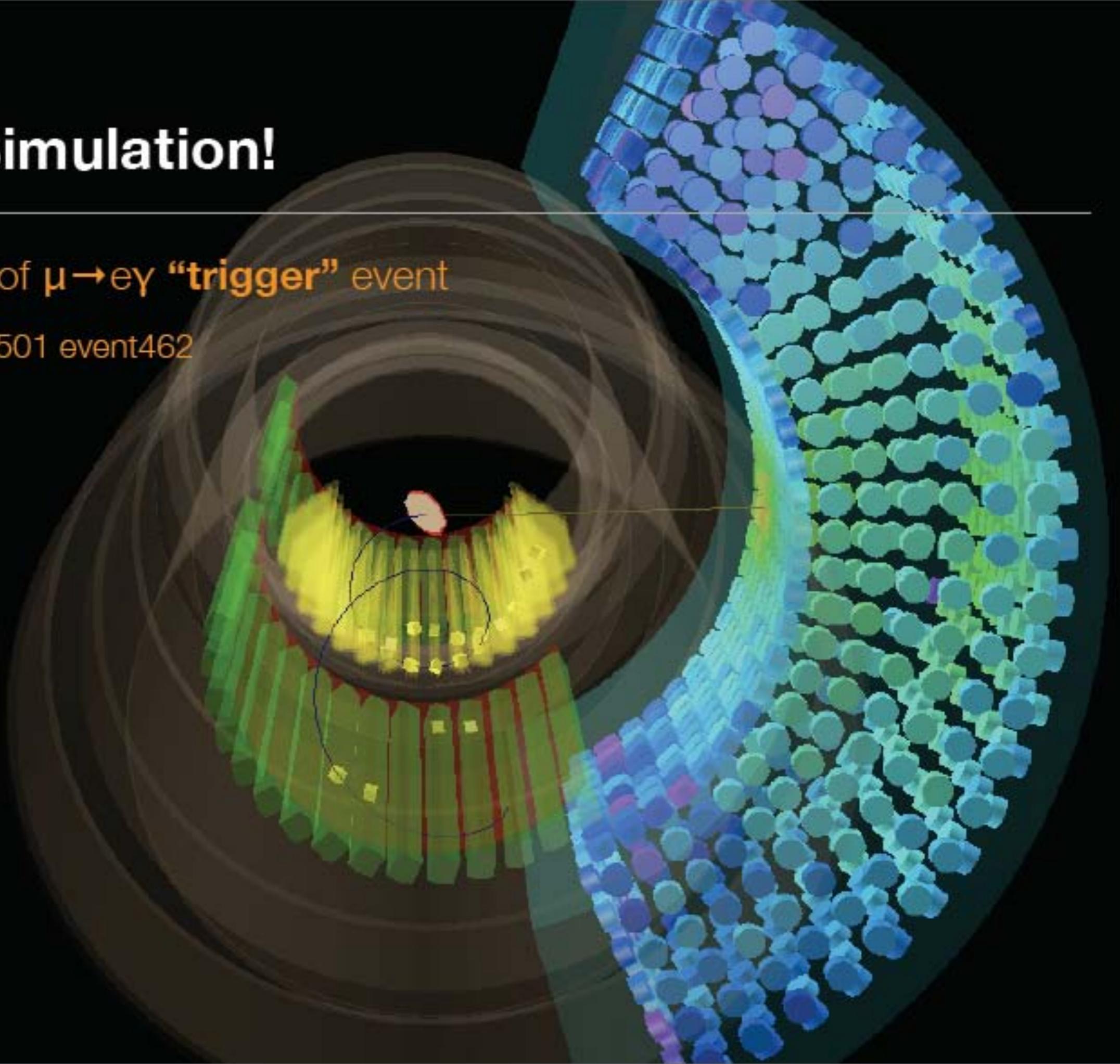


# Not a Simulation!

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Example of  $\mu \rightarrow e\gamma$  “trigger” event

Run#24501 event462



- Preliminary
- Calibration is in progress for 2008 data



- Blue numbers likely to change    - Grey numbers may vanish

| (%)   | “Goal”               | 2008<br>Provisional Lower Limits                            | 2009<br>Provisional Prospects |
|---|----------------------|---|-------------------------------|
| Gamma   | > 40                 | > 50 x (65 x 85)<br><small>depth    pileup</small>          | > 50 x 90                     |
| e+  | 65                   | 30 x 40<br><small>DC    DC-TC</small>                       | 85 x 50                       |
| Trigger                                       | 100                  | 100 x 99 x 80<br><small>energy    time    direction</small> | > 99                          |
| Selection                                     | 90 <sup>4</sup> = 66 | 90 <sup>3</sup> x 95 = 69                                   | 69                            |
| DAQ   | (> 90)               | > 80 x 93<br><small>live    run transition</small>          | > 90 x 99                     |
| Calibration Run etc                           | (> 95)               | ~70   | 90                            |
| Running Time (week)                           | 100*                 | 11.5**  | 11.5                          |
| Single Event Sensitivity (10 <sup>-13</sup> ) | 0.5                  | < 30 - 50   | < 3 - 5                       |

\* 1 week = 4x10<sup>6</sup> sec (66%)

\*\* CEX runs not included

## Efficiencies Summary

- All 2008 numbers are provisional



| (in sigma)                      | “Goal”    | 2008 Provisional | 2009 Provisional Prospects |
|---------------------------------|-----------|------------------|----------------------------|
| Gamma Energy (%)                | 1.2 - 1.5 | < 2.3            | < 1.7                      |
| Gamma Timing (ps)               | 65        | < 100*           | < 80                       |
| Gamma Position (mm)             | 2 - 4     | 5 - 6.5          | 5                          |
| e+ Momentum (%)                 | 0.35      | 1.5 - 2.0        | 0.7 - 0.8                  |
| e+ Timing (ps)                  | 45        | < 60 - 90        | 60                         |
| e+ Angle (mrad)                 | 4.5       | 9 - 18           | 11                         |
| mu Decay Point (mm)             | 0.9       | 3 - 4            | 2                          |
| Gamma - e+ Timing (ps)          | 80        | 150              | 100                        |
| Background (10 <sup>-13</sup> ) | 0.1 - 0.3 | -                | < 0.6 - 3                  |

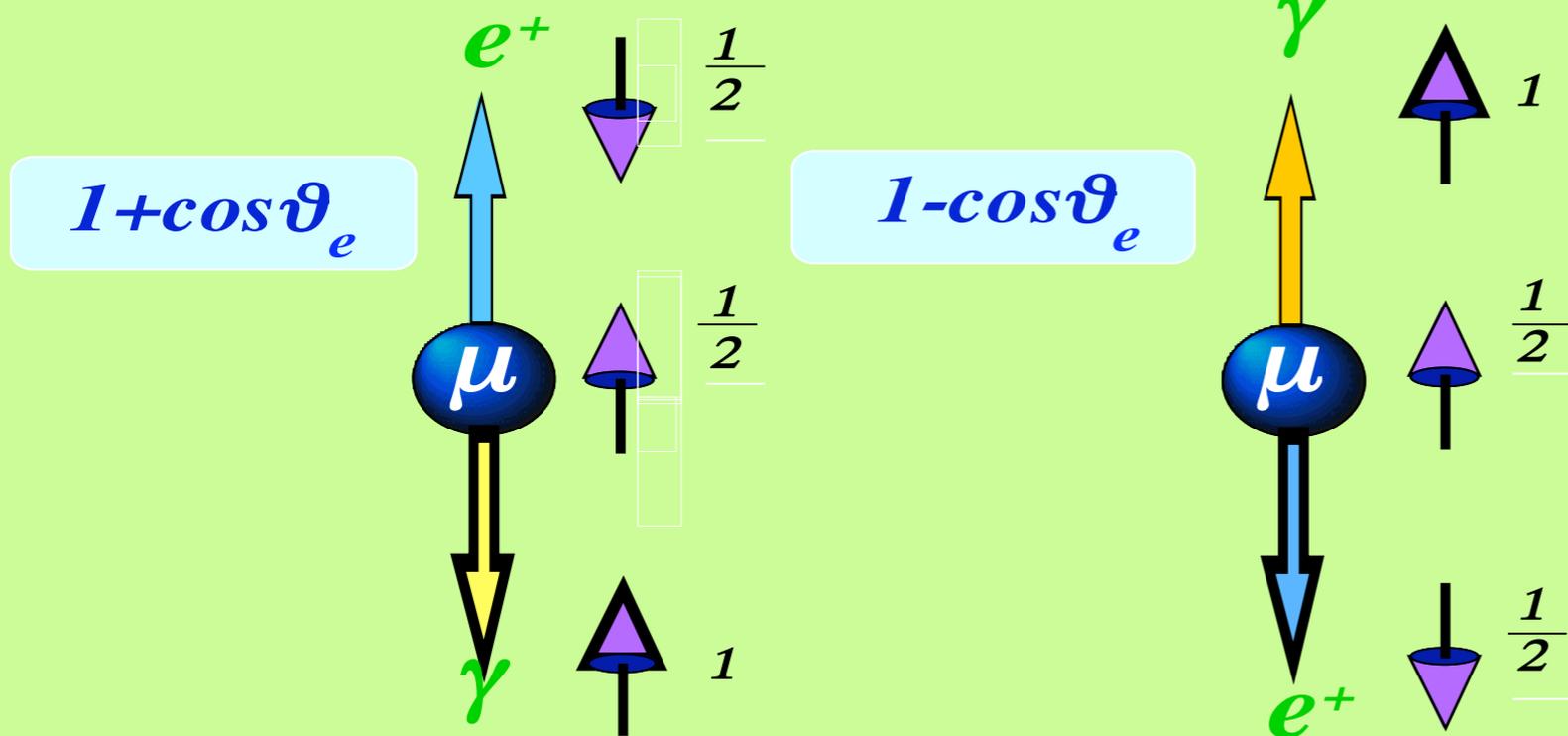
\* clock error of -60ps included

# Resolutions

# P-Odd Angular Distribution of Polarized $\mu \rightarrow e\gamma$ Decay (after its observation)

*Left handed  $e^+$*

*Right handed  $e^+$*



*useful to distinguish different theoretical models*

*$SU(5)$  SUSY-GUT*

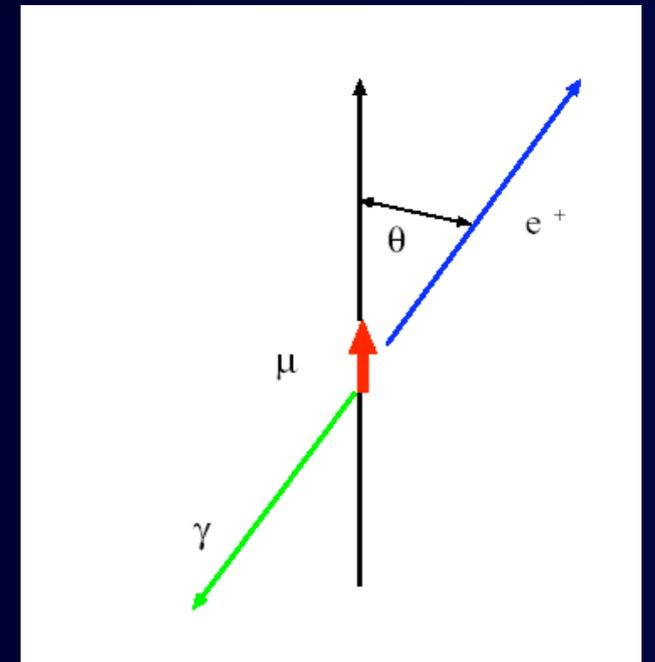
*non-unified SUSY  
with heavy neutrino*

*Left-right symmetric model*

*$SO(10)$  SUSY-GUT*

*Y.Kuno and Y. Okada, Physical Review Letters 77 (1996) 434*

*Y.Kuno, A. Maki and Y. Okada, Physical Reviews D55 (1997) R2517-2520*



P-odd asymmetry reflects whether right or left-handed slepton have flavor mixing,

Discriminate theoretical models

surface muons

# Suppression of Physics Background with Polarized $\mu \rightarrow e\gamma$ Decay

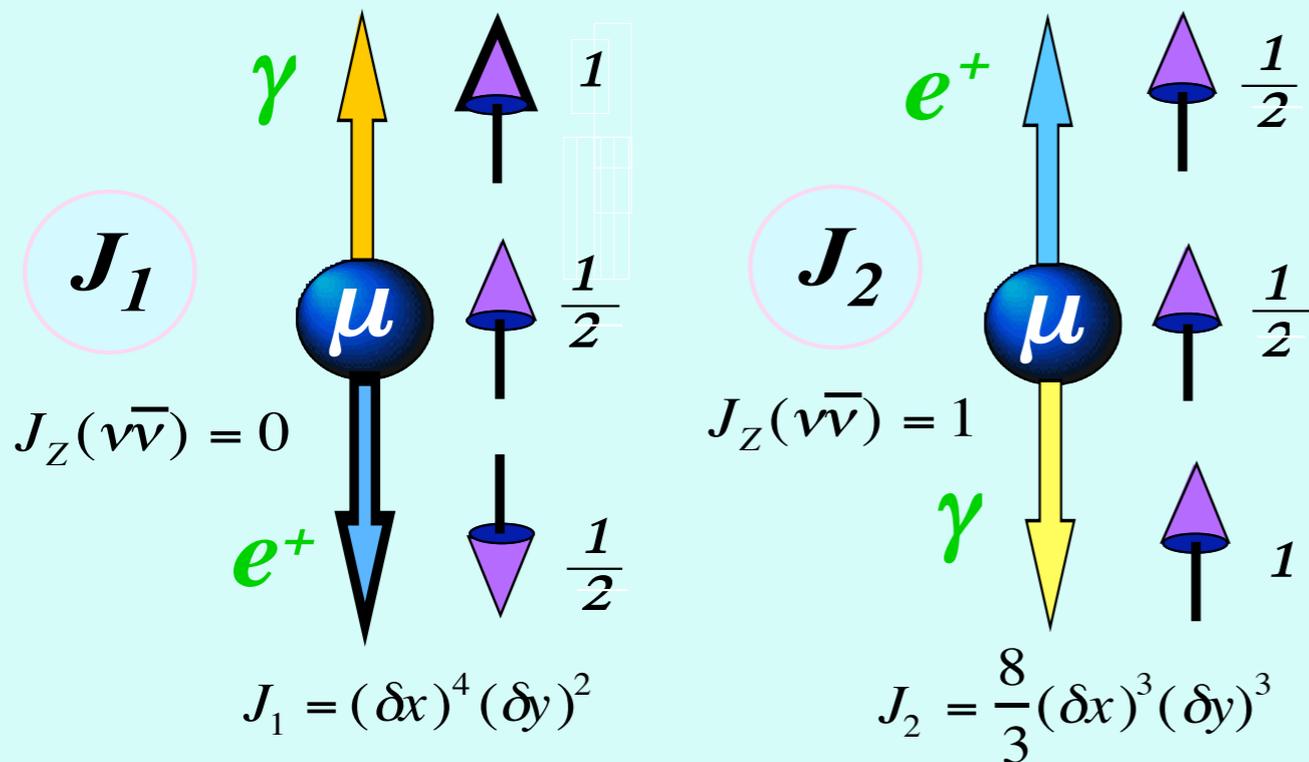
## radiative muon decay

at end-point of spectrum when neutrinos have small energy

integrate the decay width

|                        |                                    |
|------------------------|------------------------------------|
| $1 - \delta x < x < 1$ | $\delta x : e \text{ energy}$      |
| $1 - \delta y < y < 1$ | $\delta y : \gamma \text{ energy}$ |
| $0 < z < \delta z$     | $\delta z : \text{angle}$          |

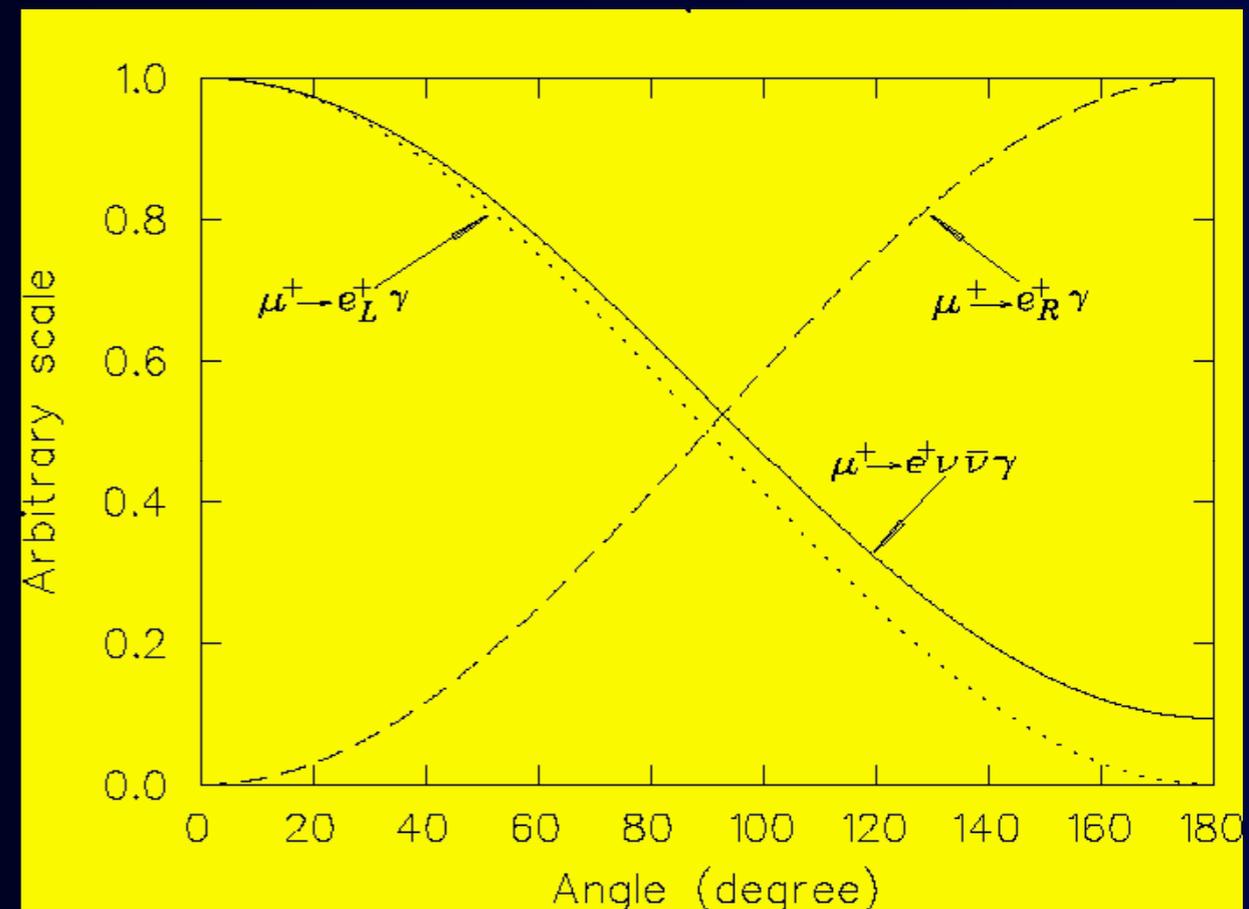
$$dB = \frac{\alpha}{16\pi} \left[ J_1 (1 - P_\mu \cos\theta_{e\gamma}) + J_2 (1 + P_\mu \cos\theta_{e\gamma}) \right]$$



if  $(\delta y) > (\delta x)$ , then  $J_2 > J_1$ , following a  $(1 + P_\mu \cos\vartheta)$

Improve a S/B ratio for  $\mu^+ \rightarrow e_R \gamma$

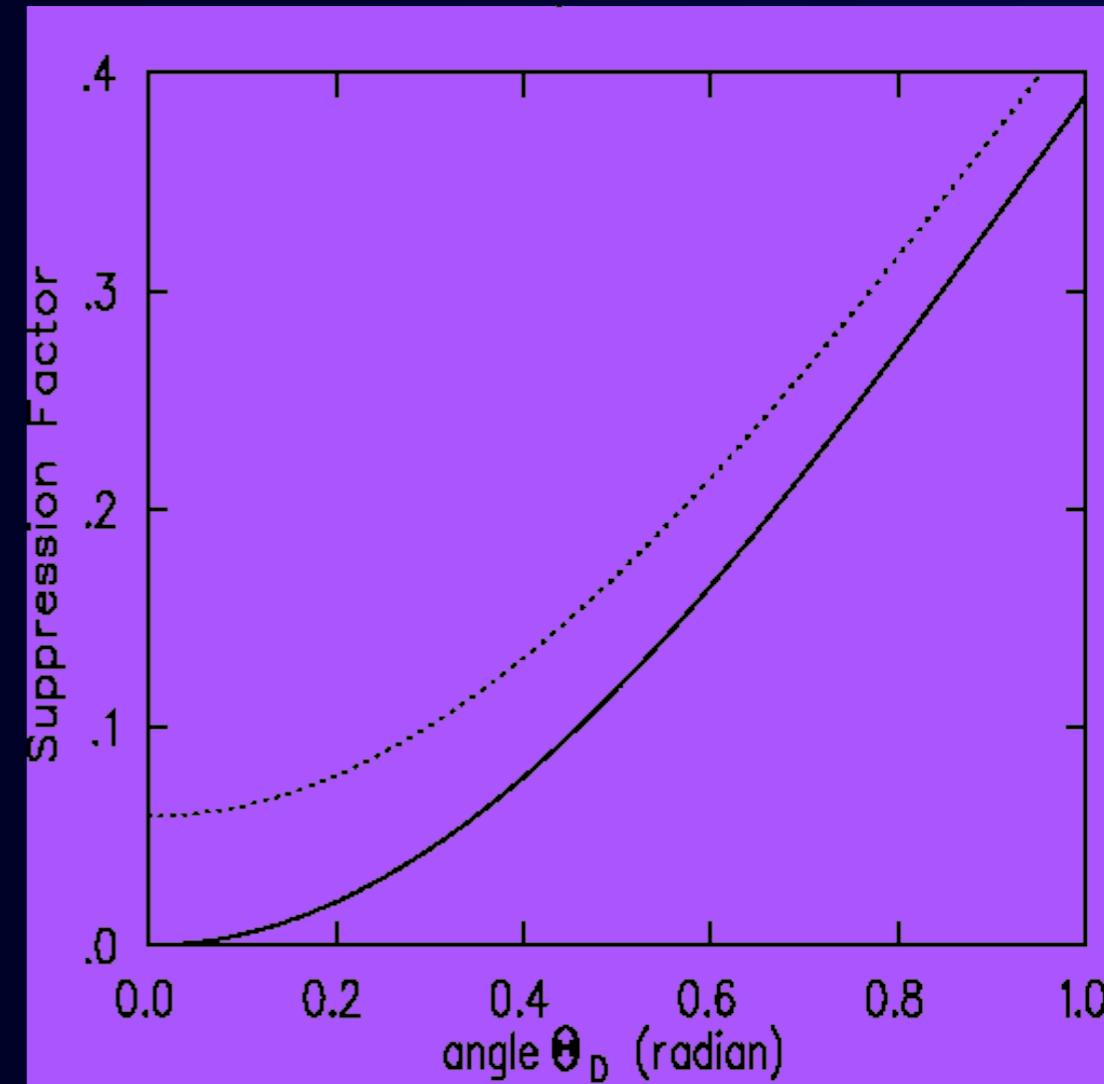
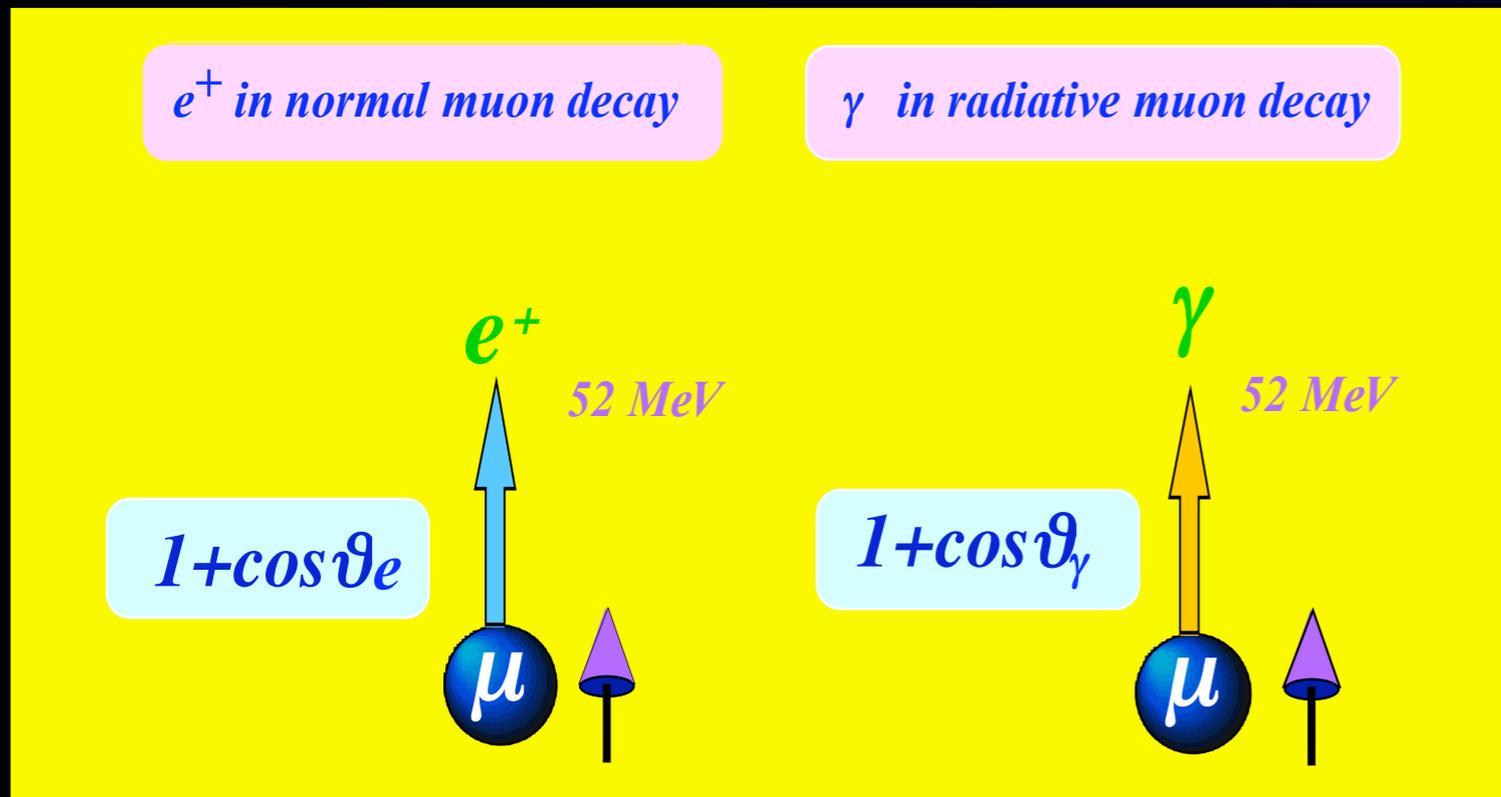
## Angular distribution of Physics Background with polarized muon decays



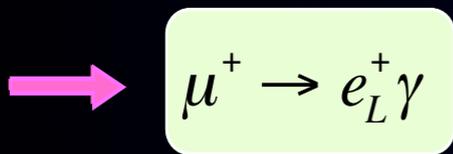
Y. Kuno and Y. Okada, Phys. Rev. Lett. 77 (1996) 434

# Suppression of Accidental Background with Polarized $\mu \rightarrow e\gamma$ Decay

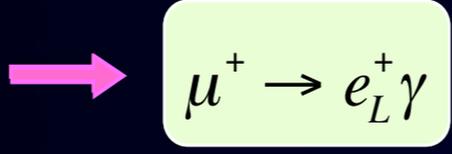
*accidental coincidence between 52.8 MeV  $e^+$  and 52.8 MeV photon.  
In a high-intensity beam, it becomes more serious.*



*suppressed if  $e^+$  going opposite to muon spin is measured*



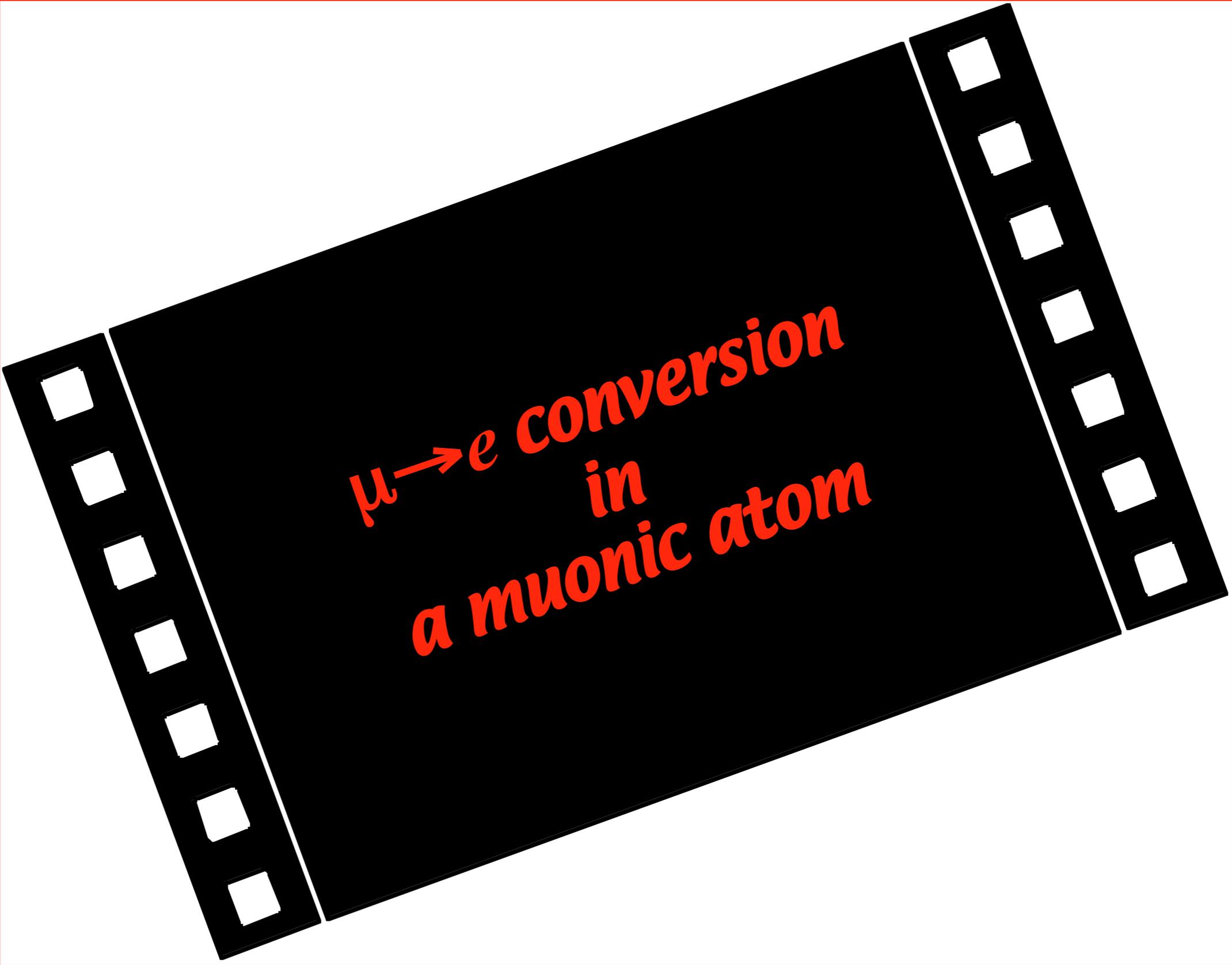
*suppressed if photons going opposite to muon spin is measured.*



*Both helicities are OK!*

$$\eta = \frac{\int_{\cos\theta_D}^1 d(\cos\theta) (1 + P_\mu \cos\theta)(1 - P_\mu \cos\theta)}{\int_{\cos\theta_D}^1 d(\cos\theta_D)}$$

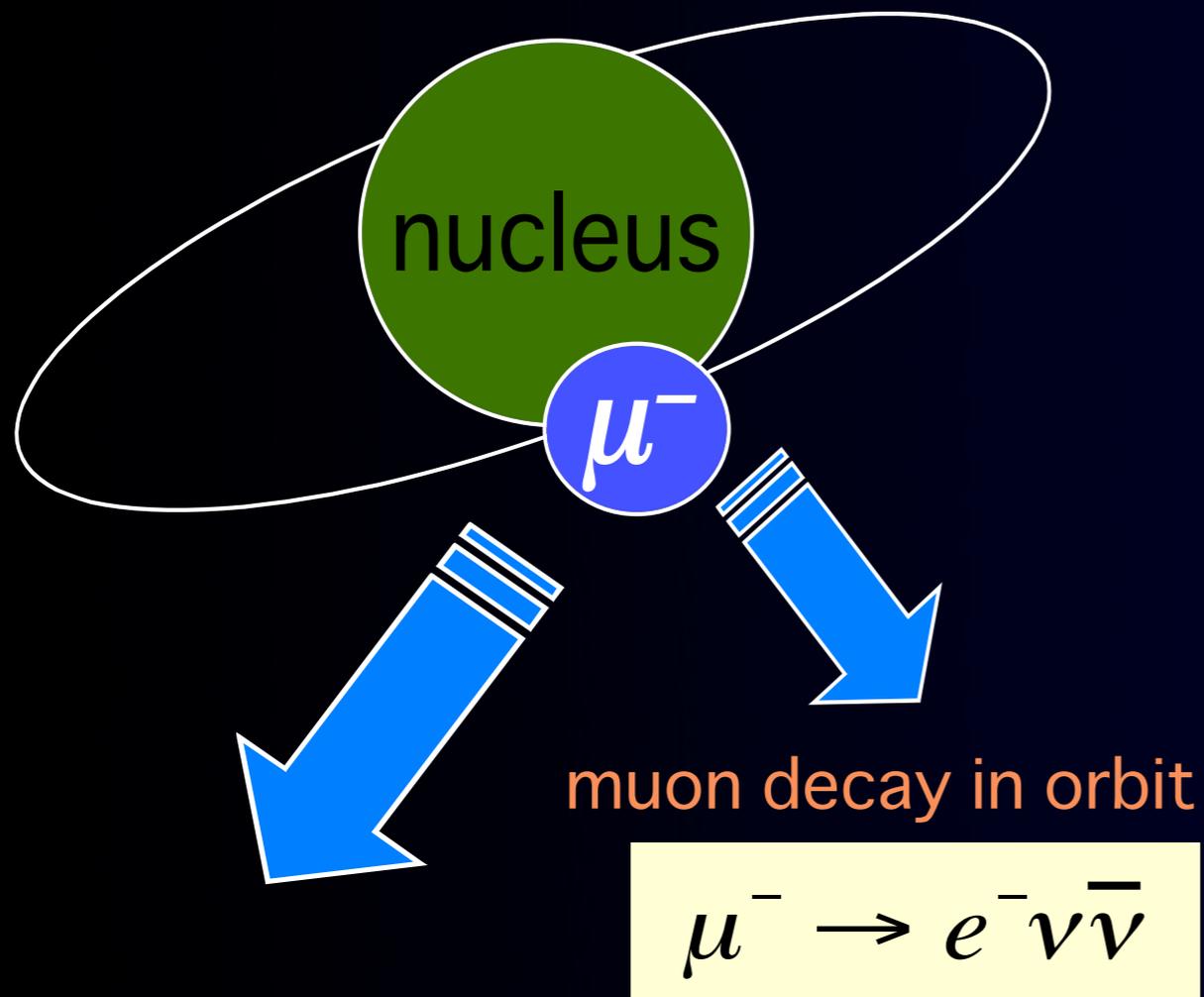
$$= (1 - P_\mu^2) + \frac{1}{3} P_\mu^2 (1 - \cos\theta_D)(2 + \cos\theta_D)$$



$\mu \rightarrow e$  conversion  
in  
a muonic atom

# What is a Muon to Electron Conversion ?

1s state in a muonic atom



nuclear muon capture

$$\mu^- + (A, Z) \rightarrow \nu_\mu + (A, Z - 1)$$

Neutrino-less muon  
nuclear capture  
(=μ-e conversion)

$$\mu^- + (A, Z) \rightarrow e^- + (A, Z)$$

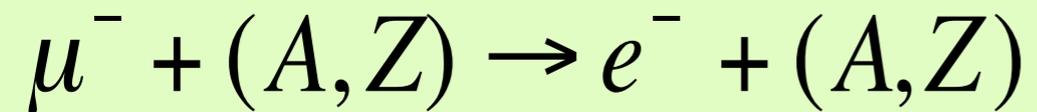
lepton flavors  
changes by one unit.

$$B(\mu^- N \rightarrow e^- N) = \frac{\Gamma(\mu^- N \rightarrow e^- N)}{\Gamma(\mu^- N \rightarrow \nu N')}$$

# $\mu$ -e Conversion

## Signal and Backgrounds

---



- **Signal**

- single mono-energetic electron

$$m_\mu - B_\mu \sim 105 \text{ MeV}$$

- The transition to the ground state is a coherent process, and enhanced by a number of nucleus.

$$\propto Z^5$$

- The ratio of excited states versus the ground state is about 1:9 for Ti.

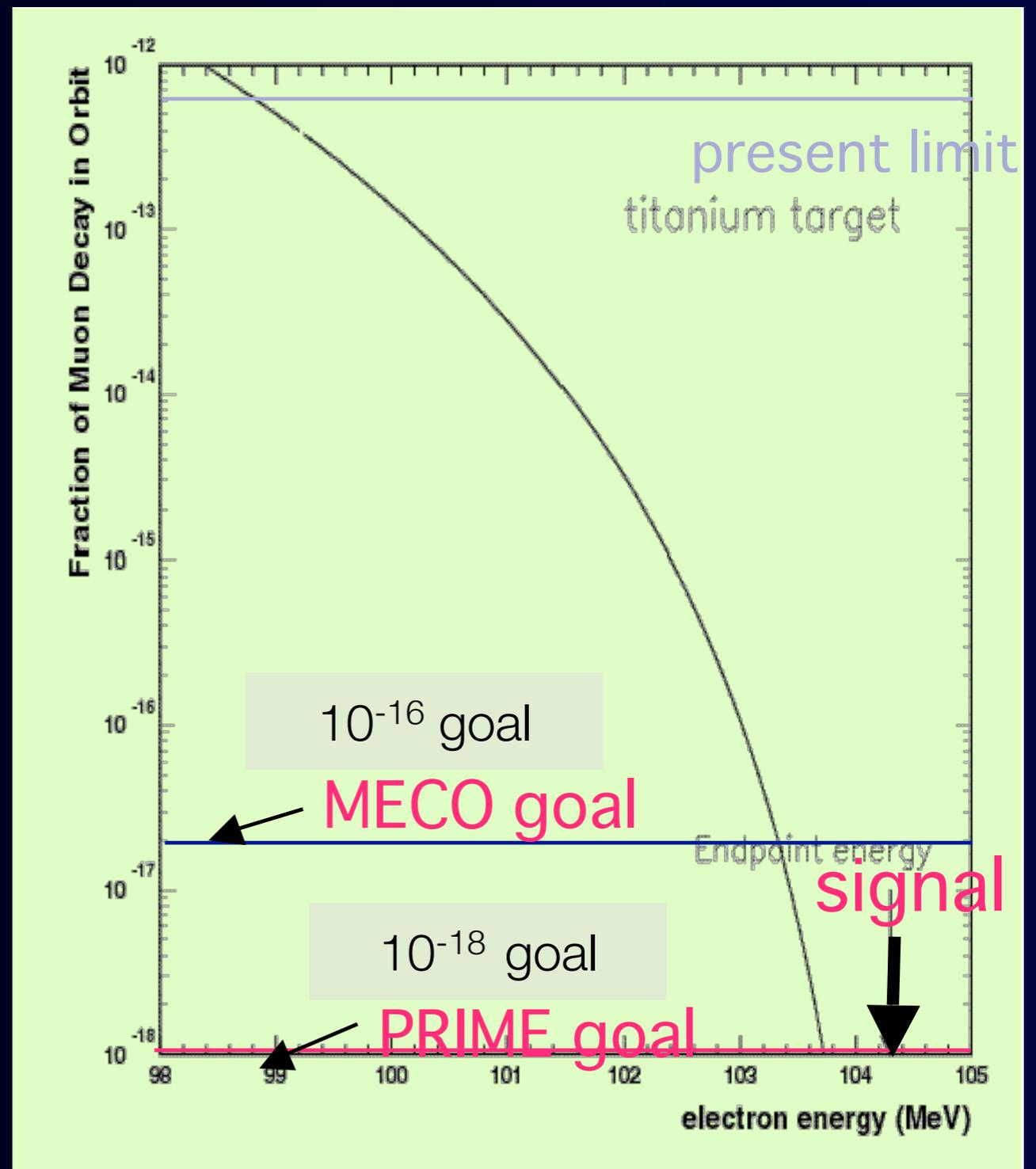
# Backgrounds

| Category                      | Examples of backgrounds                      |
|-------------------------------|--|
| Intrinsic Physics Backgrounds | muon decay in orbit (DIO)                    |
|                               | particle emissions from nuclear muon capture |
|                               | radiative muon capture (RMC)                 |
| Beam-related backgrounds      | radiative pion capture (RPC)                 |
|                               | muon decay in flight                         |
|                               | neutrons, kaons, and anti-protons            |
| Other Backgrounds             | cosmic rays                                  |
|                               | miss-tracking events                         |

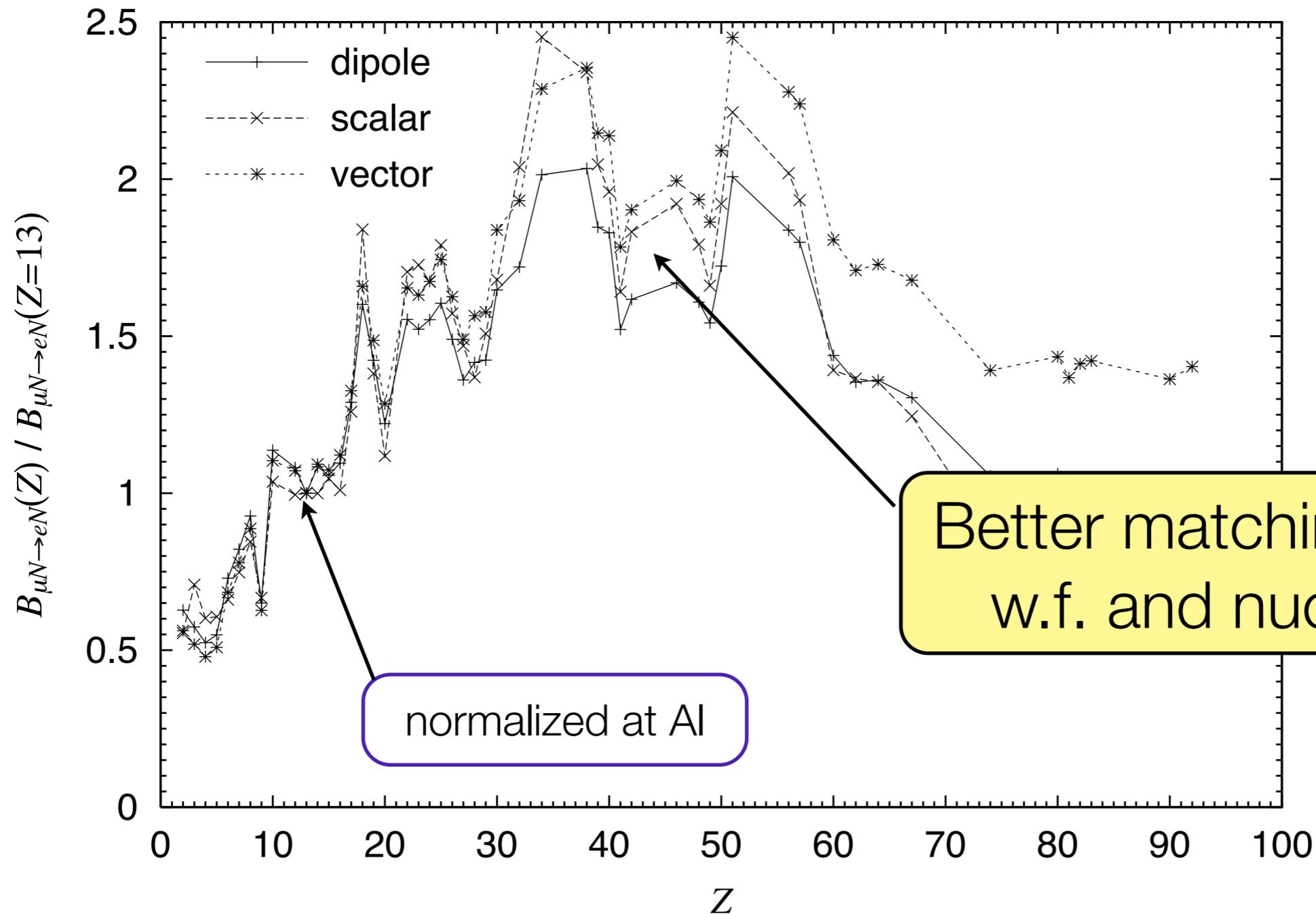
# Muon Decay In Orbit (DIO) in a Muonic Atom

- Normal muon decay has an endpoint of 52.8 MeV, whereas the end point of muon decay in orbit comes to the signal region.
- good resolution of electron energy (momentum) is needed.

$$\propto (\Delta E)^5$$



# $\mu$ -e Conversion : Target dependence (discriminating effective interaction)

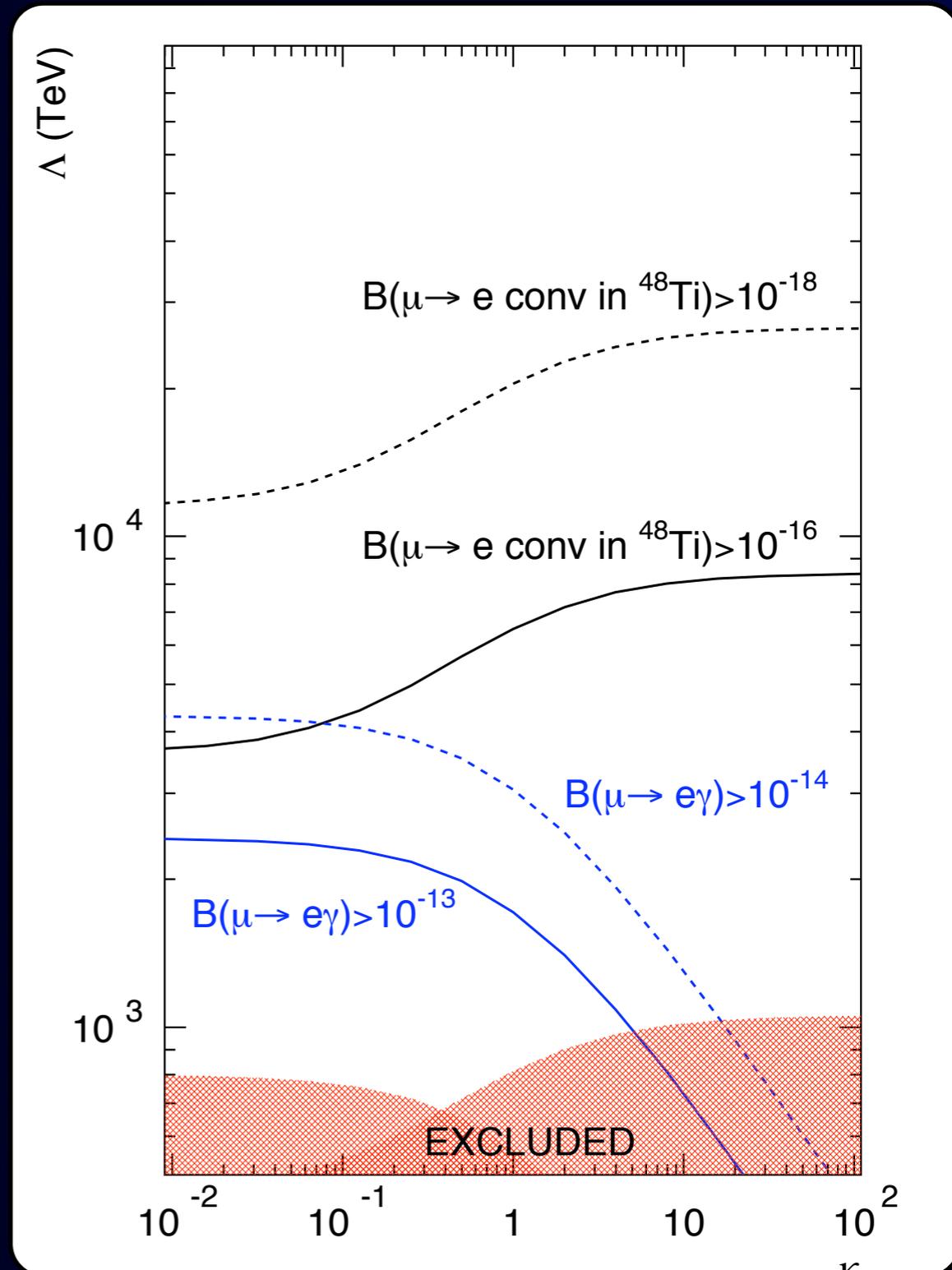


# Physics Sensitivity Comparison between $\mu \rightarrow e\gamma$ and $\mu$ -e Conversion

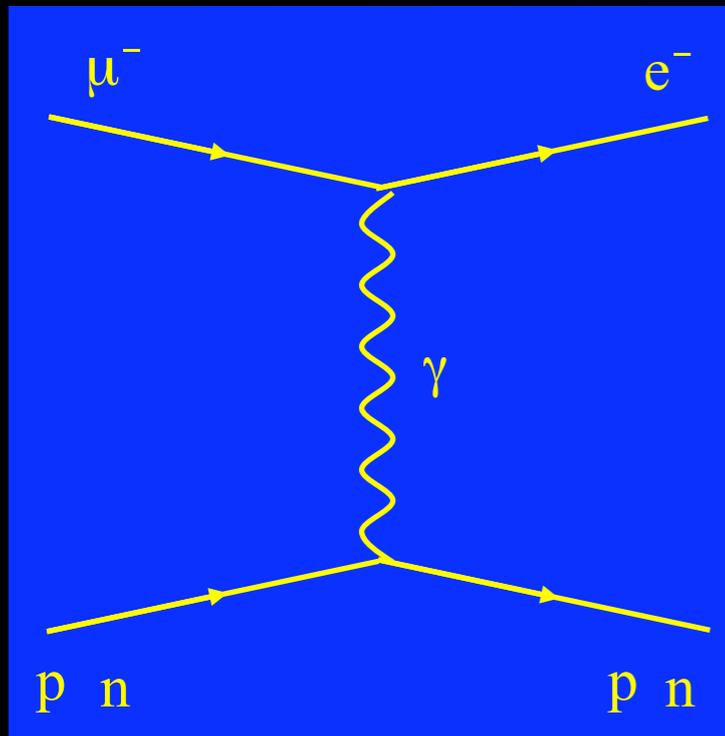
Photonic (dipole) and non-photonic contributions

|                           | photonic (dipole) | non-photonic |
|---------------------------|-------------------|--------------|
| $\mu \rightarrow e\gamma$ | yes (on-shell)    | no           |
| $\mu$ -e conversion       | yes (off-shell)   | yes          |

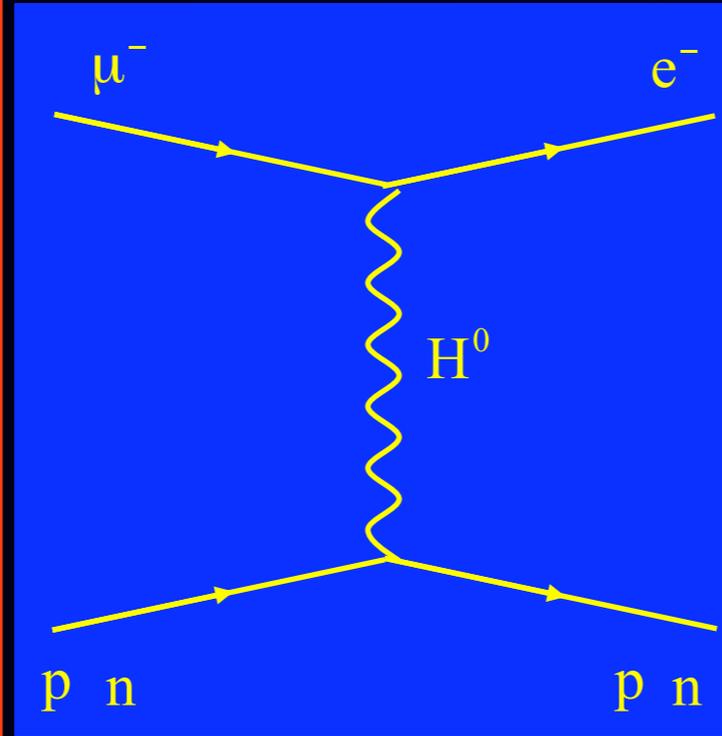
more sensitive to new physics



# SUSY Higgs Mediated Contribution (large $\tan\beta$ )

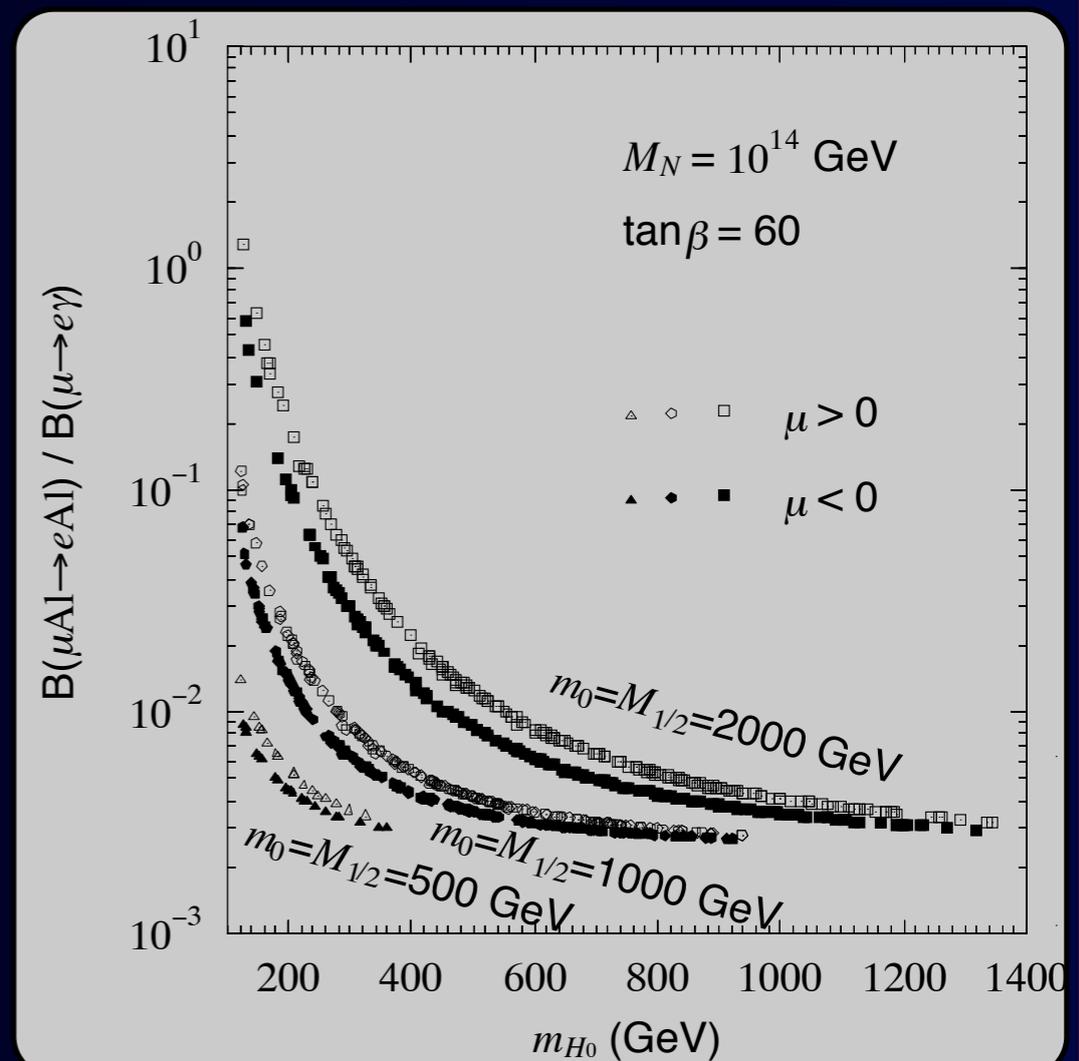


$$\frac{B(\mu N \rightarrow e N)}{B(\mu \rightarrow e \gamma)} \sim \frac{1}{100}$$



$$\frac{B(\mu N \rightarrow e N)}{B(\mu \rightarrow e \gamma)} \sim O(1)$$

R. Kitano, M. Koike, S. Komine and Y. Okada, Phys. Lett. B575, 300 (2003)



# Experimental Comparison between $\mu \rightarrow e\gamma$ and $\mu$ -e Conversion

---

|                             | background  | challenge           | beam intensity |
|-----------------------------|-------------|---------------------|----------------|
| • $\mu \rightarrow e\gamma$ | accidentals | detector resolution | limited        |
| • $\mu$ -e conversion       | beam        | beam background     | no limitation  |

- $\mu \rightarrow e\gamma$  : Accidental background is given by  $(\text{rate})^2$ . The detector resolutions have to be improved, but they (in particular, photon) would be hard to go beyond MEG from present technology. The ultimate sensitivity would be about  $10^{-14}$  (with about  $10^8/\text{sec}$ ) unless the detector resolution is radically improved.
- $\mu$ -e conversion : Improvement of a muon beam can be possible, both in purity (no pions) and in intensity (thanks to muon collider R&D). A higher beam intensity can be taken because of no accidentals.

$\mu$ -e conversion might be a next step.



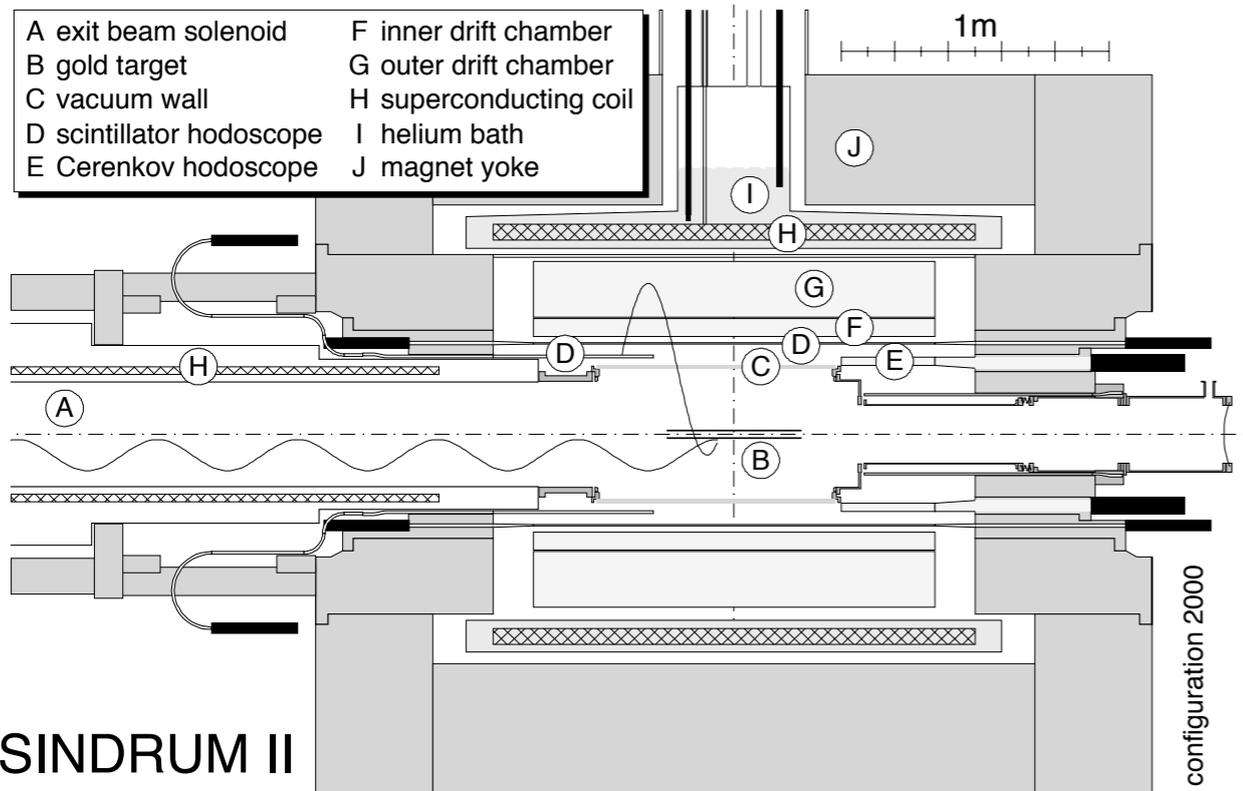
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throughout 2009

**extreme  
BEAM**

# Experimental Design for Muon to Electron Conversion

# Previous Measurements

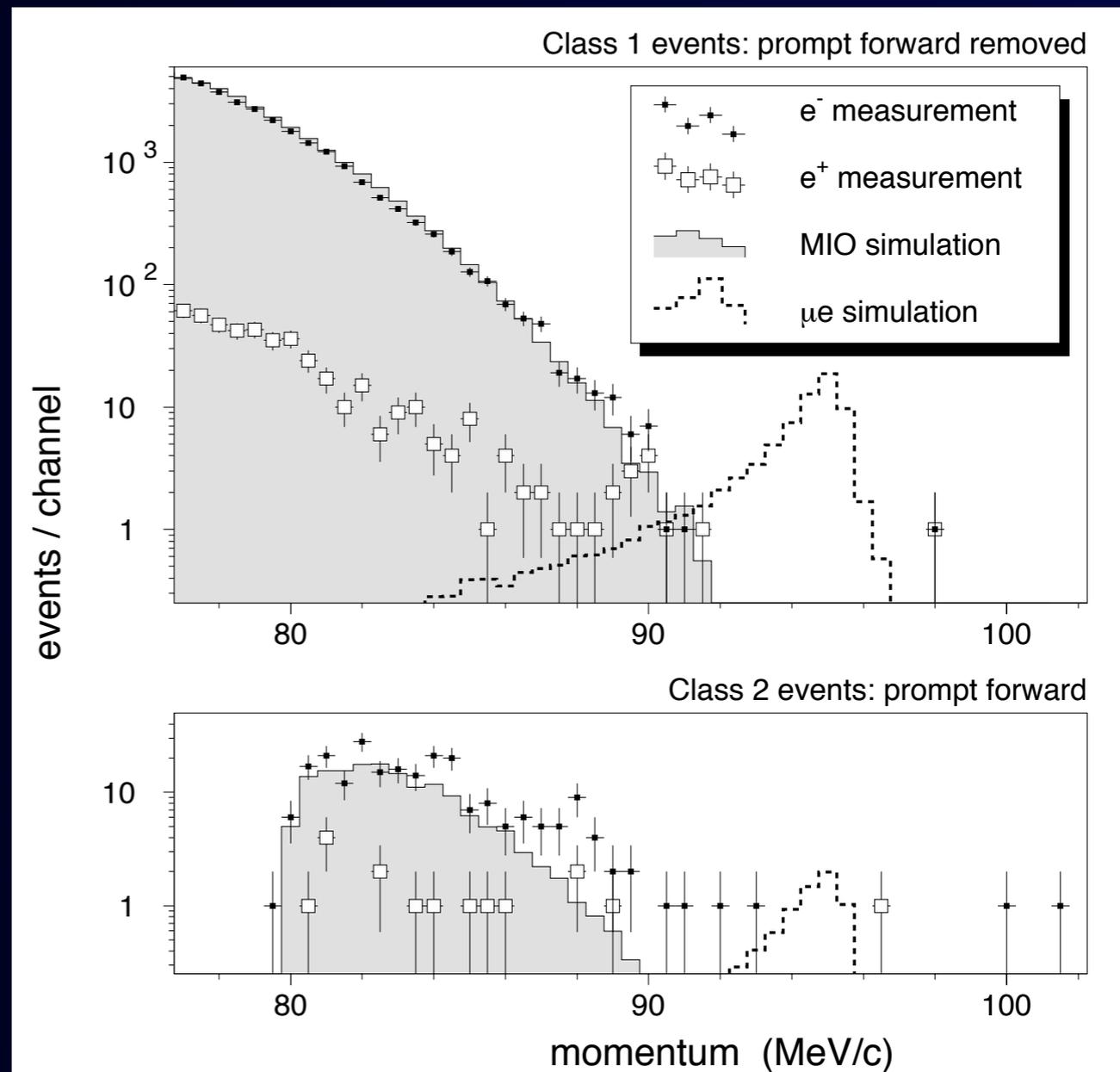
## SINDRUM-II (PSI)



PSI muon beam intensity  $\sim 10^{7-8}/\text{sec}$   
 beam from the PSI cyclotron. To eliminate  
 beam related background from a beam, a  
 beam veto counter was placed. But, it  
 could not work at a high rate.

## Published Results (2004)

$$B(\mu^- + Au \rightarrow e^- + Au) < 7 \times 10^{-13}$$



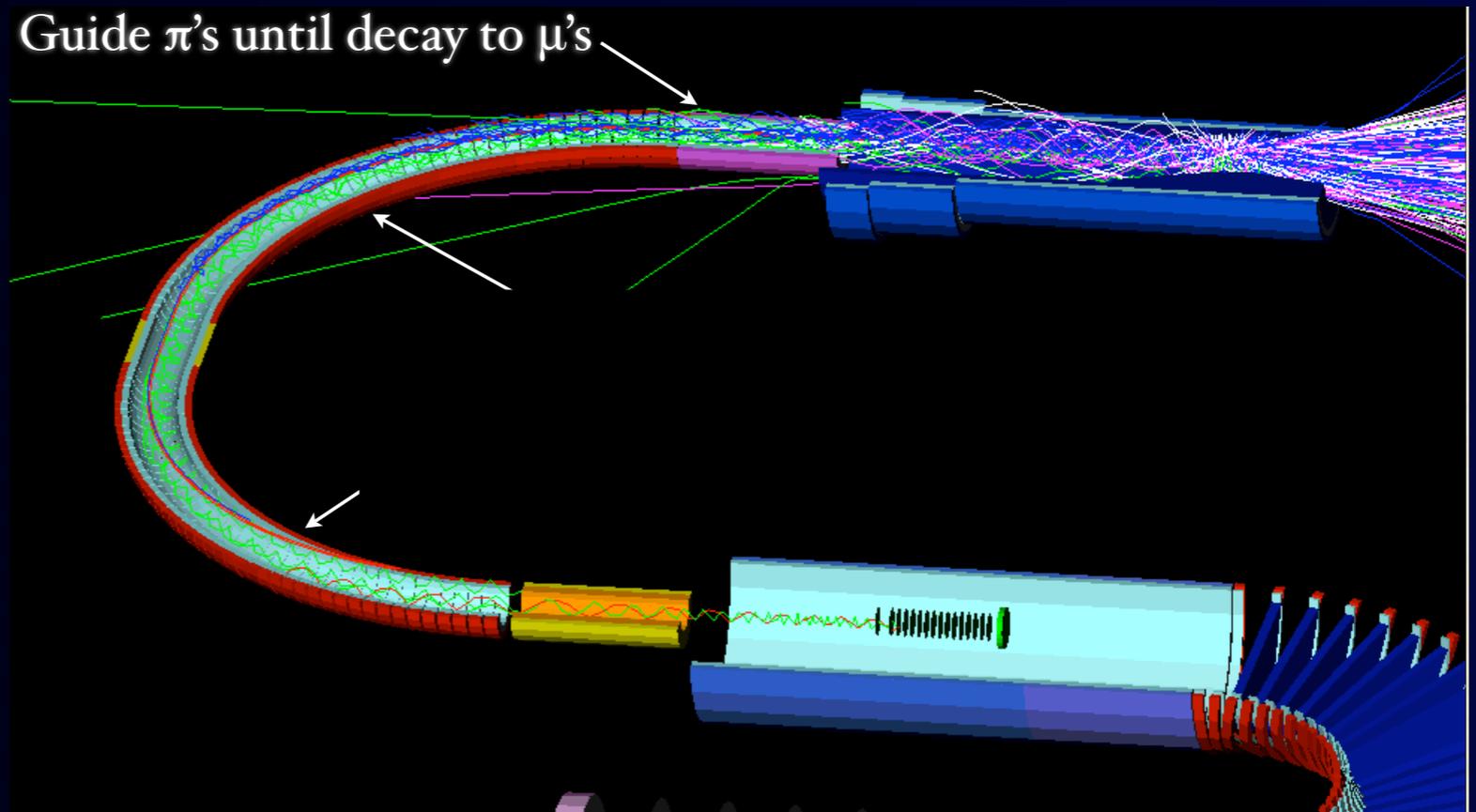
# Improvements for Signal Sensitivity

To achieve a single sensitivity of  $10^{-16}$ , we need

**$10^{11}$  muons/sec** (with  $10^7$  sec running)

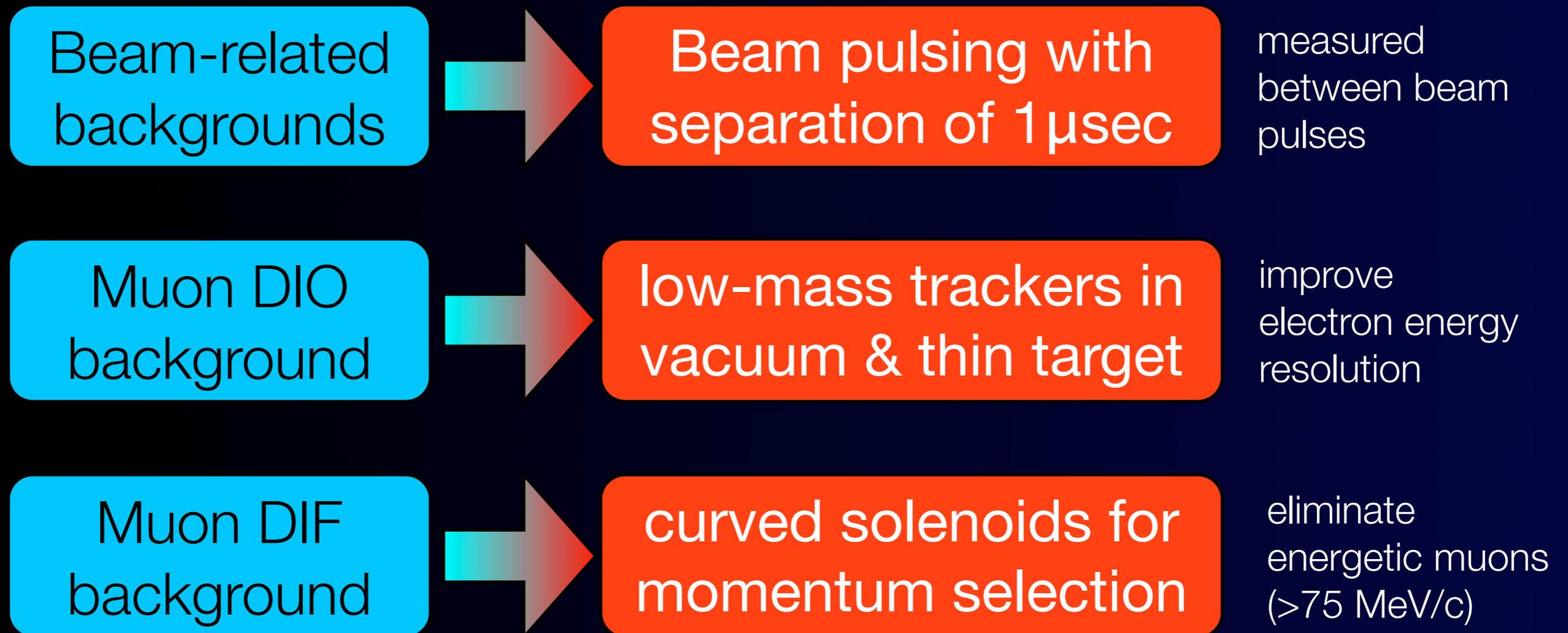
whereas the current highest intensity is  $10^8$ /sec at PSI.

Pion Capture and  
Muon Transport by  
Superconducting  
Solenoid System



# Improvements for Background Rejection

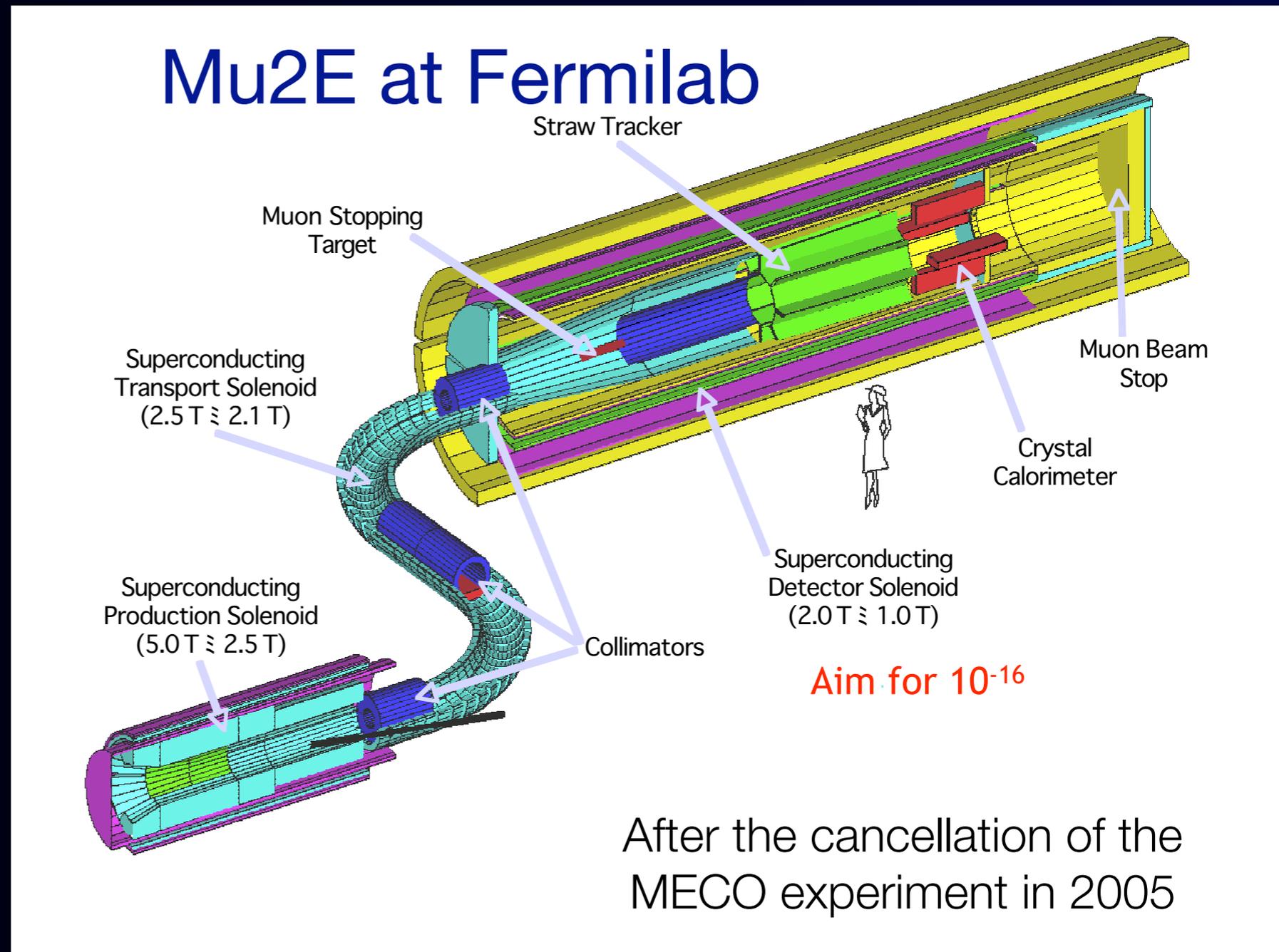
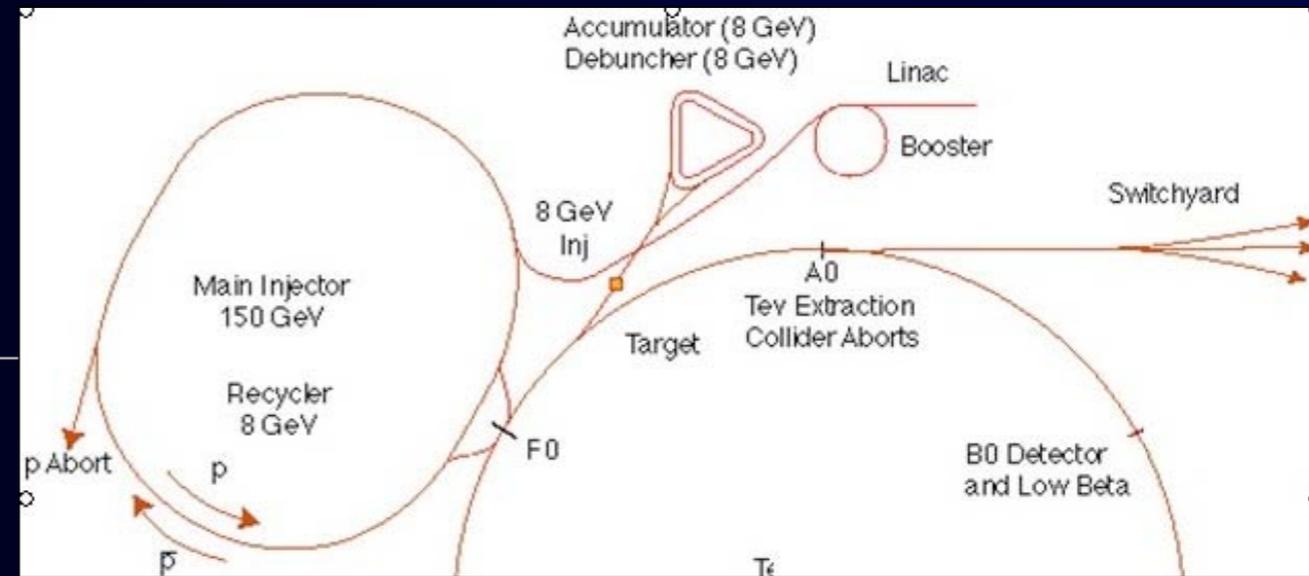
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base on the MELC proposal at Moscow Meson Factory

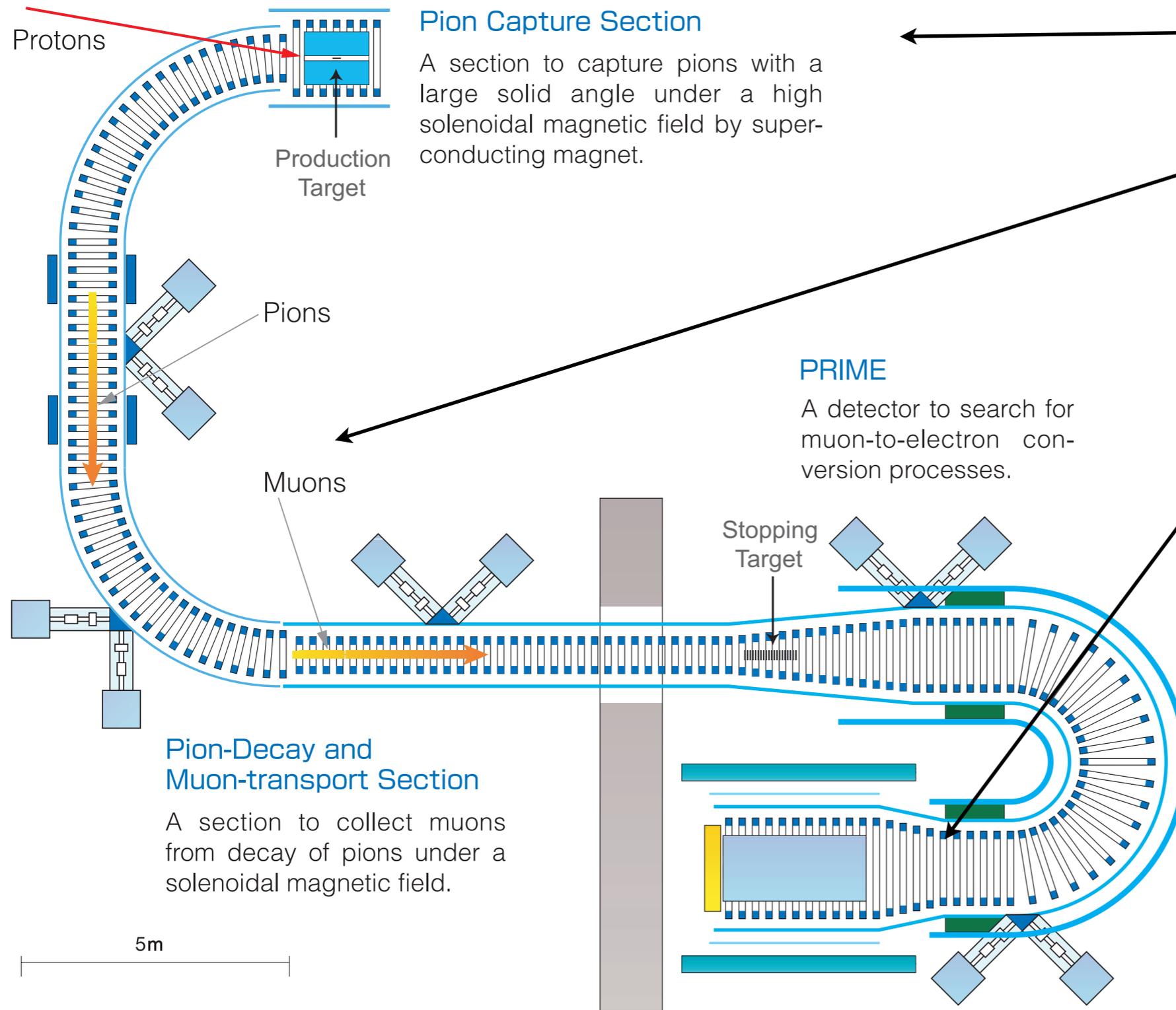
# Mu2E at Fermilab

- After Tevatron shutdown, use the antiproton accumulator ring and debuncher ring for beam pulsing.
- Proton beam power is 20 kW and 200 kW for pre and post Project-X.



# COMET (COherent Muon to Electron Transition) in Japan

$$B(\mu^- + Al \rightarrow e^- + Al) < 10^{-16}$$



Proton Beam

The Muon Source

- Proton Target
- Pion Capture
- Muon Transport

The Detector

- Muon Stopping Target
- Electron Transport
- Electron Detection

proposed to  
J-PARC

# Design Difference Between Mu2e and COMET

---

|                       | Mu2e              | COMET           |
|-----------------------|-------------------|-----------------|
| Muon Beam-line        | S-shape           | C-shape         |
| Electron Spectrometer | Straight solenoid | Curved solenoid |

# Charged Particle Trajectory in Curved Solenoids

- A center of helical trajectory of charged particles in a curved solenoidal field is drifted by

$$D = \frac{p}{qB} \theta_{bend} \frac{1}{2} \left( \cos \theta + \frac{1}{\cos \theta} \right)$$

$D$  : drift distance

$B$  : Solenoid field

$\theta_{bend}$  : Bending angle of the solenoid channel

$p$  : Momentum of the particle

$q$  : Charge of the particle

$\theta$  :  $\text{atan}(P_T/P_L)$

- This can be used for charge and momentum selection.

- This drift can be compensated by an auxiliary field parallel to the drift direction given by

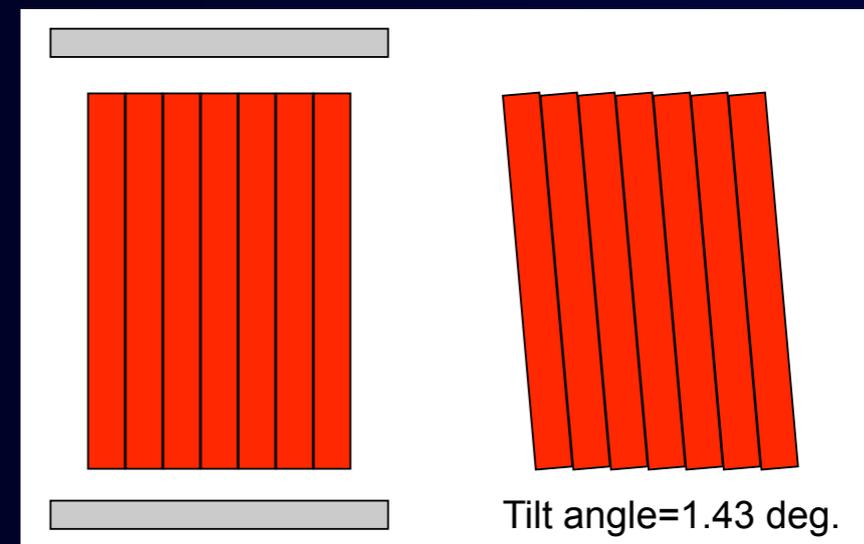
$$B_{comp} = \frac{p}{qr} \frac{1}{2} \left( \cos \theta + \frac{1}{\cos \theta} \right)$$

$p$  : Momentum of the particle

$q$  : Charge of the particle

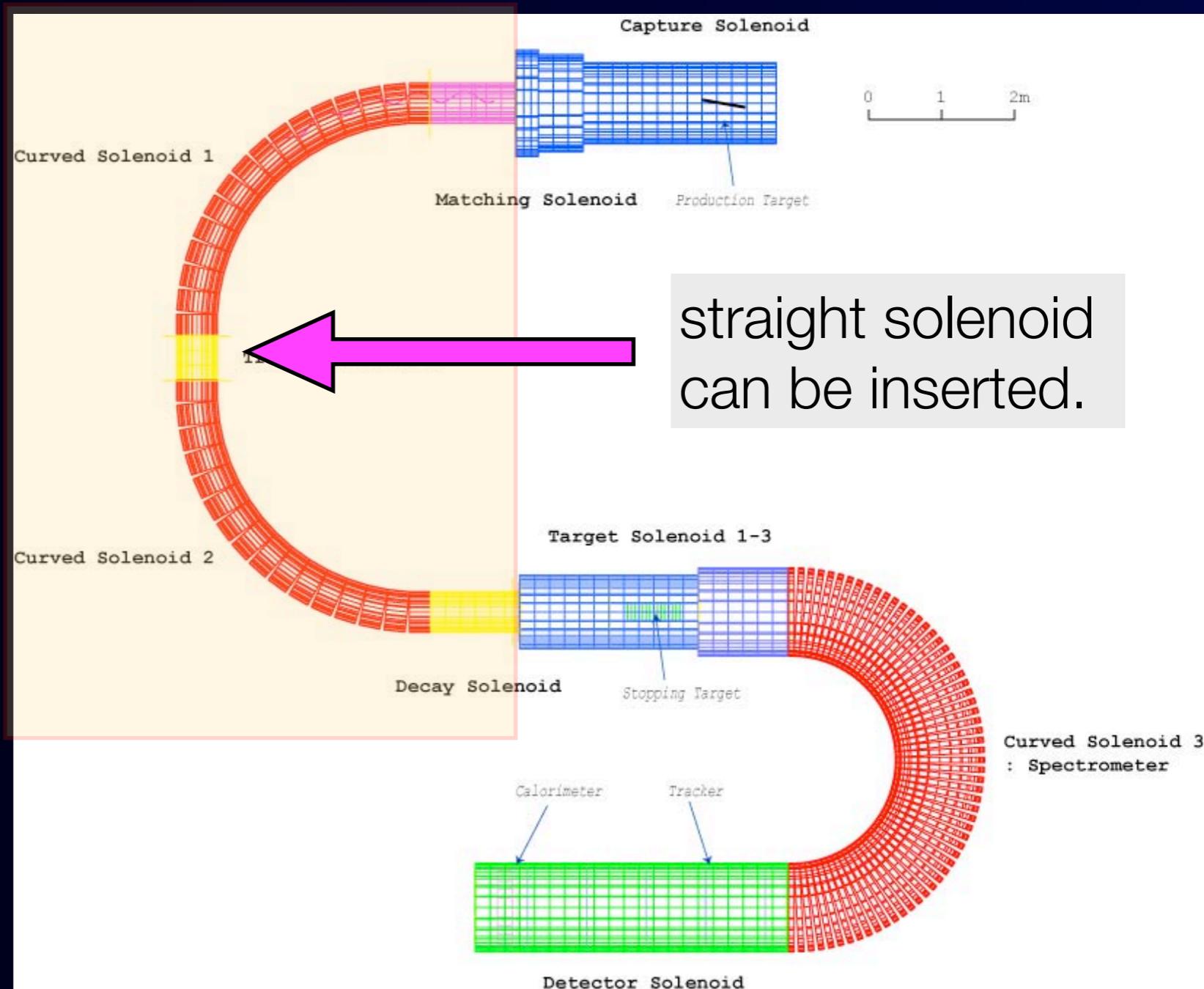
$r$  : Major radius of the solenoid

$\theta$  :  $\text{atan}(P_T/P_L)$



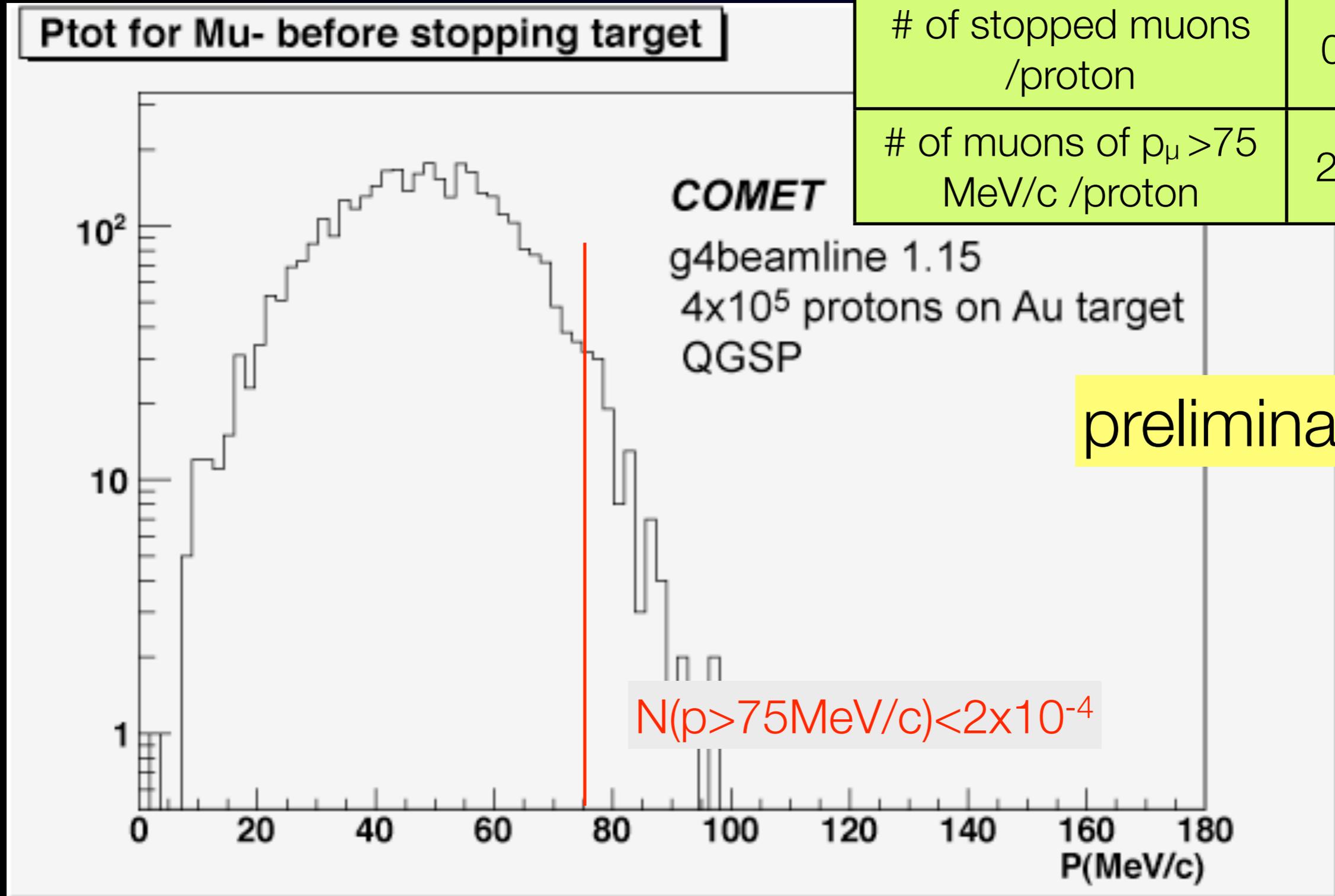
# Muon Transport Solenoid Beam-line for COMET

- C-shape beam line :
  - better beam momentum separation
  - collimators can be placed anywhere.
- Radius of curvature is about 3 meters.
- A straight solenoid section can be inserted between the two toroids.
- Reference momentum is 35 MeV/c for 1st bend and 47 MeV/c for 2nd bend.



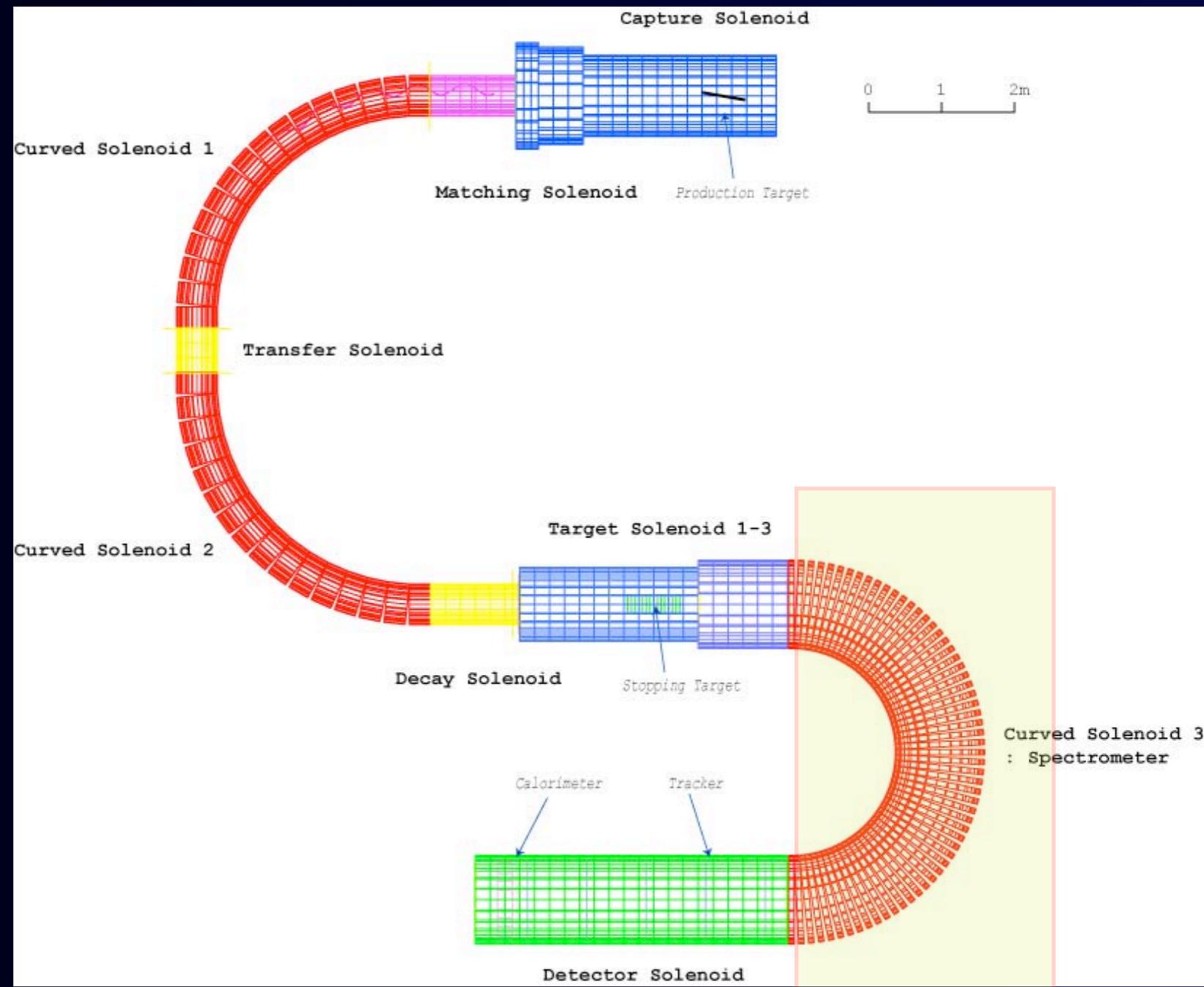
# Muon Momentum Spectrum at the End of the Transport Beam Line

|  |                    |
|--|--------------------|
| # of muons /proton                       | 0.009              |
| # of stopped muons /proton               | 0.003              |
| # of muons of $p_\mu > 75$ MeV/c /proton | $2 \times 10^{-4}$ |



# Curved Solenoid Spectrometer for COMET

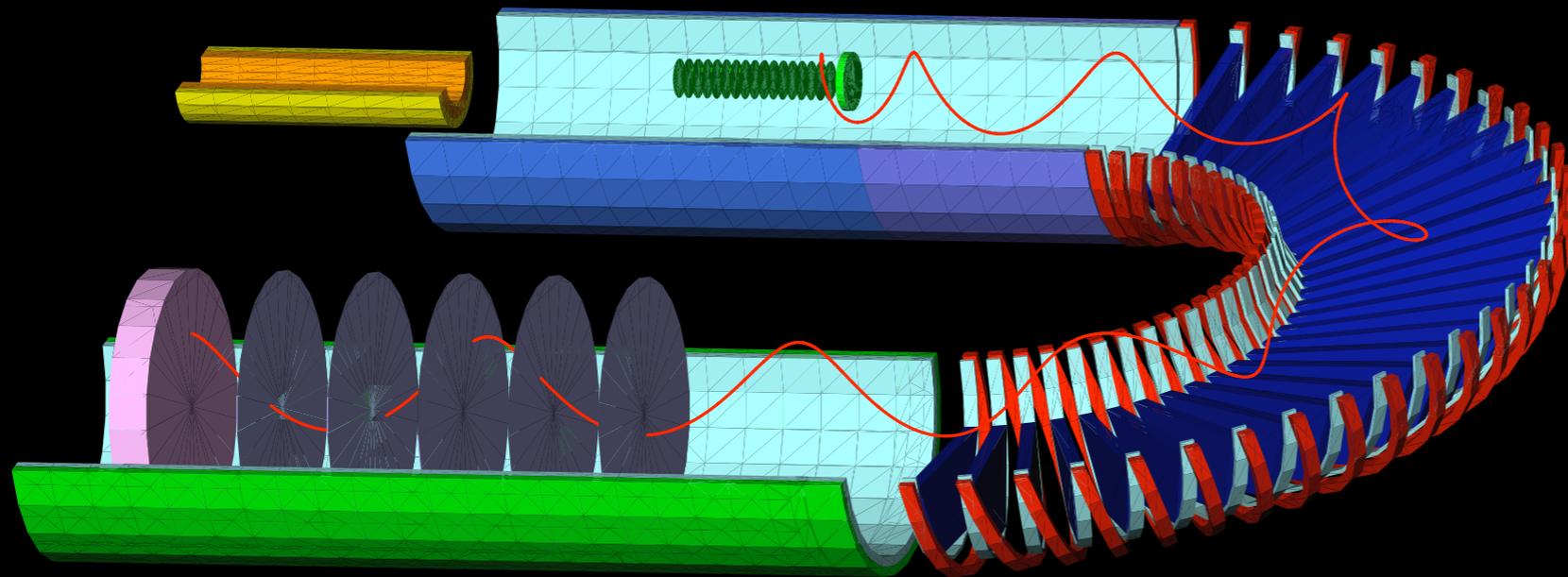
- 180 degree curved
  - Bore radius : 50 cm
  - Magnetic field : 1T
  - Bending angle : 180 degrees
- reference momentum  $\sim 104 \text{ MeV}/c$
- elimination of particles less than  $80 \text{ MeV}/c$  for rate issues
- a straight solenoid where detectors are placed follows the curved spectrometer.



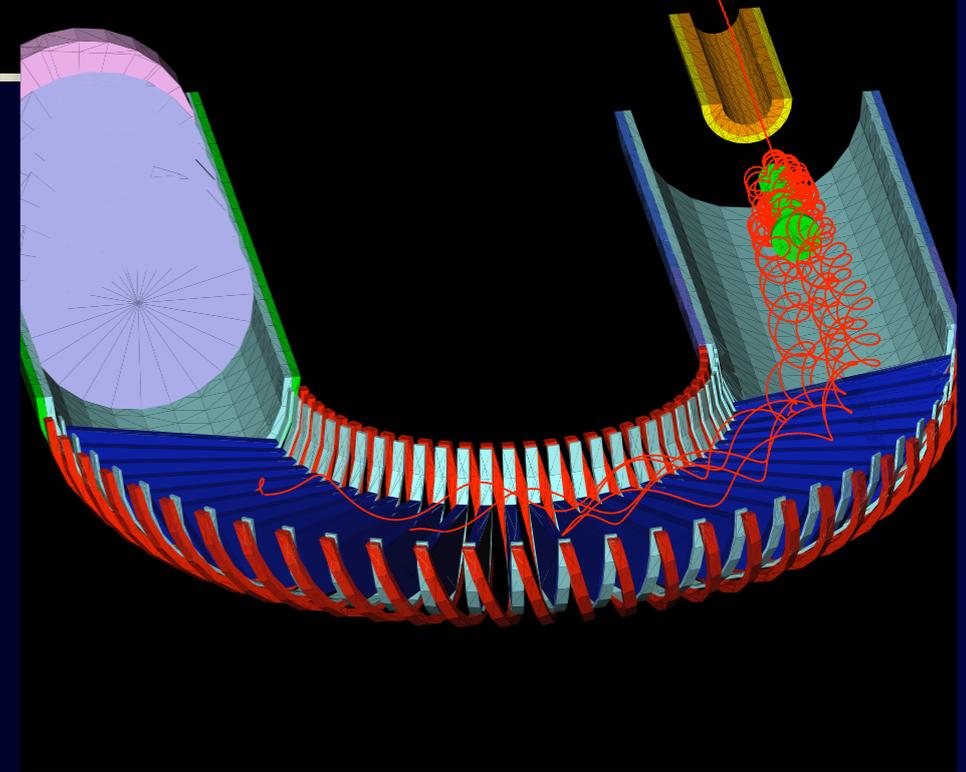
# Event Displays for Curved Solenoid Spectrometer

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105-MeV/c  $\mu$ -e electron



60-MeV/c DIO electrons



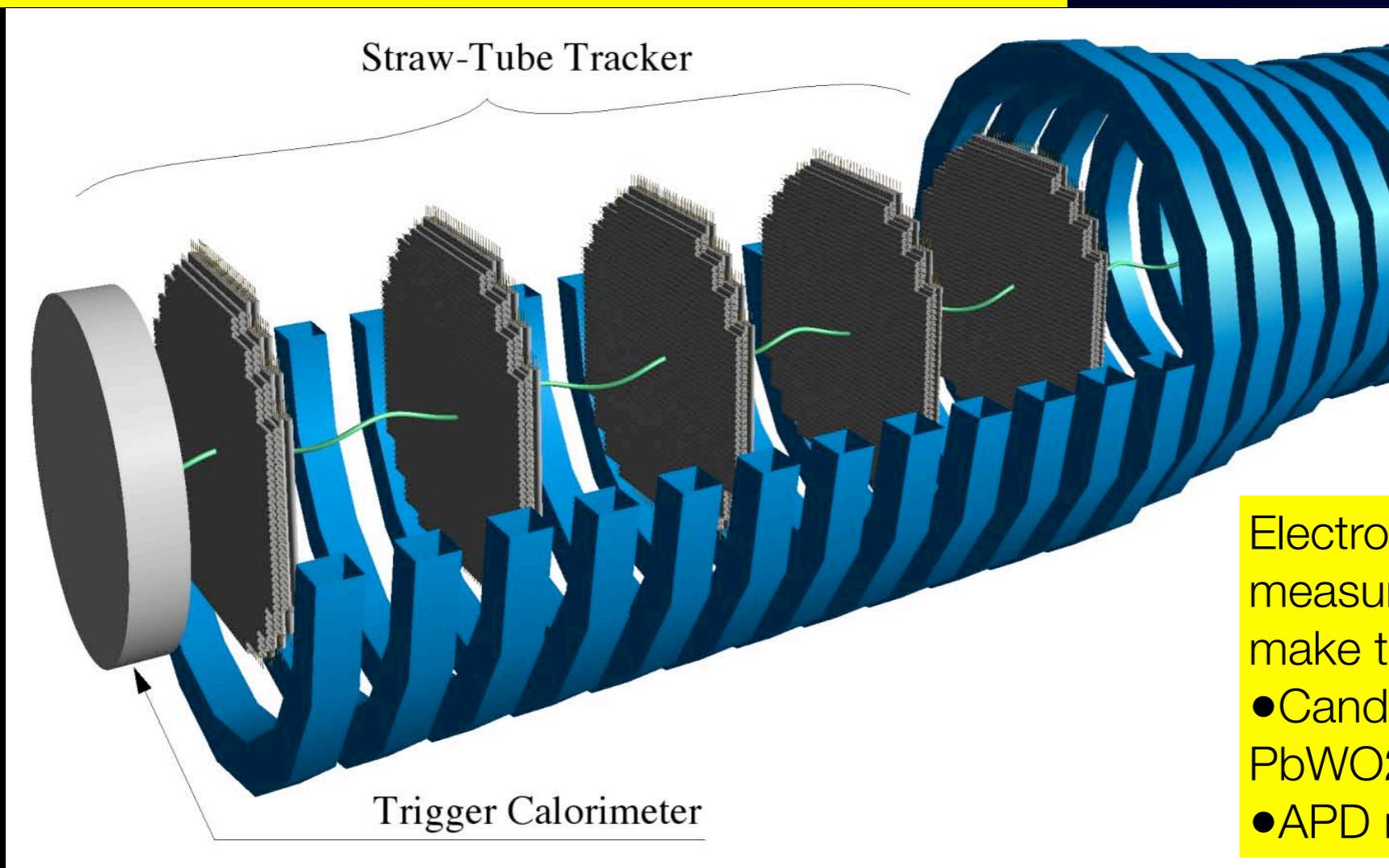
# Electron Detection (preliminary)

Straw-tube Trackers to measure electron momentum.

- should work in vacuum and under a magnetic field.
- A straw tube has  $25\mu\text{m}$  thick, 5 mm diameter.
- One plane has 2 views (x and y) with 2 layers per view.
- Five planes are placed with 48 cm distance.
- $250\mu\text{m}$  position resolution.

Under a solenoidal magnetic field of 1 Tesla.

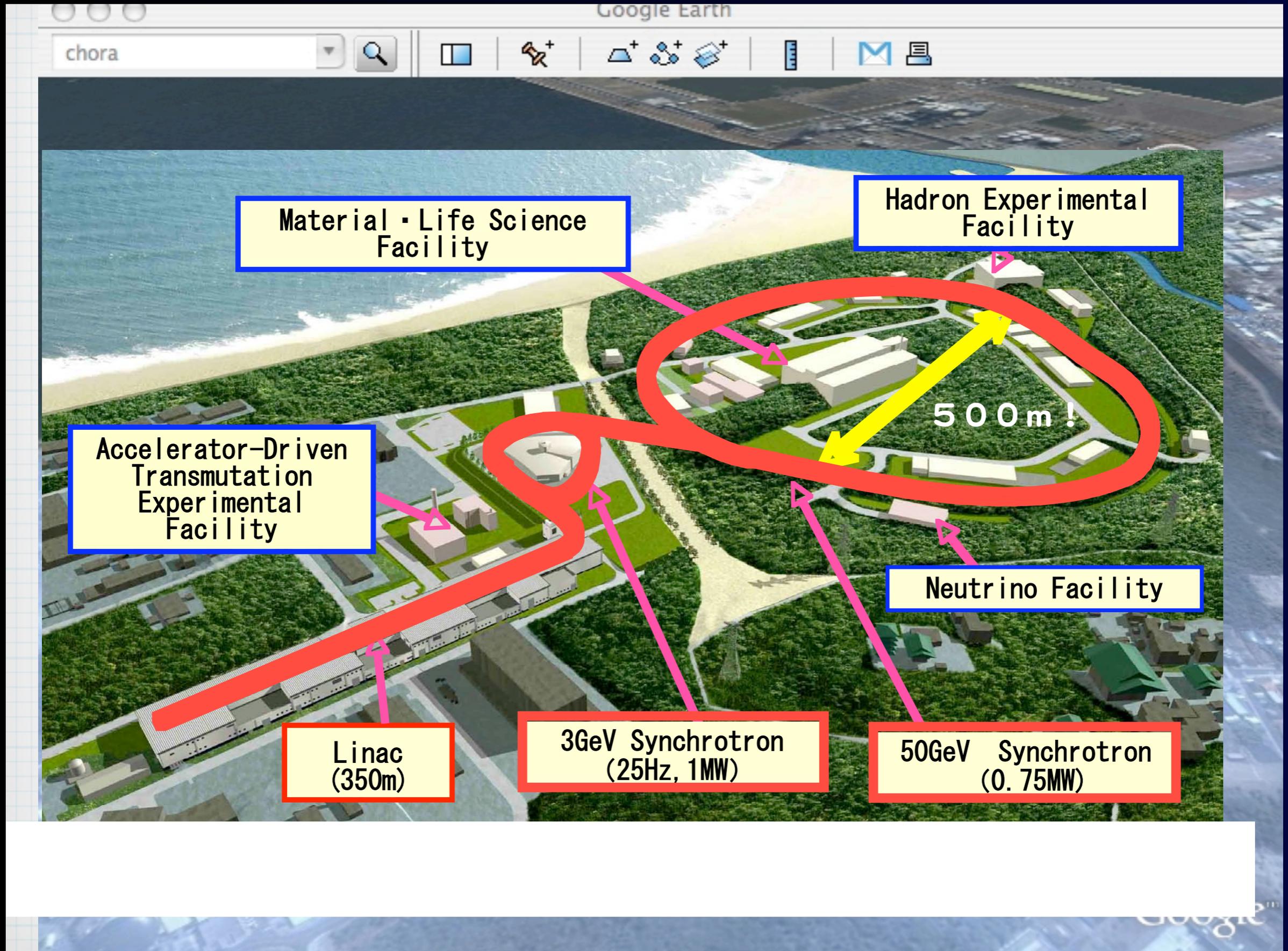
In vacuum to reduce multiple scattering.



Electron calorimeter to measure electron energy and make triggers.

- Candidate are GSO or  $\text{PbWO}_2$ .
- APD readout (no PMT).

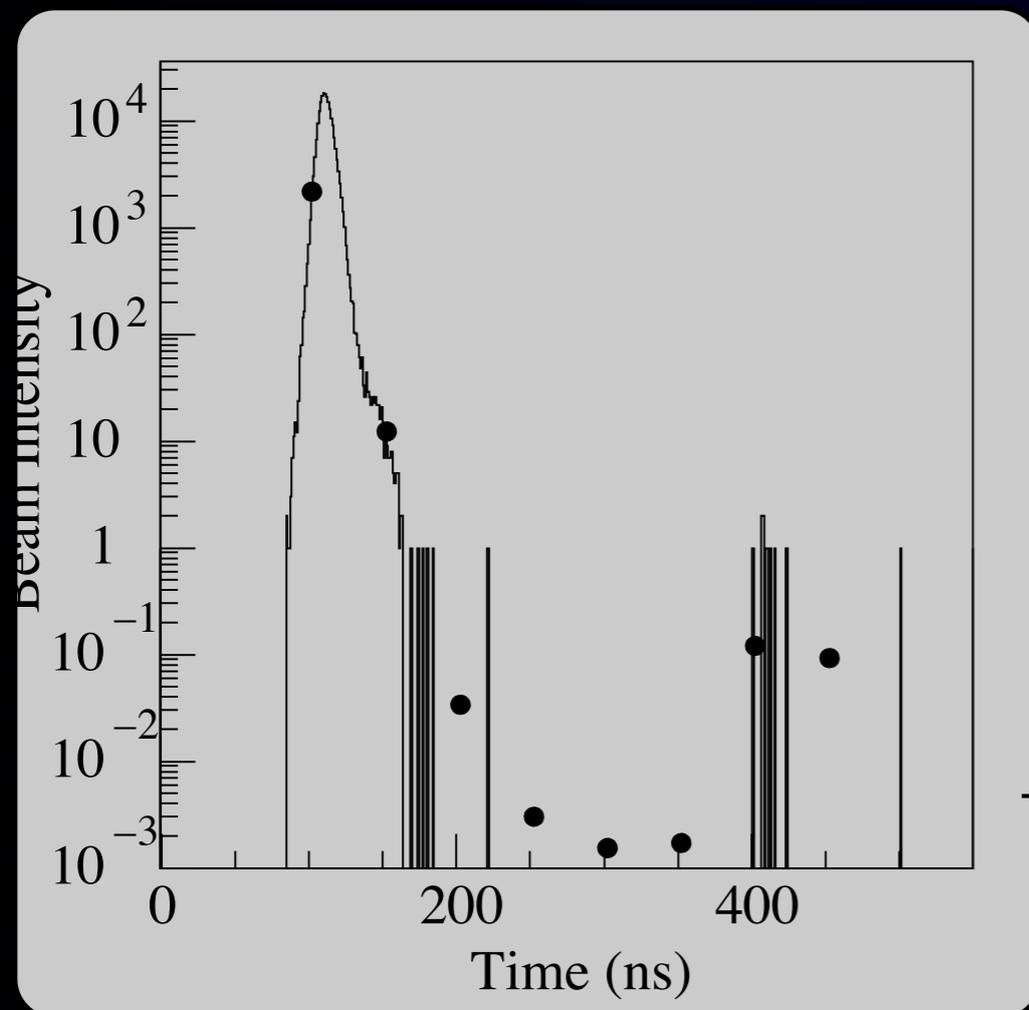
# J-PARC at Tokai, Japan





# Proton Beam at J-PARC (2)

- Proton Extinction :
  - $(\text{delayed})/(\text{prompt}) < 10^{-9}$
  - Test done at BNL-AGS gave  $10^{-7}$  (shown below).
  - Extra extinction are needed.



- Required Protons :
  - $4 \times 10^{20}$  protons of 8 GeV in total for a single event sensitivity of about  $0.33 \times 10^{-17}$ .
  - For  $1 \times 10^7$  sec running,  $4 \times 10^{13}$  protons /sec (= 7  $\mu$ A).
  - A total beam power is 56 kW, which is about 1/8 of the J-PARC full beam power of 450 kW (30 GeV x 15 $\mu$ A).

Test of Extinction at BNL-AGS

# Signal Sensitivity (preliminary) - 1 SSC years

- Single event sensitivity

$$B(\mu^- + Al \rightarrow e^- + Al) \sim \frac{1}{N_\mu \cdot f_{cap} \cdot A_e},$$

- $N_\mu$  is a number of stopping muons in the muon stopping target. It is  $1.1 \times 10^{18}$  muons.
- $f_{cap}$  is a fraction of muon capture, which is 0.6 for aluminum.
- $A_e$  is the detector acceptance, which is 0.04.

|                           |                      |
|---------------------------|----------------------|
| total protons             | $4 \times 10^{20}$   |
| muon transport efficiency | 0.009                |
| muon stopping efficiency  | 0.3                  |
| # of stopped muons        | $1.1 \times 10^{18}$ |

$$B(\mu^- + Al \rightarrow e^- + Al) = 3.3 \times 10^{-17}$$

$$B(\mu^- + Al \rightarrow e^- + Al) < 7 \times 10^{-17} \quad (90\% C.L.)$$

# Background Rejection Summary (preliminary)

| Backgrounds                                 | Events | Comments  |
|---|--------|---|
| Muon decay in orbit                         | 0.05   | 230 keV resolution                                |
| Radiative muon capture                      | <0.001 |   |
| Muon capture with neutron emission          | <0.001 |   |
| Muon capture with charged particle emission | <0.001 |   |
| Radiative pion capture*                     | 0.12   | prompt  |
| Radiative pion capture                      | 0.002  | late arriving pions                               |
| Muon decay in flight*                       | <0.02  |   |
| Pion decay in flight*                       | <0.001 |   |
| Beam electrons*                             | 0.08   |   |
| Neutron induced*                            | 0.024  | for high energy neutrons                          |
| Antiproton induced                          | 0.007  | for 8 GeV protons                                 |
| Cosmic-ray induced                          | 0.10   | 10 <sup>-4</sup> veto & 2x10 <sup>7</sup> sec run |
| Pattern recognition errors                  | <0.001 |   |
| Total                                       | 0.4    |   |



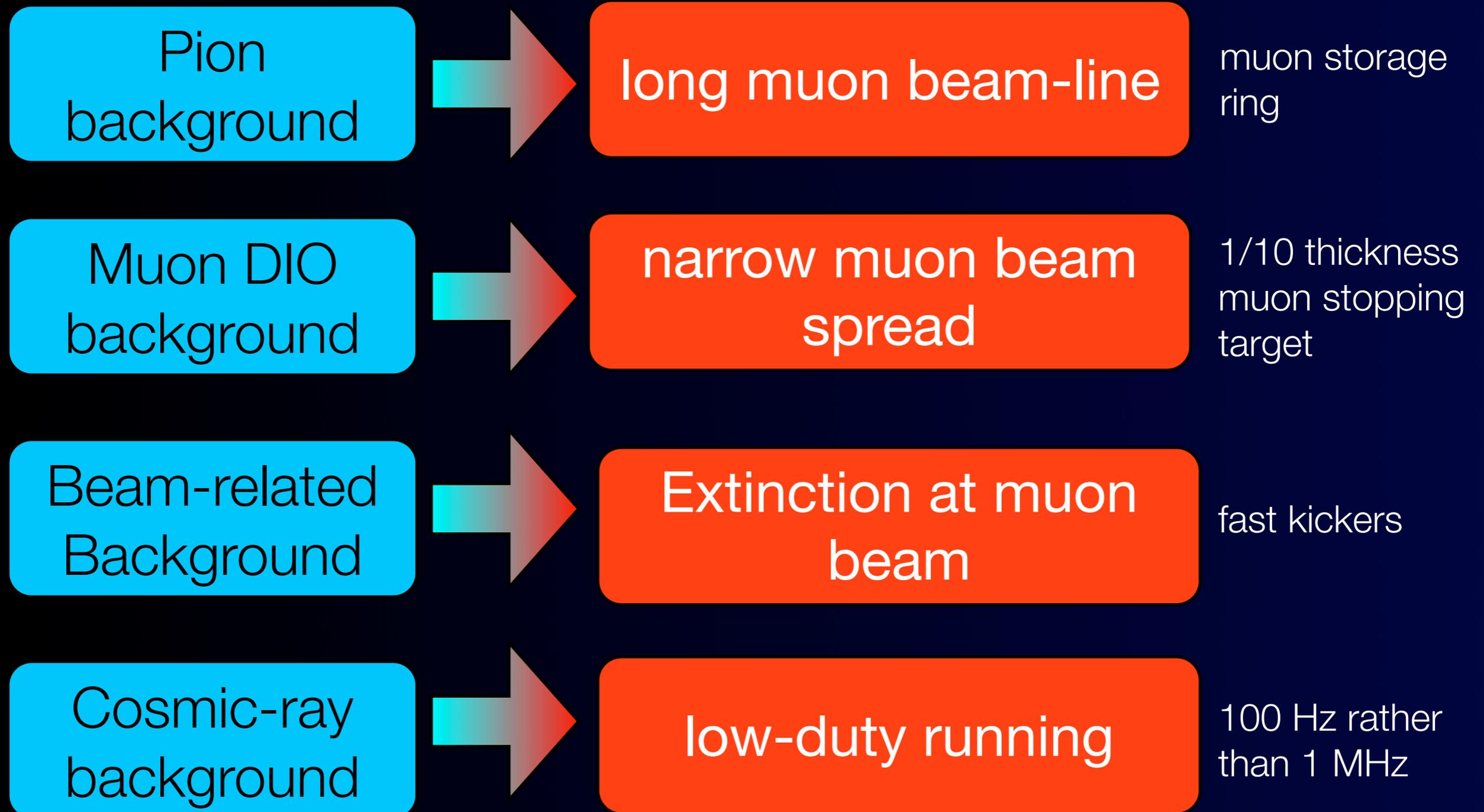
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$10^{-18}$  Sensitivity with PRISM

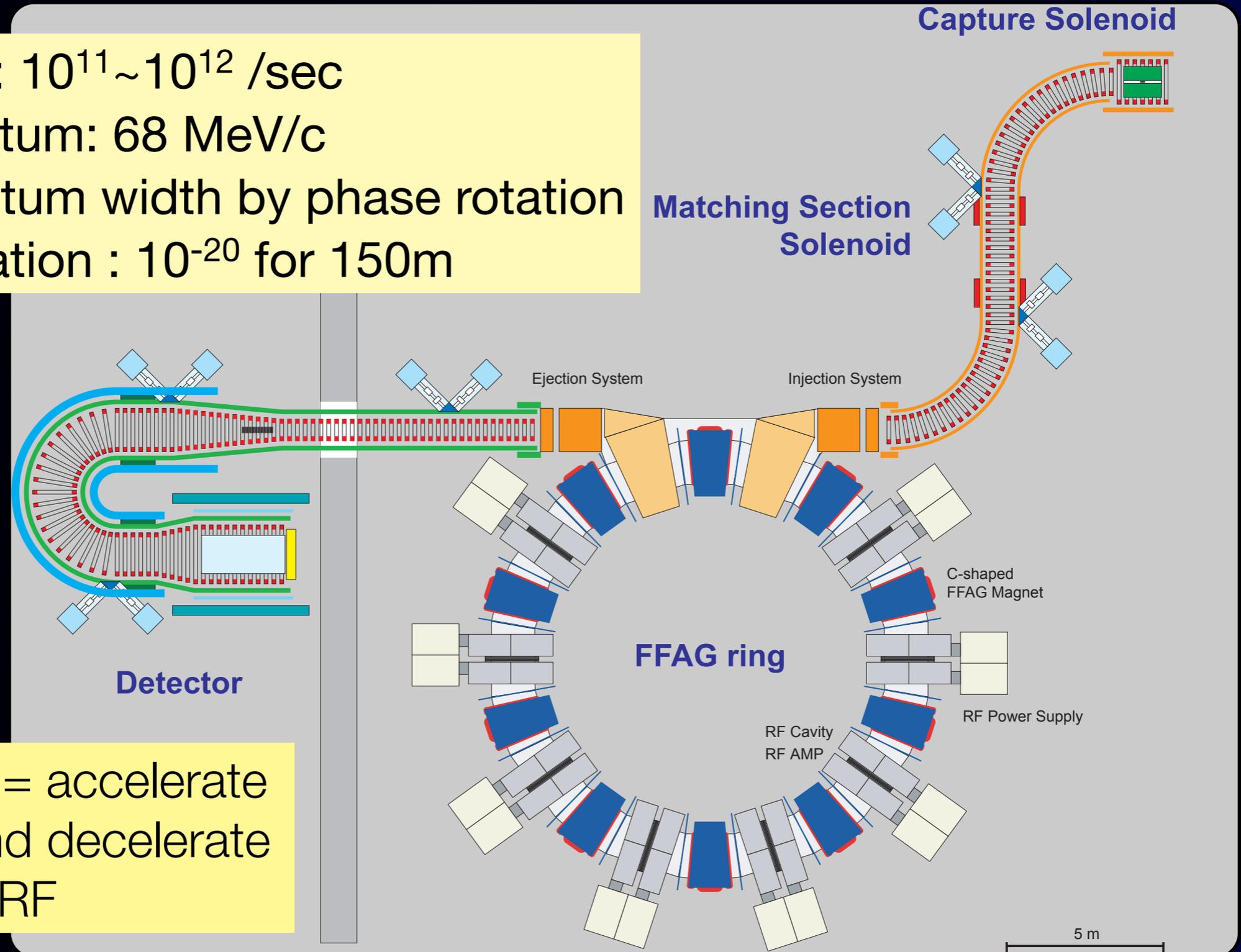
# Further Background Rejection to $< 10^{-18}$

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# PRISM Muon Beam

muon intensity:  $10^{11} \sim 10^{12}$  /sec  
 central momentum: 68 MeV/c  
 narrow momentum width by phase rotation  
 pion contamination :  $10^{-20}$  for 150m



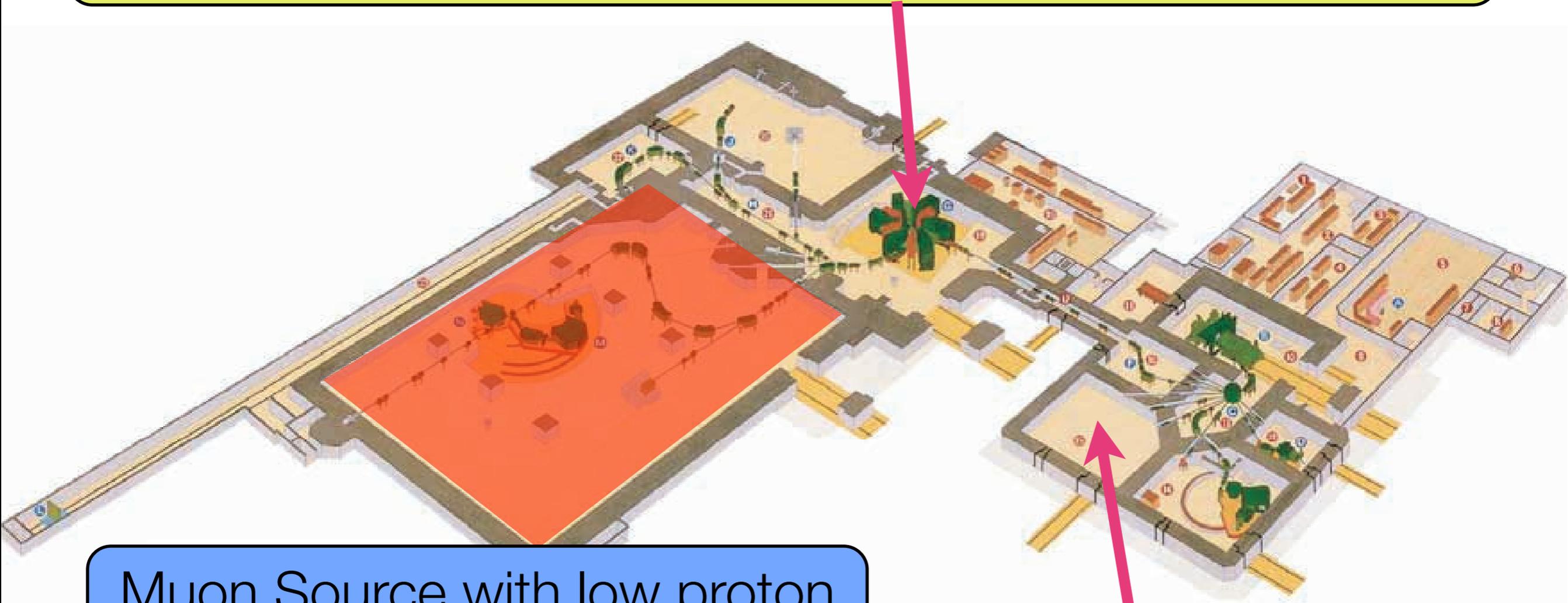
Phase rotation = accelerate  
 slow muons and decelerate  
 fast muons by RF

# R&D on the PRISM Muon Storage (FFAG) Ring at Osaka University



# Research Center for Nuclear Physics (RCNP), Osaka University

Research Center for Nuclear Physics (RCNP), Osaka University has a cyclotron of 400 MeV with 1 microA. The energy is above pion threshold.

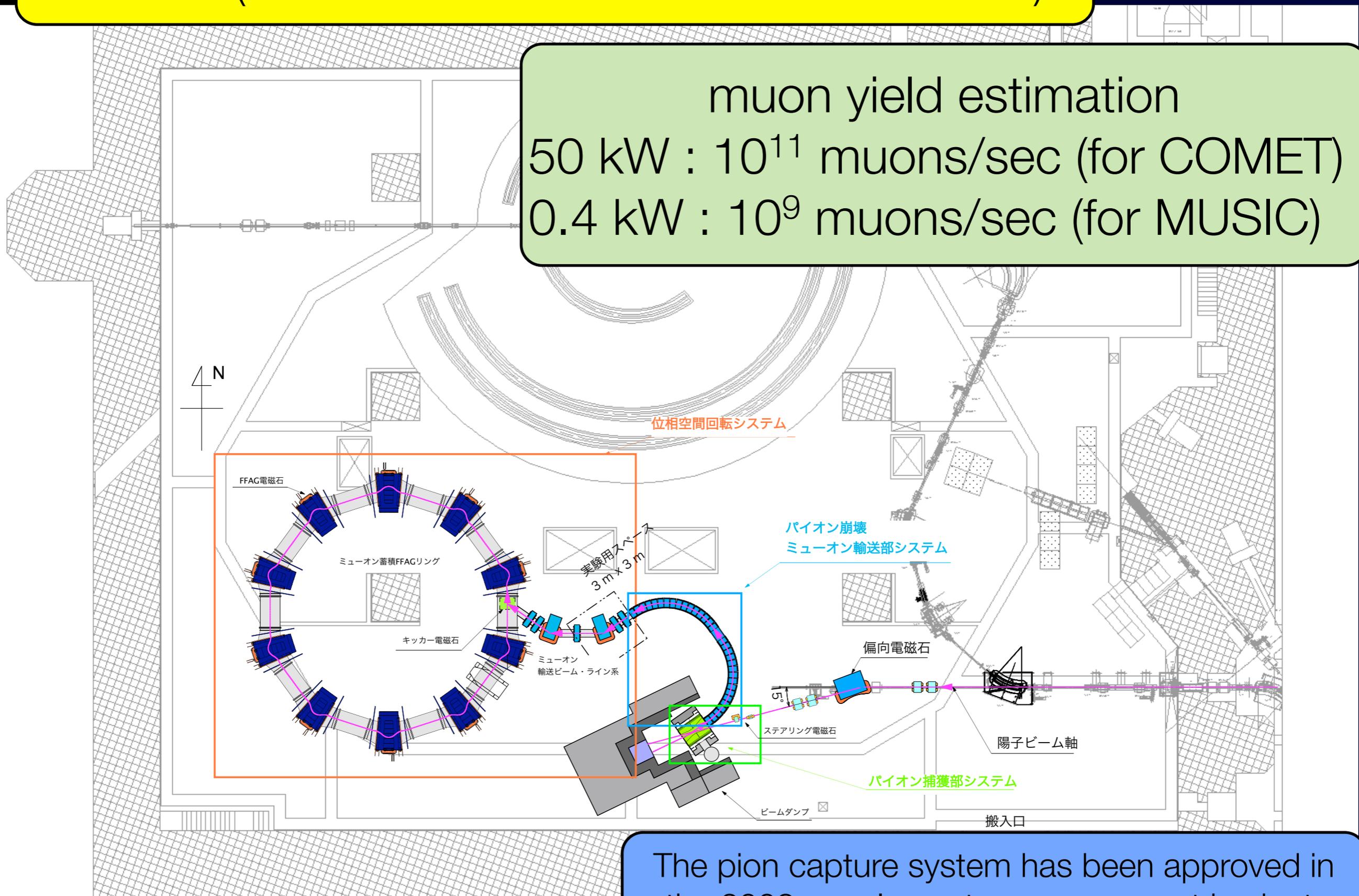


Muon Source with low proton power at Osaka U.?

PRISM-FFAG R&D

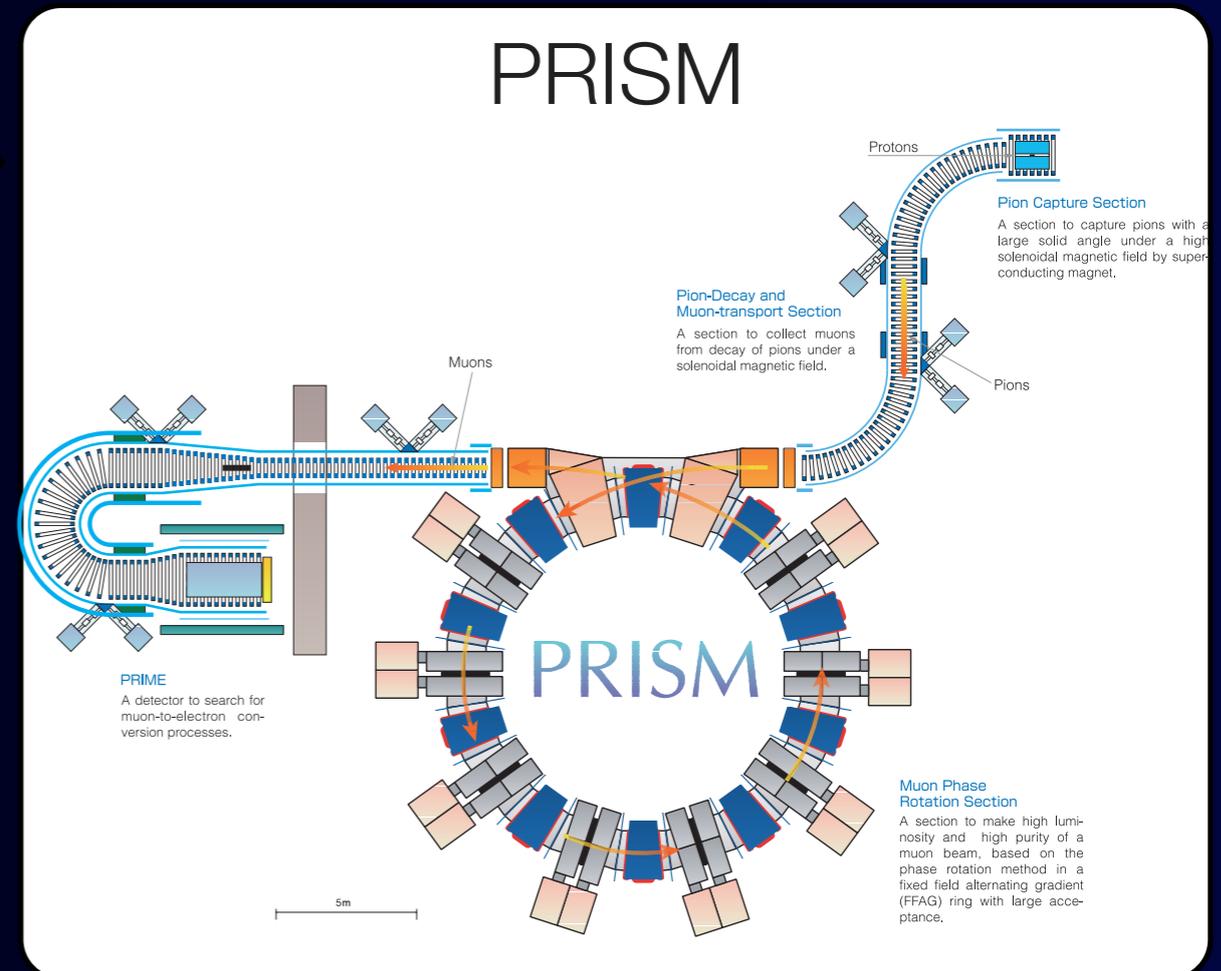
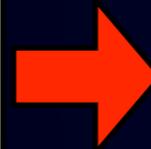
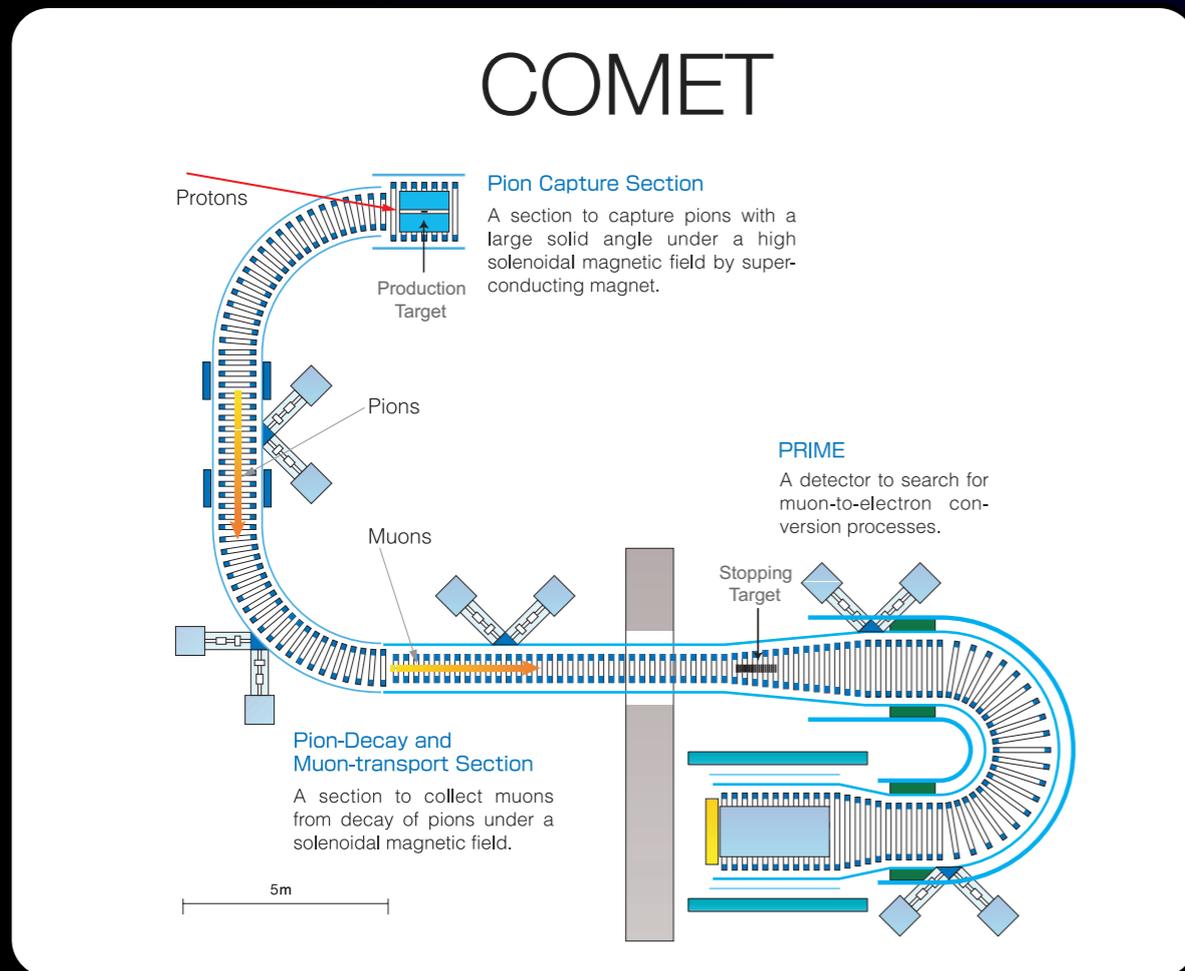
# MUSIC (=MUon Science International Center)

muon yield estimation  
50 kW :  $10^{11}$  muons/sec (for COMET)  
0.4 kW :  $10^9$  muons/sec (for MUSIC)



The pion capture system has been approved in the 2008 supplementary government budget.

# Long Future Prospects : From COMET to PRISM



$$B(\mu^- + Al \rightarrow e^- + Al) < 10^{-16}$$

- without a muon storage ring.
- with a slowly-extracted pulsed proton beam.
- doable at the J-PARC NP Hall.
- regarded as the first phase / MECO type
- Early realization

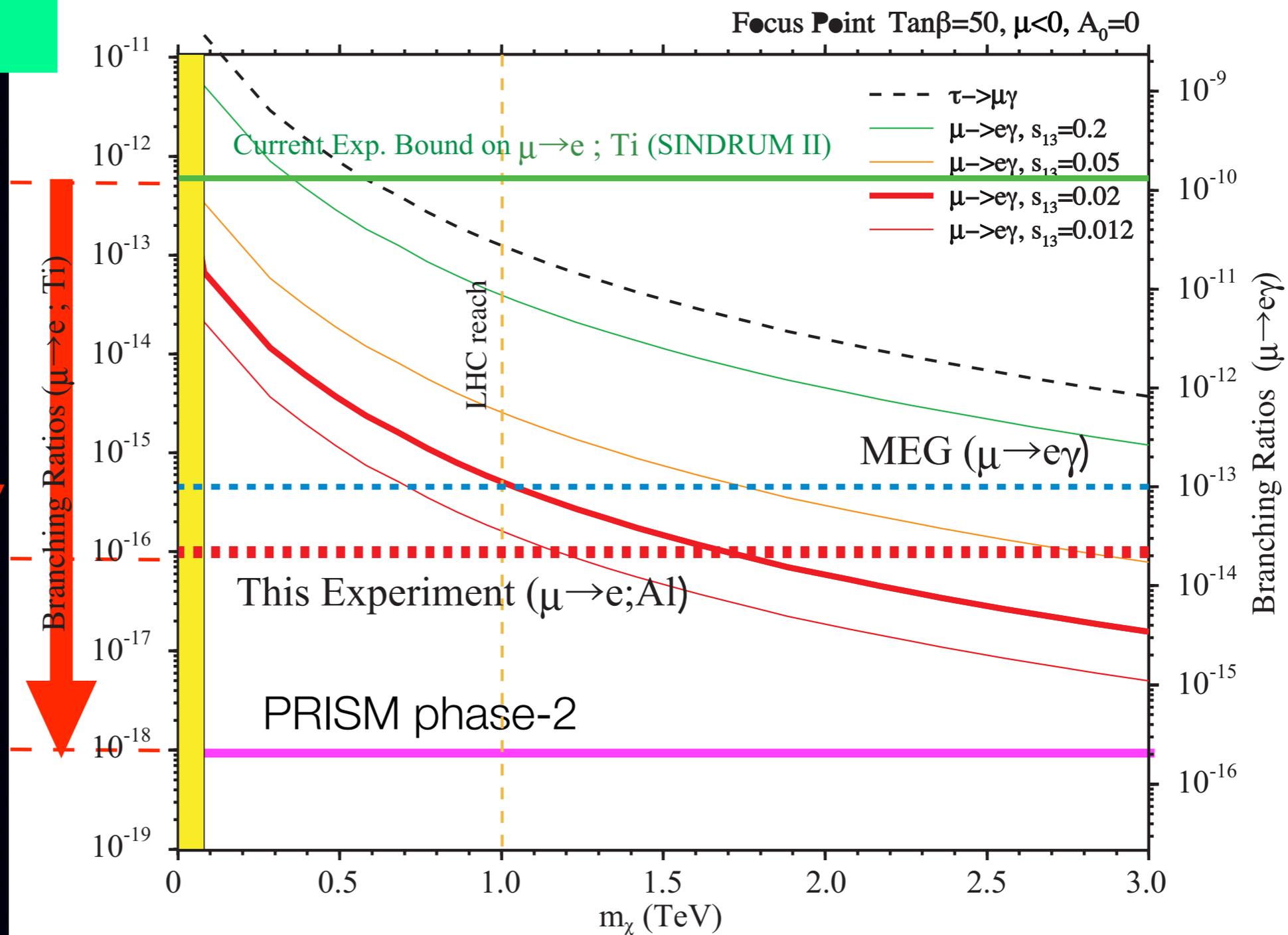
$$B(\mu^- + Ti \rightarrow e^- + Ti) < 10^{-18}$$

- with a fast-extracted pulsed proton beam.
- need a new beam-line and experimental hall.
- regarded as the second phase.
- Ultimate search

mSUGRA with right-handed neutrinos

will be improved by a factor of 10,000.

will be improved by a factor of 1,000,000.



Sensitivity Goal

$$B(\mu^- + Al \rightarrow e^- + Al) < 10^{-16}$$

$$B(\mu^- + Ti \rightarrow e^- + Ti) < 10^{-18}$$



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extreme  
**BEAM**

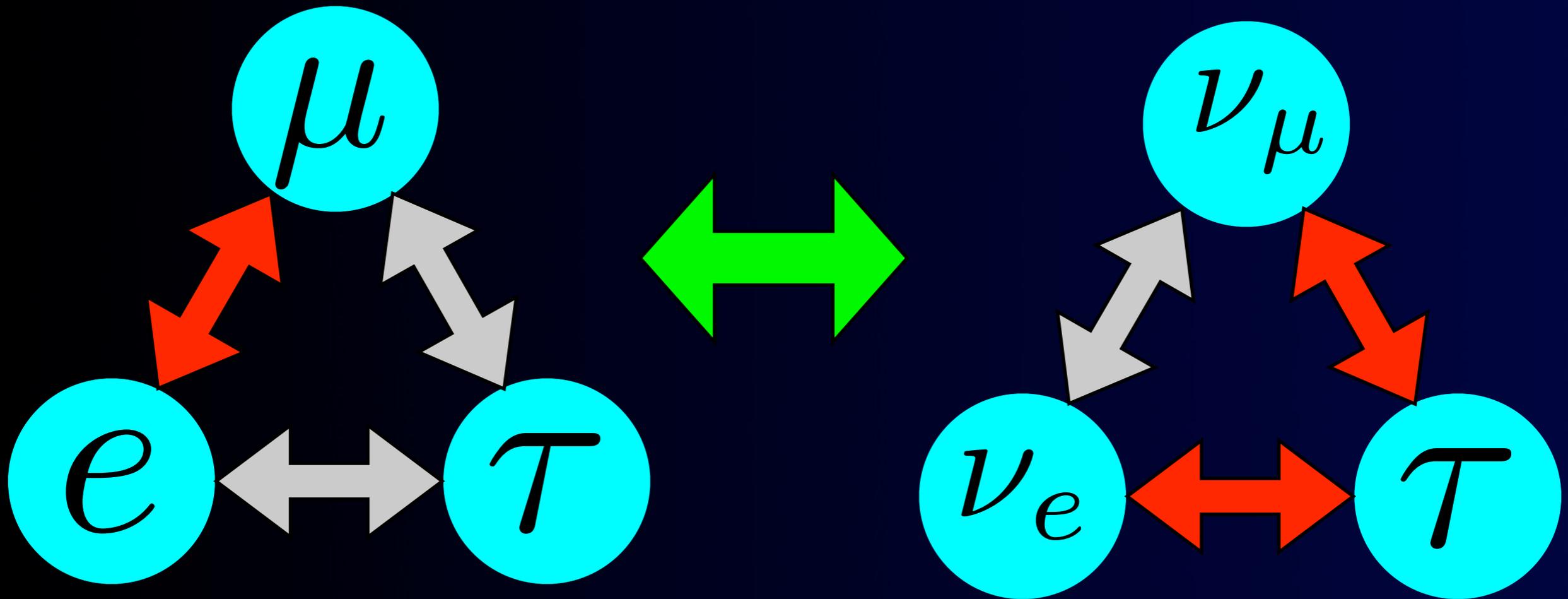
cLFV with Tau Leptons



# cLFV with Tau Leptons

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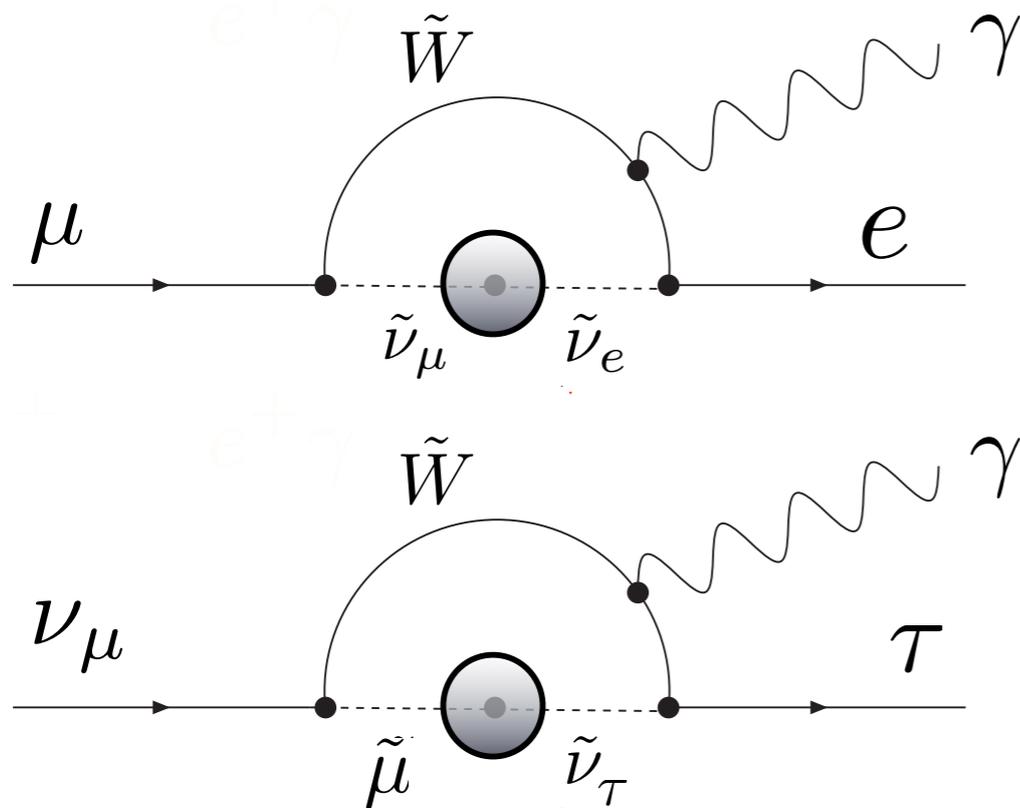
- How can we improve the limits between tau and muon (electron) ?
  - The Super B factory will aim at about 10-100 times luminosity.



If SU(2) symmetry in the weak doublet holds

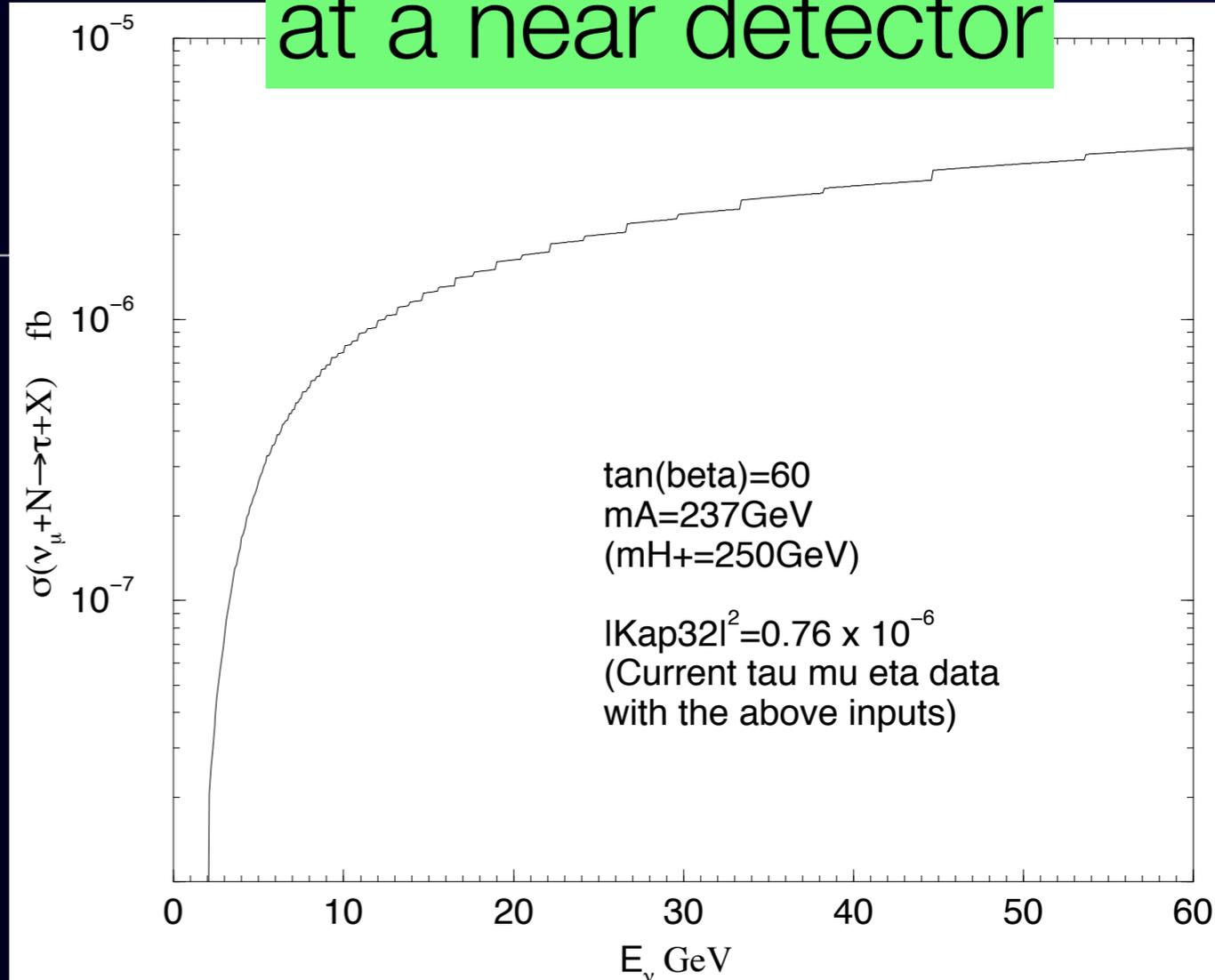
# Neutrino-induced Charged LFV Current

$$\nu_{\mu(e)} + N \rightarrow \tau + X$$



If SU(2) is valid in new physics, the two are related (constrained) one another.

at a near detector



- The present upper limit is obtained by tau rare decays at B factories.
- When  $E_\nu = 30$  GeV, the upper limit of the cross section is about  $10^{-6}$  fb.
- $10^{20}$  vs/year at a neutrino factory, a 100 kg (1 ton) detector,  $10^5$  ( $10^6$ ) events are expected.

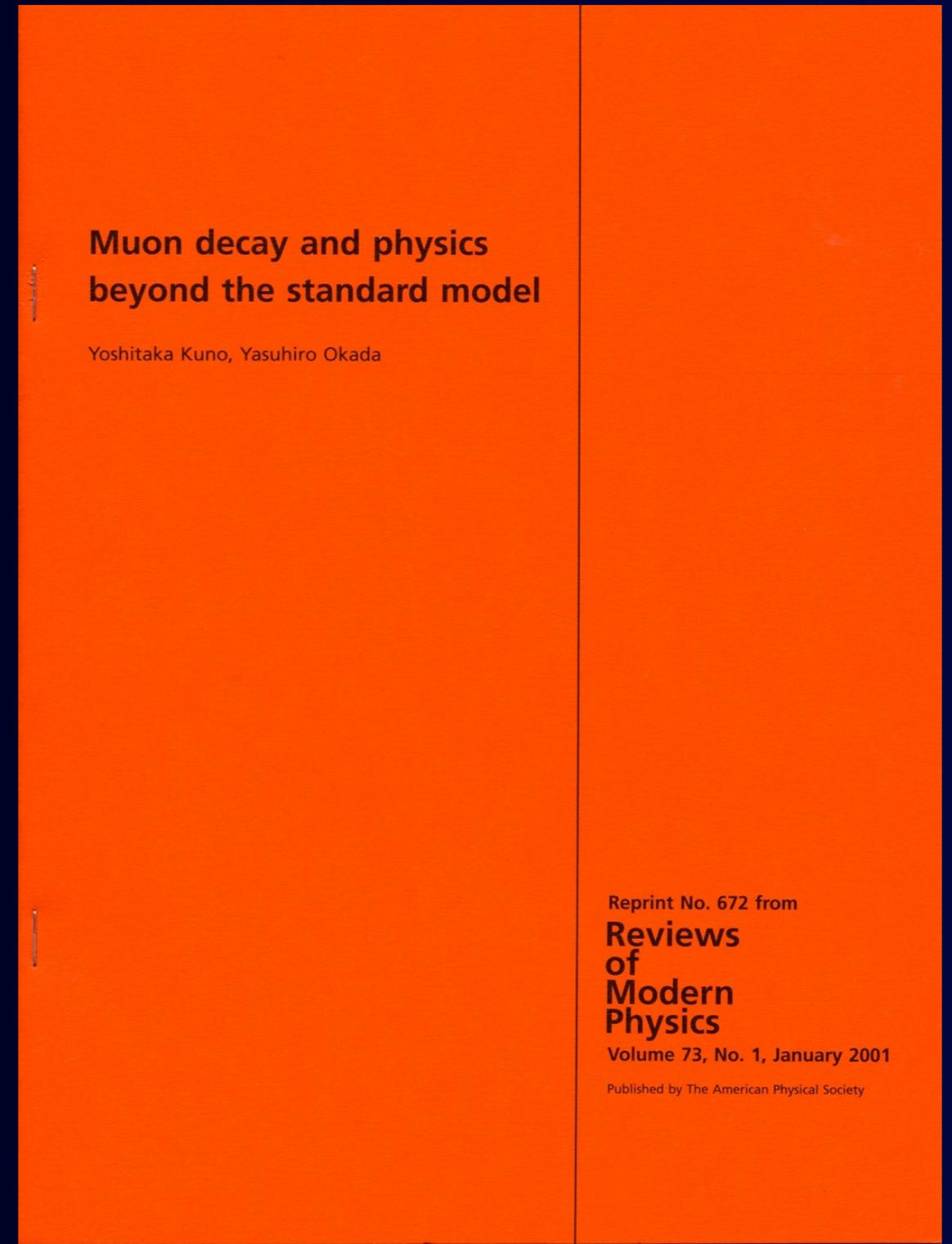
# For Further References

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## Muon decay and physics beyond the standard model

Yoshitaka Kuno and Yasuhiro Okada

Review of Modern Physics 73 (2001)



# Summary

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- Physics motivation of cLFV processes is robust and strong.
- The cLFV processes with muons are, for example,  $\mu \rightarrow e\gamma$  and  $\mu$ -e conversion.
- The MEG experiment to search for  $\mu \rightarrow e\gamma$  with sensitivity of  $10^{-13}$  is running.
- The future next step would be  $\mu$ -e conversion, where **Mu2E** (for  $10^{-16}$  sensitivity) in Fermilab and **COMET** (for  $10^{-16}$  sensitivity) in Japan are being planned. For further development, **PRISM/PRIME** (for  $10^{-18}$  sensitivity) are considered.

End of  
My Slides

